

# CONSUMER DIVERSITY IN SENSORY EVALUATION DATA

**John C. Castura**

VP Innovation & Research

AGROSTAT 2018, édition 2018



Decisions related to experimental design and statistical analysis in sensory evaluation are often guided by standard practices.

Does a study that is designed and analyzed in a manner that is consistent with these practices always make sense?

**“A foolish consistency is  
the hobgoblin of little  
minds...”**



**Ralph Waldo Emerson**  
1841

A young boy wearing a baseball cap and a red and white striped shirt is sitting at a table, eating a sandwich. In the foreground, there is a plate with a sandwich and some fries, and two condiment bottles (ketchup and mustard) on the table. The background is blurred.

Who is an  
“average consumer”?

# Part I: Hedonic data

A vibrant, crowded street scene, likely Istiklal Street in Istanbul, during a festive period. The street is lined with buildings adorned with numerous Christmas lights, stars, and decorative garlands. A red and white tram is visible in the center of the street, surrounded by a dense crowd of people. The atmosphere is festive and bustling.

# Part I: Consumer acceptance





1



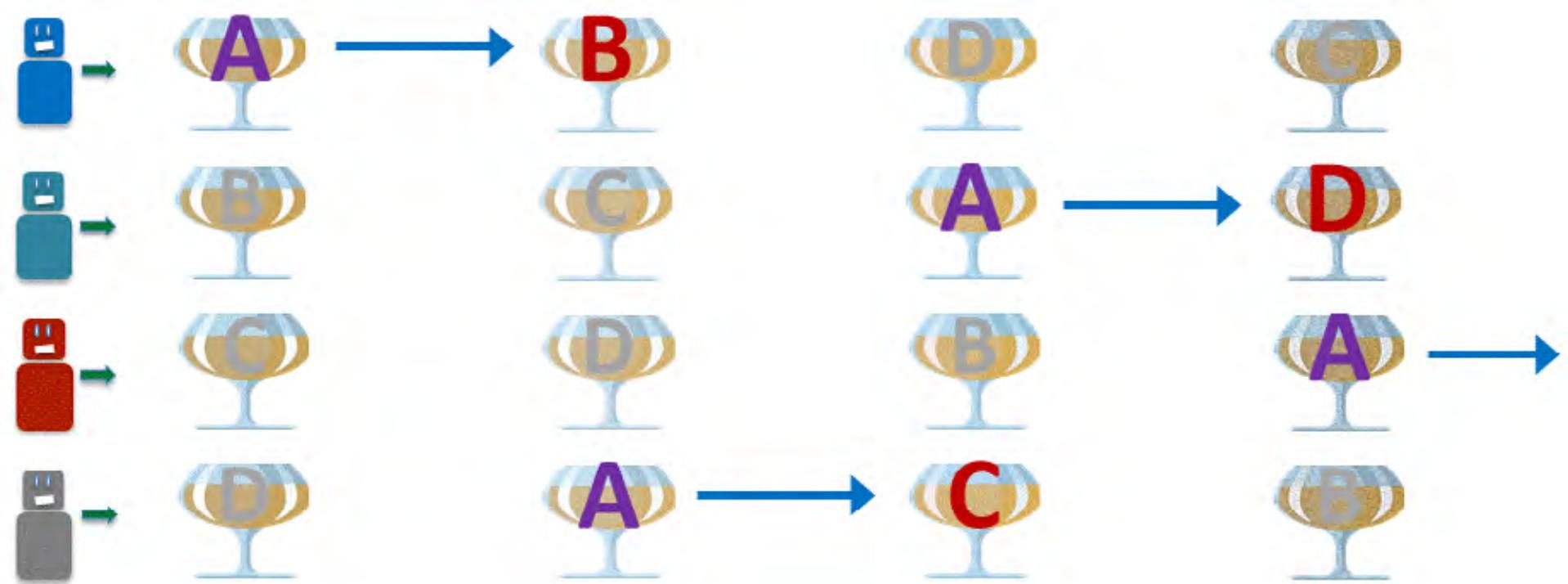
1

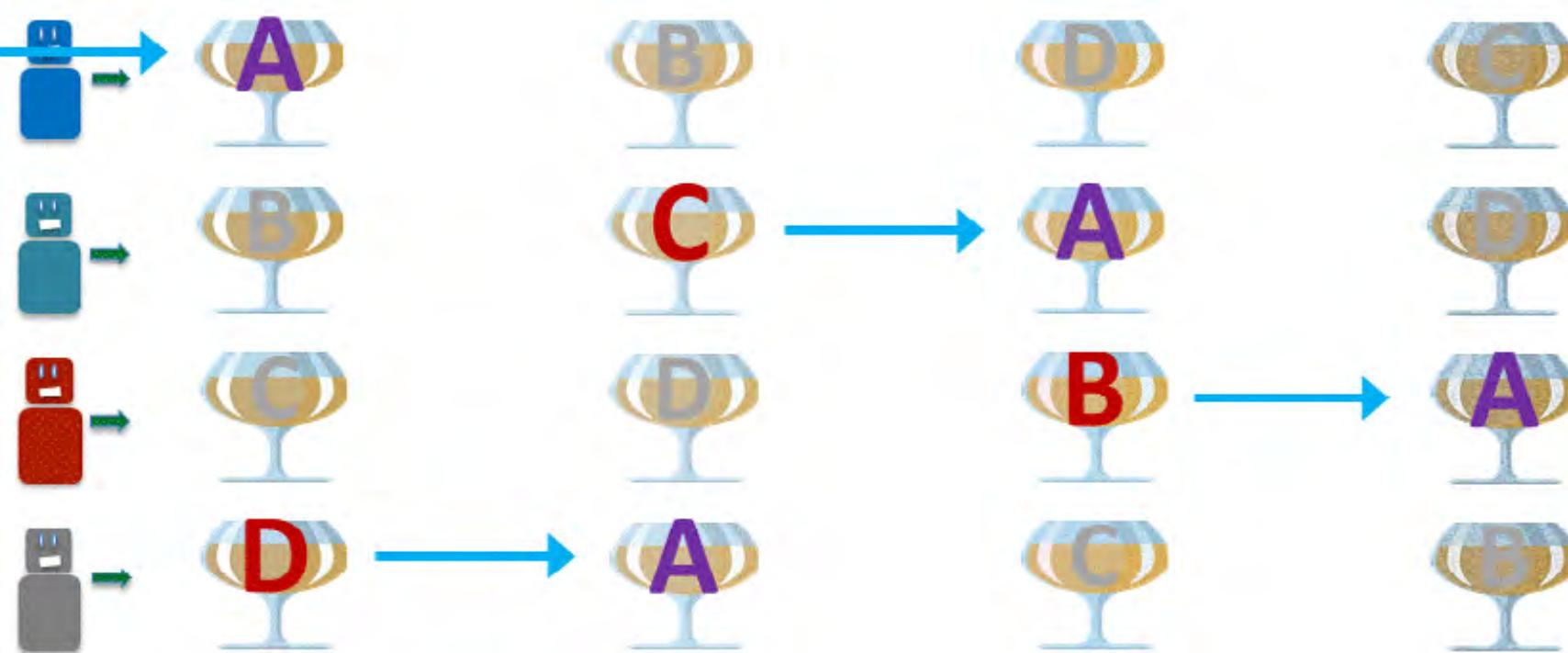


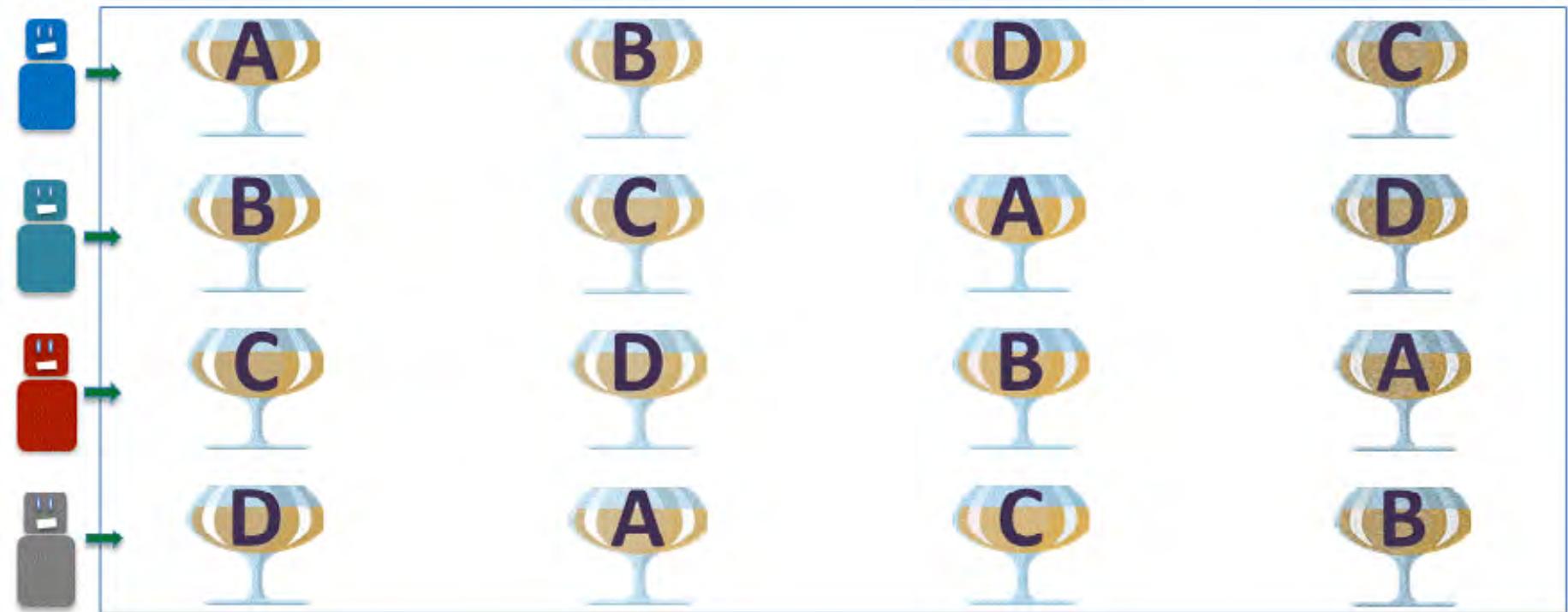
1



1







Williams design (4 treatments)

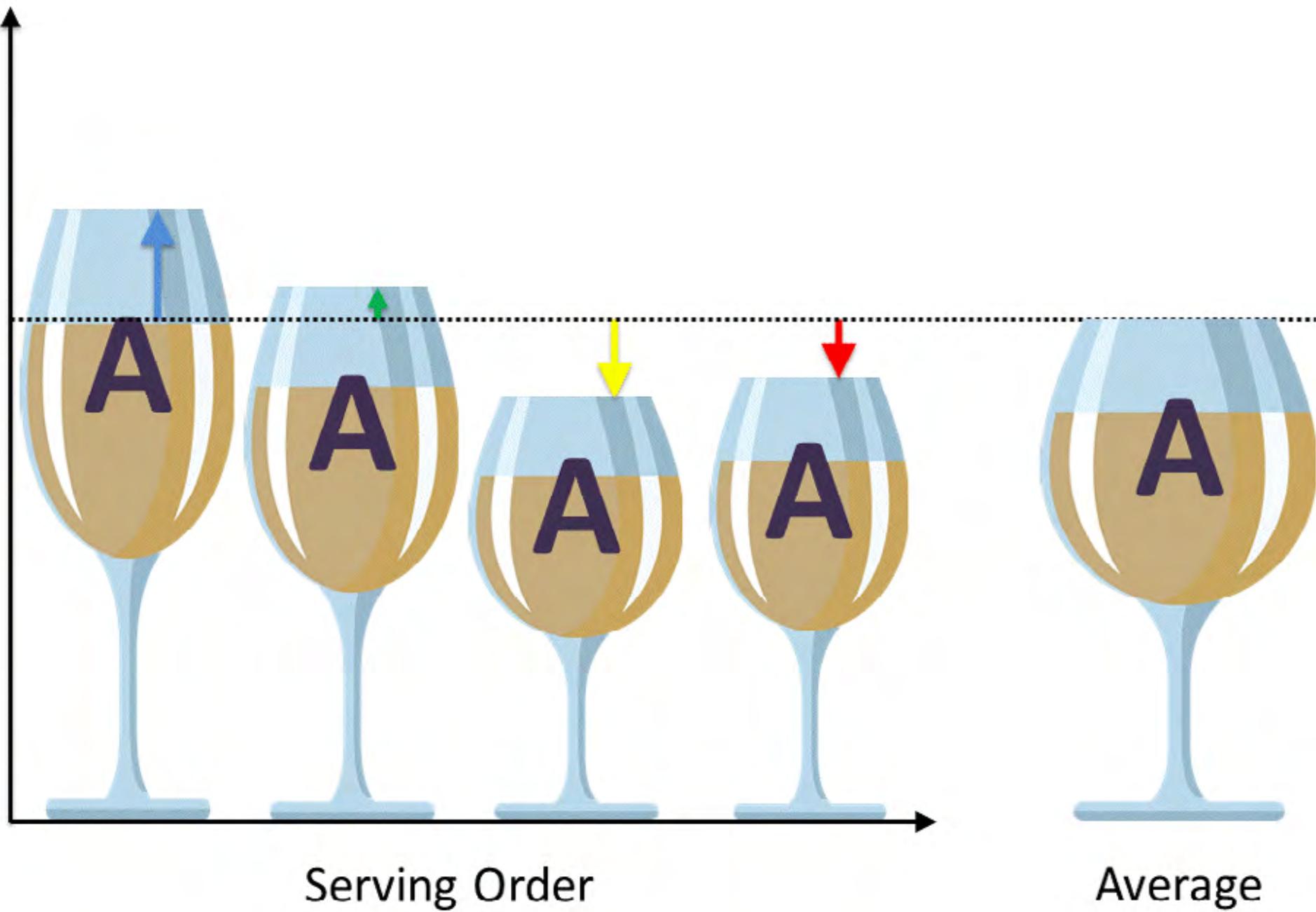
Blue	A	B	D	C
Blue	B	C	A	D
Red	C	D	B	A
Grey	D	A	C	B
<hr/>				
Purple	B	A	C	D
Yellow	A	D	B	C
Green	D	C	A	B
Red	C	B	D	A

