

# Guide to Day Count Conventions and Interest Payments

Rohan Dutta

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# Interest

Interest payments are calculated by,

$$\text{Interest} = \frac{P \times R \times \text{Days}}{\text{Denominator}}$$

Where,

P = Principal amount, R = Interest rate in % p. a.

Days and Denominator vary across day counting conventions. The ratio  $\frac{\text{Days}}{\text{Denominator}}$  can also be called the Year Fraction, the fraction of the year covered by the accrual period, which scales the per annum interest. e.g. interest of 5% per annum for  $\frac{1}{2}$  year, has

$$\text{YF} = \frac{1}{2}, \text{ and Interest} = P \times 5\% \times \frac{1}{2}$$

## Day count conventions

### ACT/360

Typically used in USD/EUR/CHF money markets and repo.

- Day count = Actual day count
- Denominator = 360 (Fixed)

#### Example:

Leap: 15 Dec 2023 to 15 Mar 2024 → 91 days

$$\text{Interest} = \frac{(100M \times 5\% \times 91)}{360} = 1,263,888.89$$

Non-leap: 15 Dec 2024 to 15 Mar 2025 → 90 Days

$$\text{Interest} = \frac{(100M \times 5\% \times 90)}{360} = 1,250,000.00$$

### ACT/365 Fixed

Most common in GBP/JPY Money Markets, most non-US/EU Gov. Bonds.

- Day count = Actual day count
- Denominator = 365 (Fixed)

#### Example:

Leap: 15 Dec 2023 to 15 Mar 2024 → 91 days

$$\text{Interest} = \frac{100M \times 5\% \times 91}{365} = 1,246,575.34$$

Non-leap: 15 Dec 2024 to 15 Mar 2025 → 90 Days

$$\text{Interest} = \frac{100M \times 5\% \times 90}{365} = 1,232,876.71$$

For the same period, ACT/365 interest is  $\approx 98.6\%$  (slightly less) of owed ACT/360 interest.  $(\frac{360}{365} \approx 0.986)$

**ACT/365L**

Usually seen in GBP FRN's.

- Day count = Actual
- Denominator depends on coupon frequency,
  - o Annual: Denominator = 366 if 29 Feb falls within the period (excluding start date) else 365
  - o Non-Annual: Denominator = 366 if period end is in a leap year, else 365.

**Example:**

Leap: 15 Dec 2023 to 15 Mar 2024 → 91 days

D2 = 15 March 2024, leap year → Denominator = 366

$$\text{Interest} = \frac{100M \times 5\% \times 91}{366} = 1,243,169.40$$

Non-leap: 15 Dec 2024 to 15 Mar 2025 → 90 Days

D2 = 15 March 2025, not in leap year → denominator = 365

$$\text{Interest} = \frac{100M \times 5\% \times 90}{365} = 1,232,876.71$$

**ACT/ACT (ISDA)**

Commonly used in US treasuries and long-dated derivatives.

- Day count = actual day count split by year
- Denominator = actual days in the year (366 for leap years otherwise 365)

For trades with a leap year component, the interest calculation is split into the constituent parts.

**Example:**

Leap: 15 Dec 2023 to 15 Mar 2024

Split:

- 2023: 16 days, denominator = 365
- 2024: 75 days, denominator = 366

Calculate the interest for each constituent year,

$$I_{23} = \frac{100M \times 5\% \times 16}{365} = 219,178.08$$

$$I_{24} = \frac{100M \times 5\% \times 75}{366} = 1,024,590.16$$

$$\text{Interest} = I_{23} + I_{24} = 1,243,768.25$$

Non-leap: 15 Dec 2024 to 15 Mar 2025

Split:

- 2024: 16 days, denominator = 366
- 2025: 74 days, denominator = 365

$$I_{24} = \frac{100M \times 5\% \times 16}{366} = 218,579.24$$

$$I_{25} = \frac{100M \times 5\% \times 74}{365} = 1,013,698.63$$

$$\text{Interest} = I_{24} + I_{25} = 1,232,277.87$$

ACT/ACT splits the accrual period at the calendar year boundary, dividing each portion by its own year's actual length (365 or 366). Alternatively, ACT/365L uses a single denominator for the whole period, choosing 365 or 366 by rule based on coupon frequency and where the leap day falls.

Note: A separate variant, ACT/ACT ICMA, is used for most European government bonds (Bunds, OATs, BTPs, Gilts). ICMA divides actual days by (frequency × actual days in the reference coupon period), which produces exactly 1/Frequency of a year for every regular coupon period. Because it requires knowledge of the bond's coupon schedule, it is not covered in detail here.

