

# AP Microeconomics Study Guide

## Unit 4: Imperfect Competition

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# Introduction: Beyond Perfect Competition

Imperfect competition exists whenever a market violates the assumptions of perfect competition (many firms, identical products, no barriers to entry). We move from firms being **price takers** to firms being **price searchers** or **price makers**, meaning they have a downward-sloping demand curve and must choose their price.

## 1 Monopoly

### Characteristics

A pure monopoly is a single firm that is the sole seller of a product with no close substitutes.

- **Single Seller:** The firm IS the industry.
- **Unique Product:** No close substitutes.
- **High Barriers to Entry:** The key. Barriers can be natural (**natural monopoly** due to economies of scale), government-created (patents, licenses), or resource-based (control of a key input).

### Profit Maximization (The Quantitative Core)

A monopolist faces the market demand curve. To sell more, it must lower its price, leading to the crucial consequence: **Marginal Revenue (MR) is less than Price (P)**.

**The Intuition for  $MR < P$ :** This happens because of the **price effect**. To sell one more unit, the monopolist must lower the price *for all units* (not just the last one). The revenue gained from the new unit (**output effect**) is always partially offset by the revenue lost on all previous units (**price effect**).

**Quantitative Rule:** For a linear demand curve, the  $MR$  curve will always be **twice as steep** as the demand curve, originating from the same vertical intercept. (See Appendix for derivation.)

**The Profit-Maximizing Rule:** The monopolist maximizes profit by producing the quantity  $Q^*$  where:

$$MR = MC$$

1. Find the quantity  $Q^*$  where the  $MR$  and  $MC$  curves intersect.
2. Go **up** from  $Q^*$  to the **Demand Curve** to find the profit-maximizing price,  $P_m$ .
3. Find the Average Total Cost ( $ATC$ ) at  $Q^*$ .
4. Profit is calculated as:  $\Pi = (P_m - ATC) \cdot Q^*$ .

### Efficiency and Deadweight Loss

- **Allocative Inefficiency:** The monopolist produces where  $P_m > MC$ . Output is restricted to maintain a higher price, leading to a misallocation of resources ( $P = MC$  is the efficient point).
- **Deadweight Loss (DWL):** The triangle of lost surplus (consumer and producer) resulting from the restricted output ( $Q^*$ ) compared to the efficient output (where  $P = MC$ ).

**Perfect Price Discrimination:** A single-price monopoly is inefficient. However, if a monopolist can engage in **1st-degree (perfect) price discrimination**, charging each consumer their maximum willingness to pay, the firm's  $MR$  curve effectively becomes the  $D$  curve.

- The firm produces where  $P = MC$ , meaning output is **allocatively efficient (no deadweight loss!)**.

- The firm captures 100% of the total surplus (Consumer Surplus is zero).

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## 2 Monopolistic Competition

### Characteristics

This market structure combines elements of monopoly and perfect competition.

- **Many Firms and Low Barriers to Entry:** Like perfect competition.
- **Differentiated Products:** The key. Firms use branding, quality, or location to create a "mini-monopoly" over their specific variety, giving them a downward-sloping demand curve.

### Short-Run and Long-Run Equilibrium

- **Short Run:** The firm behaves exactly like a monopolist, maximizing profit where  $MR = MC$ , and setting price from the demand curve ( $P > MC$ ).
- **Long Run:** If profits are positive, new firms enter (low barriers). This entry shifts the demand curve of existing firms to the **left** until it is just **tangent** to the  $ATC$  curve.
- **Long-Run Outcome:**  $P = ATC$ , resulting in **zero economic profit**.

### Efficiency

- **Allocative Inefficiency:** In the long run,  $P > MC$ , so DWL still exists.
- **Productive Inefficiency:** The firm produces where  $P = ATC$  at the tangency point, which is **not** at the minimum of  $ATC$ .
- **Excess Capacity Theorem:** The difference between the firm's long-run output and the output at the minimum of  $ATC$  is called "excess capacity."

**The Value of Variety:** While technically inefficient ( $P > MC$  and  $P \neq \min ATC$ ), many economists view the resulting DWL as the small trade-off for the massive benefit of **product variety** and consumer choice.

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## 3 Oligopoly and Game Theory

### Characteristics

A market dominated by a few large, profitable firms.

- **Few Large Firms:** (e.g., cell phone carriers, car manufacturers).
- **Interdependence:** The **defining** characteristic. Each firm's profit depends not just on its own actions, but also on the actions of the rival firms. This leads to strategic decision-making.
- **High Barriers to Entry:** Necessary to maintain the "few large firms" structure.

## Game Theory Basics

Game theory models strategic interdependence using a payoff matrix.