# Truth

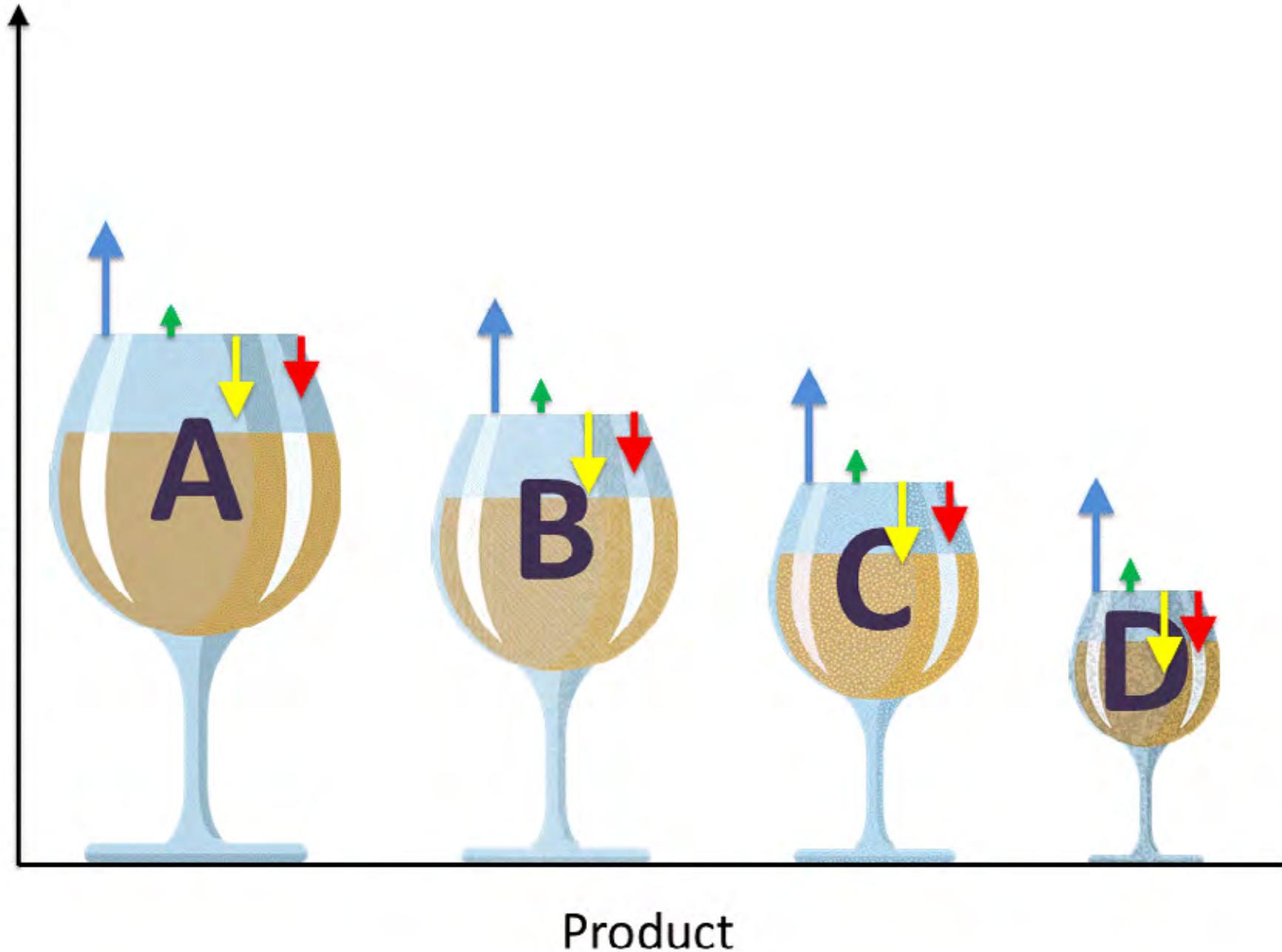
Liking



Product



Average Liking



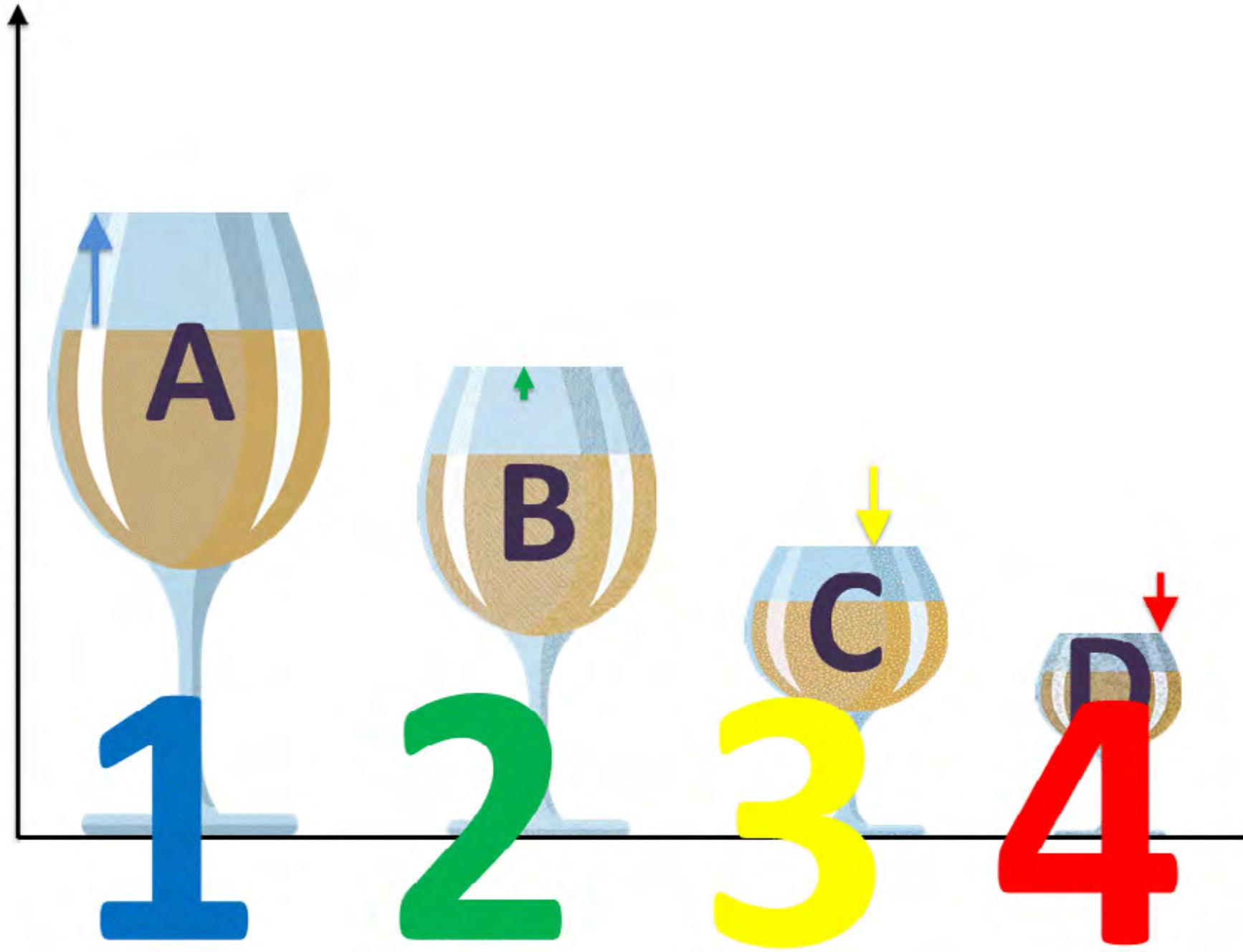


1

2

3

Average Liking



Average Liking



2



3



4





Liking

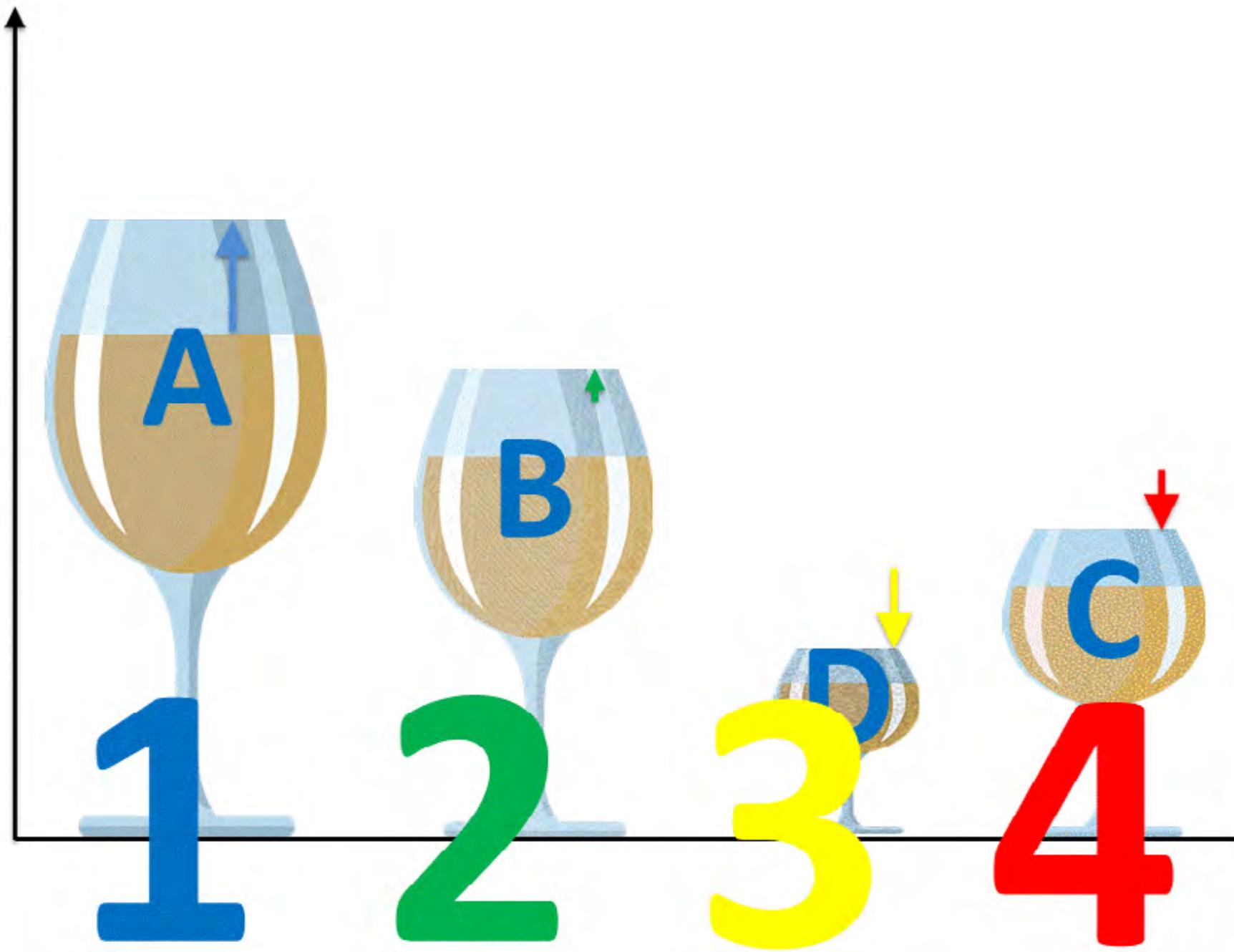