## 30/360 Day Count Formula

All 30/360 conventions assume each month to have 30 days, and a 360-day year. The base day count formula is:

$$\text{Days} = (Y_2 - Y_1) \times 360 + (M_2 - M_1) \times 30 + (D_2 - D_1)$$

Conventions differ in how D1 and D2 are adjusted, before applying the formula.

### US Bond basis

Typically used in US corporate bonds, municipal bonds; seen as collateral in USD Repo.

- Adjustment rules (in order)
  - o  $D_1 = \min(D_1, 30)$
  - o If  $D_2 = 31$  **and**  $D_1 \geq 30$ , set  $D_2 = 30$

#### Example:

Period: 15 Jan 2026 – 31 Jan 2026

$$\text{Days} = (2026 - 2026) \times 360 + (1 - 1) \times 30 + (31 - 15) = 16$$

$$\text{Interest} = \frac{100M \times 5\% \times 16}{360} = 222,222.22$$

### 30E/360

Typically used in Eurobonds and european corporate bonds; seen as collateral in EUR Repo.

- If  $D_1 = 31 \rightarrow$  set to 30
- If  $D_2 = 31 \rightarrow$  set to 30

Also known as the Eurobond basis.

#### Example:

Period: 15 Jan 2026 – 31 Jan 2026

(Adjusted Equivalent: 15 Jan 2026 – 30 Jan 2026)

$$\text{Days} = (2026 - 2026) \times 360 + (1 - 1) \times 30 + (30 - 15) = 15$$

$$\text{Interest} = \frac{100M \times 5\% \times 15}{360} = 208,333.33$$

The two conventions only diverge when exactly one of the dates is the 31<sup>st</sup>. This arises due the US basis allowing months to end on the 31<sup>st</sup>. As seen in the example, a period of 15 Jan to 31 Jan

would have 16 days according to the Bond Basis convention, whereas the 30E/360 snaps the maturity date to 30 Jan, and gives 15 days.

This produces a small quirk, for two “equivalent”, end of month February trades, the one starting Feb 29<sup>th</sup> has one less accrual day vs one starting Feb 28<sup>th</sup> (Non-leap year) according to the day count formula.

### 30E/360 ISDA

Rarely used outside specific OTC derivatives.

Adjustment Rules:

- If D1 = 31 or D1 is last day of Feb
  - o Set D1 = 30
  - o Otherwise D1 = D1
- If D2 = 31 or D2 is last day of Feb but not the maturity date (e.g. coupon payment) (if maturity on Feb28/29 then D2 = 28/29 respectively)
  - o Set D2 to 30
  - o Otherwise D2 = D2

## Differences Across Conventions

Convention	Days Basis	Denominator	Special Handling
ACT/360	Actual	360	None
ACT/365 Fixed	Actual	365	Fixed year
ACT/ACT ISDA	Actual	Split by year	Sum of constituents
ACT/365L	Actual	365 or 366	Leap day
30/360 US	30-day months	360	US adjustments
30E/360	30-day months	360	31 snapped to 30
30E/360 ISDA	30-day months	360	EOM handling

# Date ordering

Given a value date, maturity date and payment frequency, construct a schedule of intermediate payment dates. There are two approaches:

## Forward generation

Start from the value date, step forward at the specified frequency. The leftover period becomes the back stub and is paid at the end.

## Back generation

Start from maturity date and step backwards at the specified frequency. The leftover period becomes the front stub and is paid at the start.

### Example:

29 Jan - Aug 15 (Non-Leap)

Period	Forward Generation	Back Generation
1	29 Jan – 28 Feb (Feb has no 29th → adjusted)	29 Jan – 15 Feb (Front Stub)
2	28 Feb – 29 Mar (rolls back to scheduled 29th)	15 Feb – 15 Mar
3	29 Mar – 29 Apr	15 Mar – 15 Apr
4	29 Apr – 29 May	15 Apr – 15 May
5	29 May – 29 June	15 May – 15 June
6	29 June – 29 July	15 June – 15 July
7	29 July – 15 Aug (Back Stub)	15 July – 15 Aug

# Date rolling

Date rolling answers the question: What do I do when the scheduled payment date lands on a non-business day?

- Following
  - Push it forward to the next possible business day.
- Modified following
  - Push it forward to the next possible business day,
  - UNLESS: the next business day is a new month, then roll it back to the previous business day.
- Previous
  - Roll the date back to the previous business day.
- Modified previous
  - Roll the date back to the previous business day.
  - UNLESS: the previous business day is in the previous month, then roll it forward to the next business day