- **Payoff Matrix:** A table showing the profits for each firm for every possible combination of strategies.
- **Dominant Strategy:** A strategy that yields the highest payoff for a player, **regardless** of what the other player chooses.
- **Nash Equilibrium:** An outcome where no player has an incentive to **unilaterally** change their strategy. This is the non-cooperative, stable outcome.

**Example: The Prisoner's Dilemma** Two firms, A and B, must decide whether to Price Low (compete) or Price High (collude). (Payoffs: Firm A, Firm B)

|                    | Firm B             |                    |
|--------------------|--------------------|--------------------|
|                    | Price Low          | Price High         |
| Firm A: Price Low  | (\$10, \$10)       | <b>(\$30, \$0)</b> |
| Firm A: Price High | <b>(\$0, \$30)</b> | (\$20, \$20)       |

In this case, **Price Low** is the dominant strategy for both firms, leading to the Nash Equilibrium (\$10, \$10), which is worse for both than the cooperative outcome (\$20, \$20). This illustrates the incentive to cheat on collusion.

**Bertrand vs. Cournot** The **Bertrand Model** (price competition) with identical products predicts that the price will fall to  $P = MC$  (the perfectly competitive outcome) even with only two firms, due to fierce undercutting. The **Cournot Model** (quantity competition) predicts an outcome between monopoly and perfect competition. This illustrates how the \*type\* of competition (price vs. quantity) matters more than the number of firms in some cases.

## 4 Efficiency Comparisons Across Market Structures

Table 1: Market Structure Long-Run Comparison

| Characteristic                     | Perfect Comp. | Monopolistic Comp.   | Oligopoly          | Monopoly        |
|------------------------------------|---------------|----------------------|--------------------|-----------------|
| Number of Firms                    | Very Many     | Many                 | Few                | One             |
| Product Type                       | Identical     | Differentiated       | Identical or Diff. | Unique          |
| Barriers to Entry                  | None          | Low                  | High               | Very High       |
| Long-Run Profit ( $\Pi$ )          | $\Pi = 0$     | $\Pi = 0$            | $\Pi \geq 0$       | $\Pi \geq 0$    |
| Allocative Eff? ( $P = MC$ )       | <b>Yes</b>    | No ( $P > MC$ )      | No ( $P > MC$ )    | No ( $P > MC$ ) |
| Productive Eff? ( $P = \min ATC$ ) | <b>Yes</b>    | No (Excess Capacity) | No                 | No              |
| Deadweight Loss (DWL)              | <b>None</b>   | Yes                  | Yes                | Yes             |

**Key Takeaway:** Only perfect competition achieves both allocative and productive efficiency. All imperfectly competitive markets fail on both counts and generate deadweight loss (DWL).

**Dynamic Efficiency:** Economists like Joseph Schumpeter argued that the high, short-term profits of monopolies are the necessary fuel for **innovation**. Firms pursue monopoly status to gain high profits, driving a process of **creative destruction** where new innovations replace old ones. This long-run technological progress is a form of **dynamic efficiency** that static models of DWL fail to capture.

## A Appendix: Quantitative Derivations

### Derivation of $MR < P$ for a Monopolist

Total Revenue (TR) is defined as  $TR = P \cdot Q$ . For a monopolist, Price  $P$  is a function of Quantity  $Q$ , represented by the demand function  $P(Q)$ .

$$TR = P(Q) \cdot Q$$

Marginal Revenue (MR) is the change in TR with respect to a change in  $Q$ ,  $\frac{d(TR)}{dQ}$ . Using the product rule from calculus:

$$MR = \frac{d(TR)}{dQ} = \underbrace{\frac{dP}{dQ} \cdot Q}_{\text{Price Effect}} + \underbrace{P(Q) \cdot 1}_{\text{Output Effect}}$$

Since the demand curve is downward sloping, the term  $\frac{dP}{dQ}$  is negative.

$$MR = P + (\text{a negative number})$$

Therefore,  $MR < P$ .

### Derivation of the "Twice as Steep" Rule

Consider a linear demand curve (inverse demand function):

$$P = a - bQ$$

where  $a$  is the vertical intercept and  $-b$  is the slope.

1. **Total Revenue (TR):** Substitute  $P$  into the TR equation:

$$TR = P \cdot Q = (a - bQ)Q = aQ - bQ^2$$

2. **Marginal Revenue (MR):** Take the first derivative of TR with respect to  $Q$ :

$$MR = \frac{d(TR)}{dQ} = a - 2bQ$$

**Conclusion:** The  $MR$  equation ( $a - 2bQ$ ) has the same vertical intercept ( $a$ ) as the demand equation ( $a - bQ$ ), but its slope is  $-2b$ , which is twice as steep as the demand curve's slope ( $-b$ ).