1

2

3

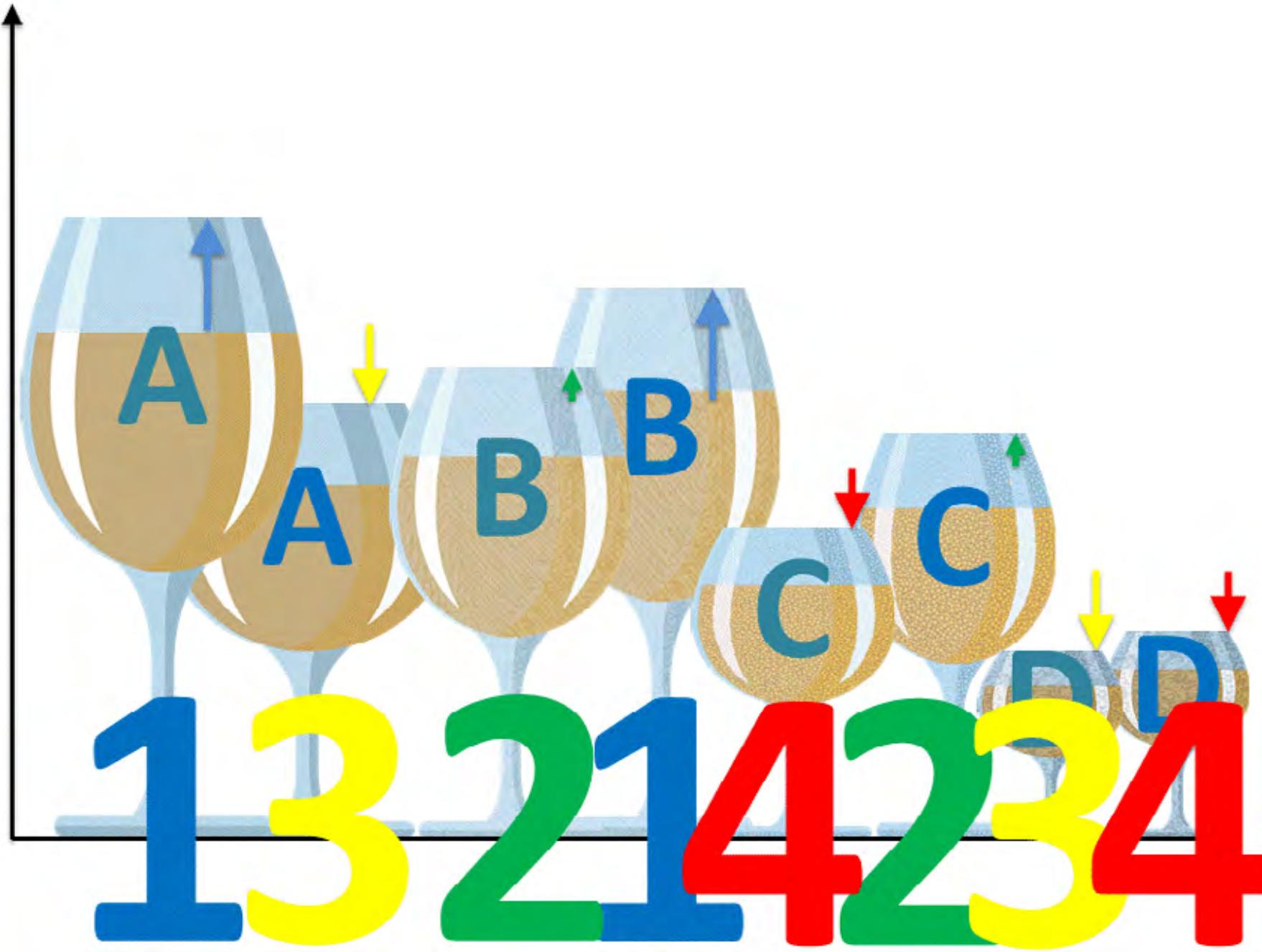
4

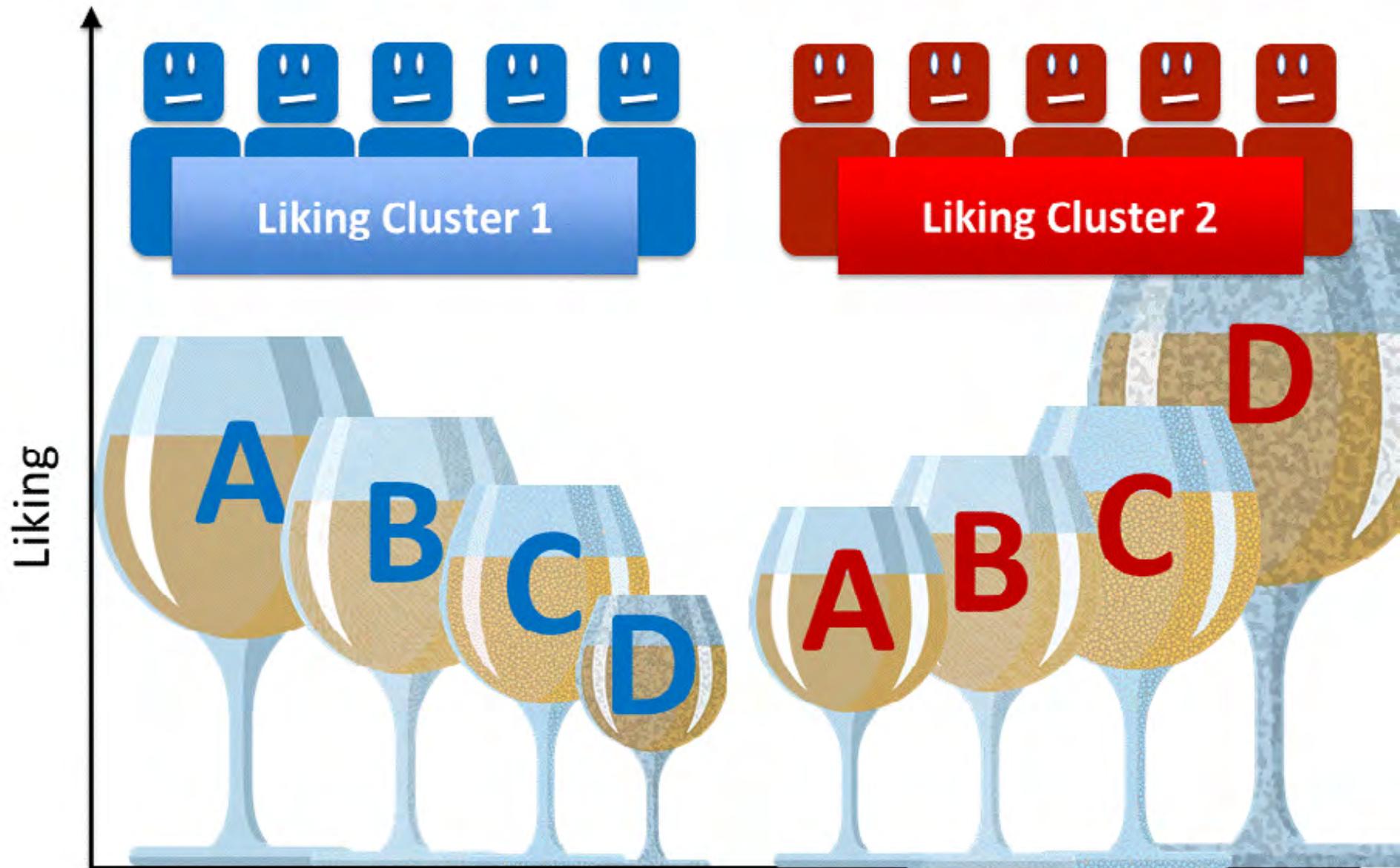
Liking



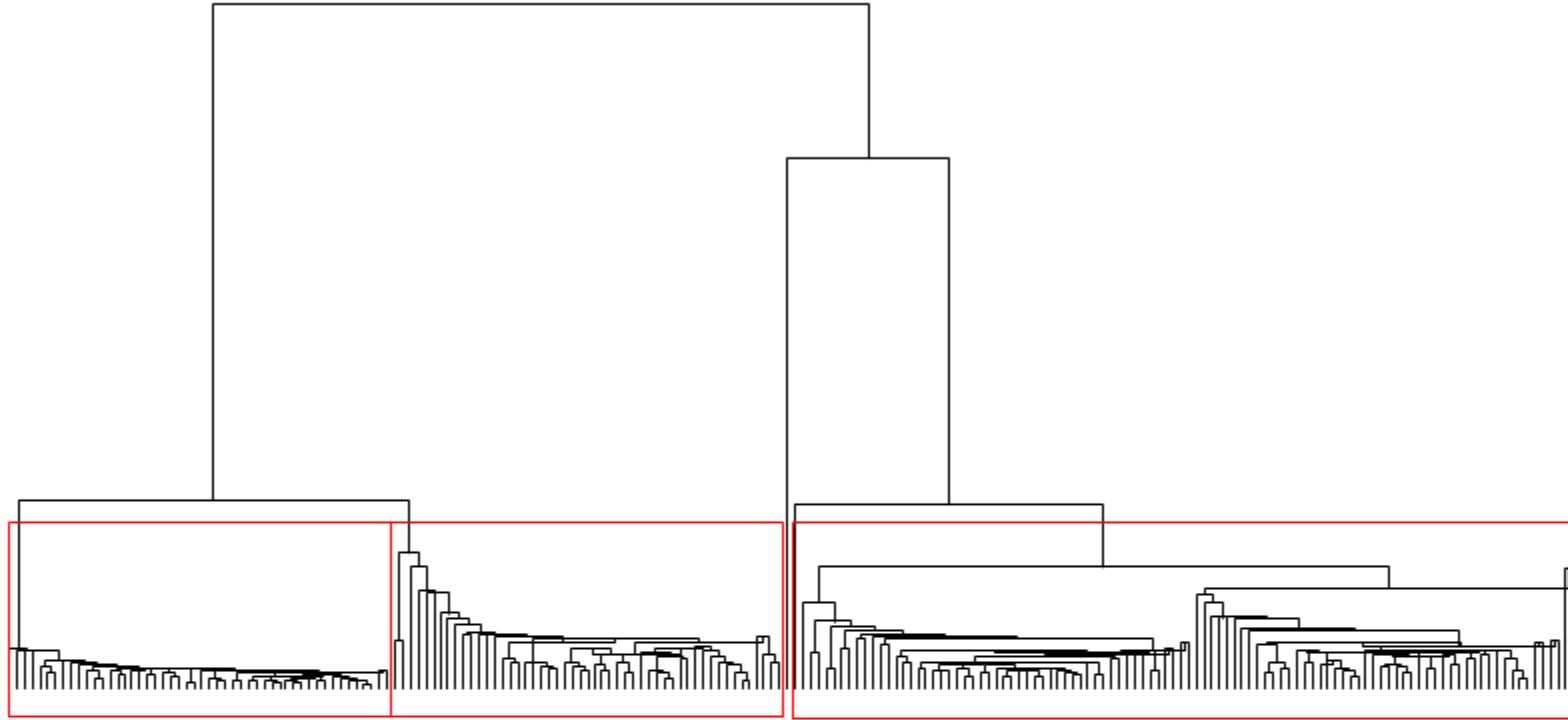


Liking

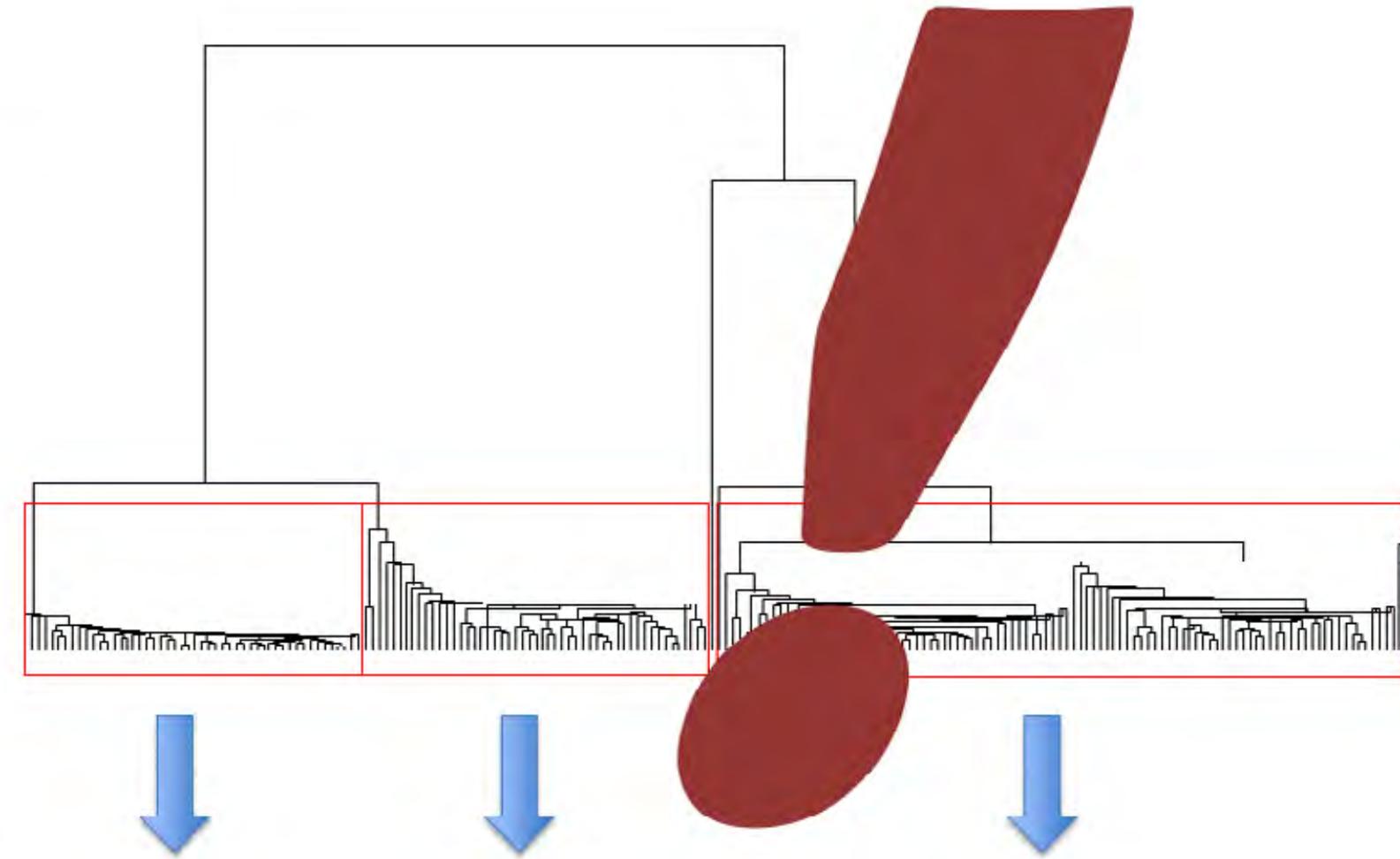




# HCA



# HCA



First  
