



Hydrogen and galaxies (10 points)

Part A - Introduction

Bohr model

A.1 (0.2pt)

$$v =$$

A.2 (0.5pt)

Expression : $r_1 =$

Numerical value : $r_1 =$

$$v_1 =$$

A.3 (0.5pt)

$$E_n =$$

$$E_1 =$$

Numerical value : $E_1 =$

Hydrogen fine and hyperfine structure

A.4 (0.5pt)

$$B_1 =$$

A.5 (0.5pt)

$$\Delta E_F =$$

Expression of $\lambda_{\text{HF}} =$

Value of $\lambda_{\text{HF}} =$

Part B - Rotation curves of galaxies

B.1 (0.2pt)

$$v_c =$$

**B.2 (0.5pt)**

$$M_b =$$

B.3 (1.8pt)

$$k_1 =$$

$$k_2 =$$

$$v_{c,m}(r \ll r_m) \simeq$$

$$v_{c,m}(r \gg r_m) \simeq$$

$$M_m(r \gg r_m) \simeq$$

$$M_{\text{in the figure}} =$$

Part C - Mass distribution in our galaxy**C.1 (0.5pt)**

Vertical motion equation :

$$\omega_0 =$$

C.2 (0.6pt)

$$\varphi_0 =$$

$$v_c(r) =$$

C.3 (0.7pt)

$$v_{rE/S} =$$

$$R =$$

C.4 (0.6pt)

$$v_{r,1} =$$

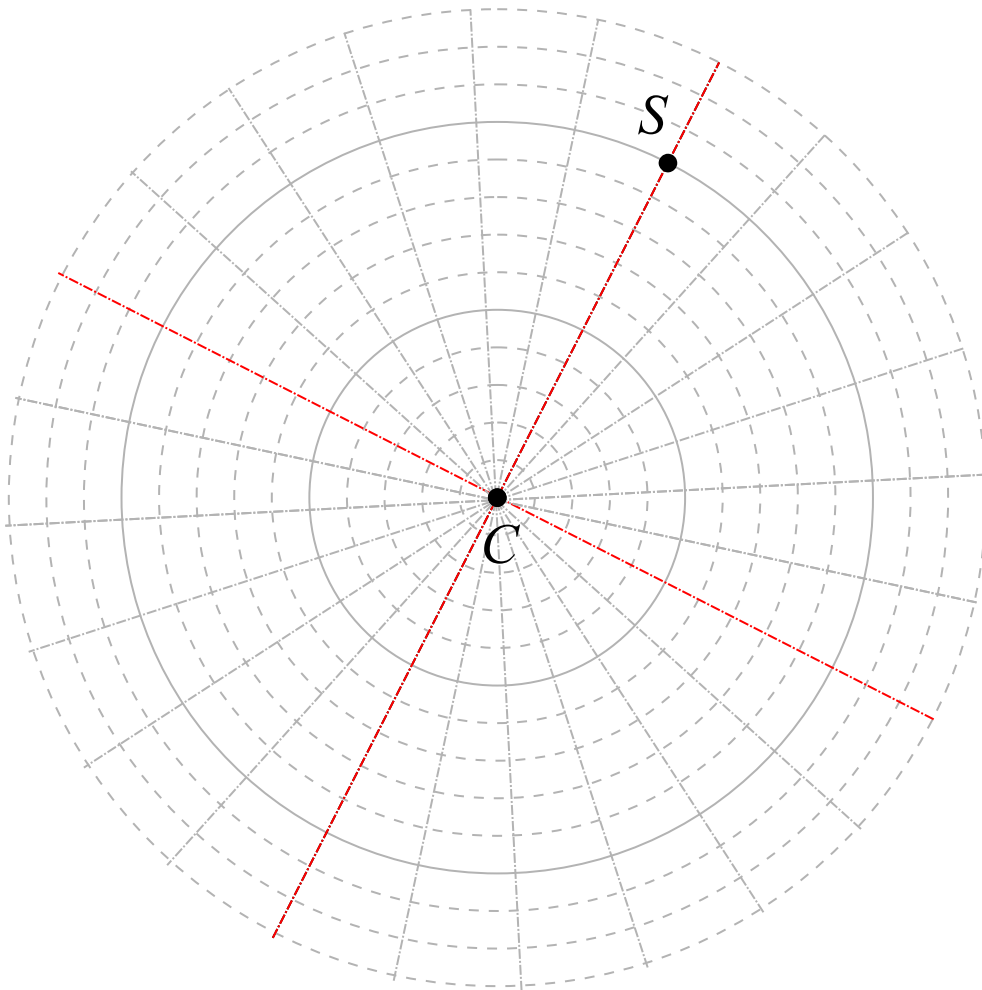
$$v_{r,2} =$$

$$v_{r,3} =$$

$$R_1 =$$

$$R_2 =$$

$$R_3 =$$

C.5 (0.6pt)

Deduction :

Part D - Tully-Fisher relation and Mond theory**D.1** (0.4pt) $\eta =$ $\gamma =$ $\gamma_{TF} =$



D.2 (0.2pt)

$$a_m =$$

D.3 (0.8pt)

if $a \ll a_0$ then $\gamma_{\text{Mond}} =$

$$a_0 =$$

D.4 (0.9pt)

$$v_c(r) =$$

$$v_c(r) =$$