sample  
was...

**A**

**D**

**B or C**

Various authors have reported situations in which consumers are clustered according to the randomly allocated serving orders.

**Think about that when using this data in preference mapping!**

Liking responses will be influenced by context effects and various biases. Thus we should think of liking responses as ***momentary*** and not as a fixed property of the consumer.

Also **replication** of consumer panel results seems more important than **repeatability** of individual consumers.

# Liking data

organize (scaled?) liking data into a 2D array

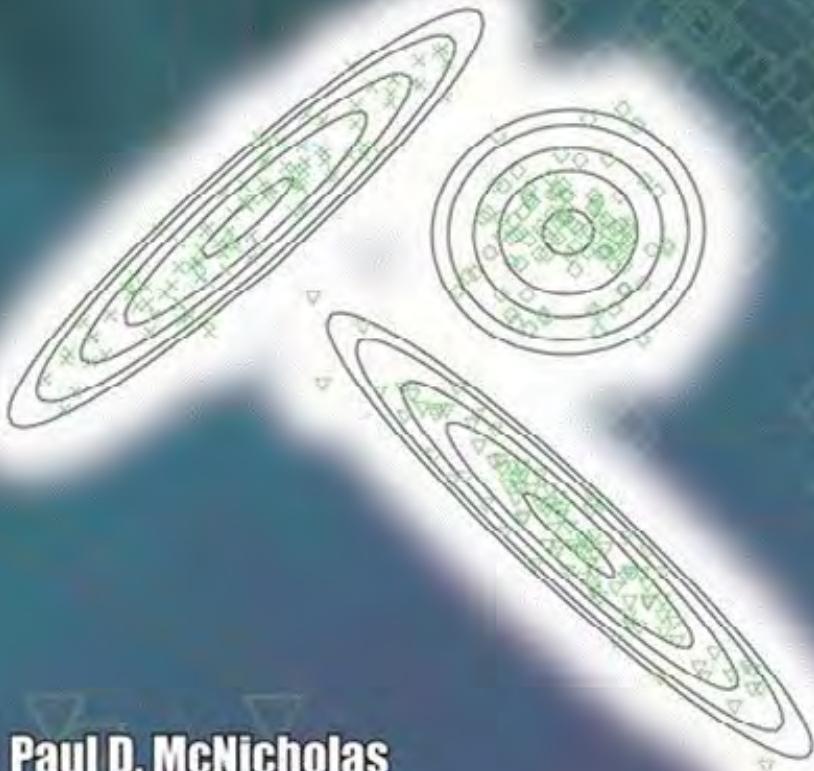
	A	B	C	D
g	5	4	5	5
u	8	6	6	6
o	7	6	6	7
h				

**Rows: Consumers**

**Columns: Products**



# MIXTURE MODEL-BASED CLASSIFICATION



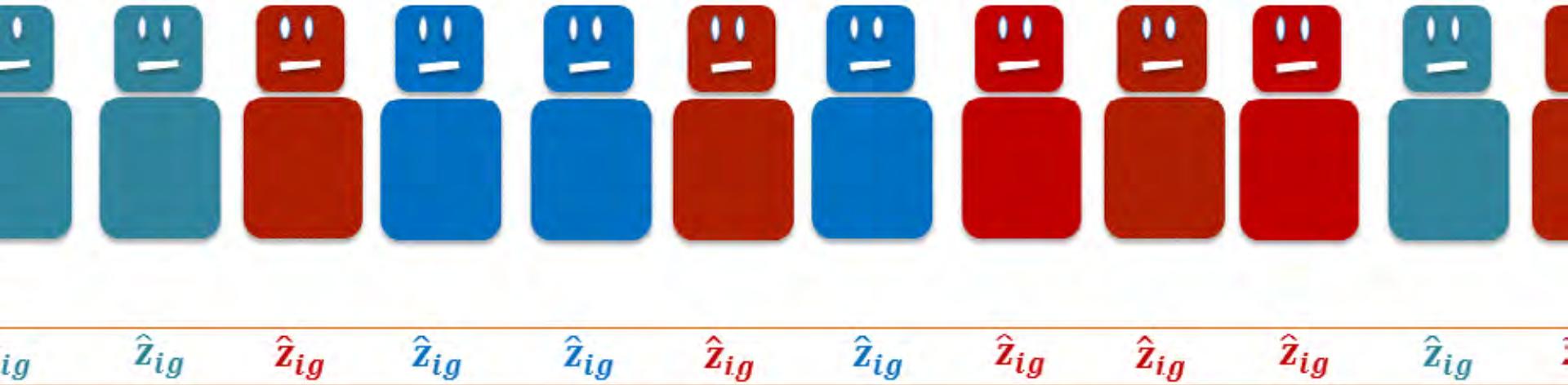
**Paul D. McNicholas**



CRC Press  
Taylor & Francis Group

A CHAPMAN & HALL BOOK

# Gaussian Mixture Model



Initialize  $\hat{z}_{ig}$ .

**M step** – update  $\hat{\pi}_g$ ,  $\hat{\mu}_g$ ,  $\hat{\Sigma}_g$ .

**E step** – update  $\hat{z}_{ig}$  classification predictions.  
(Stop when converged.)

# Higher dimensional data

Attempt to relate

**observed variables (p)**

to

**latent variables (q)**

where  $q < p$  ...and perhaps  $q \ll p$ .

## Mixture of Factor Analyzers

$$\mu_g, \Sigma_g = \Lambda_g \Lambda'_g + \Psi_g$$

**Group 1:**  $\mu, \Sigma = \Lambda \Lambda' + \Psi$

**Group 2:**  $\mu, \Sigma = \Lambda \Lambda' + \Psi$

**Group 3:**  $\mu, \Sigma = \Lambda \Lambda' + \Psi$

## Parsimonious Gaussian Mixture Model

$$\mu_g, \Sigma_g = \Lambda_g \Lambda'_g + \omega_g \Delta_g$$

with CUU constraints

$$\Lambda_g = \Lambda$$

$$\Delta_g = \Delta$$

$$\Delta_g = I$$

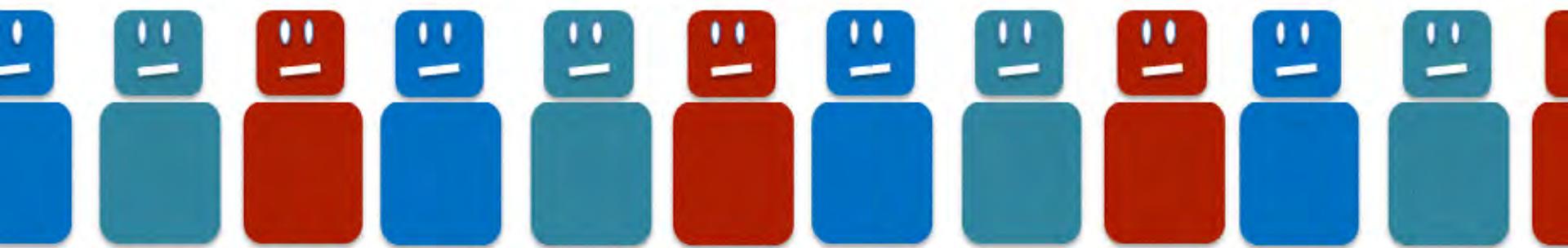
$$\omega_g = \omega$$

Model selection via the  
**Bayesian Information Criterion (BIC)**,  
which imposes a penalty for each  
additional parameter.

Clusters: heterogeneous

Products: variables

Order: nil



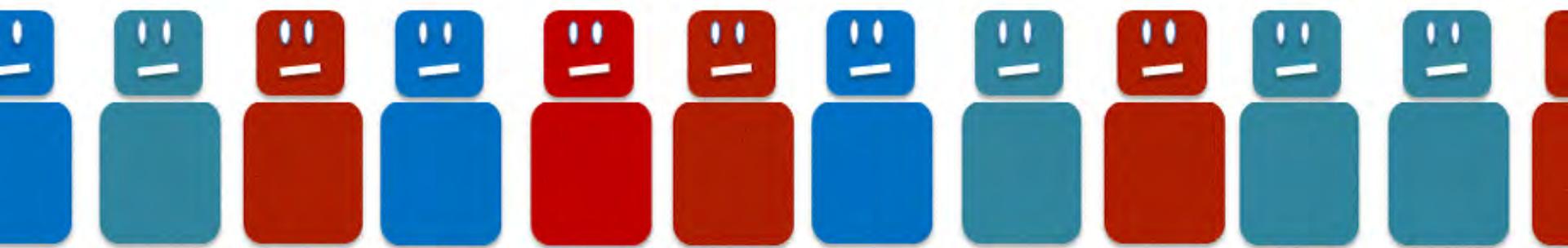
Obtain the best model\*

\* e.g. Franczak et al. (2015) used a mixture of factor analyzers with data imputation that was updated iteratively based on predicted cluster memberships

Clusters: heterogeneous

Products: variables

Order: homogeneous



Estimate and remove *common* order effects

Penalize BIC accordingly.

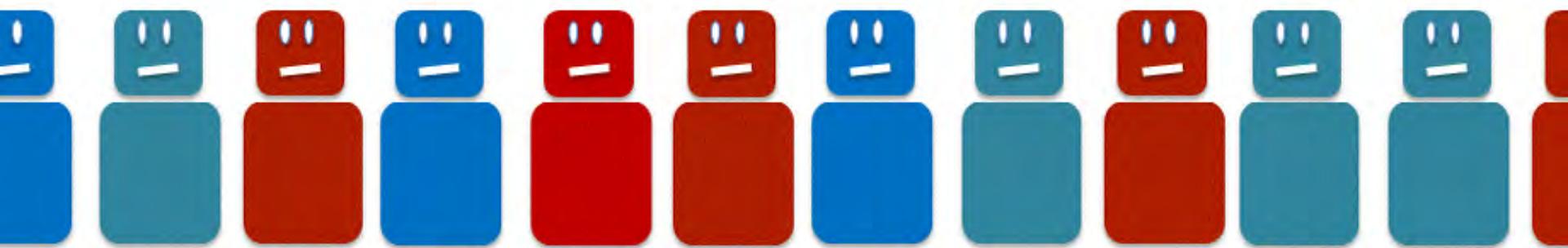
Obtain best mixture model.

Research in Progress...

Clusters: heterogeneous

Products: variables

Order: heterogeneous



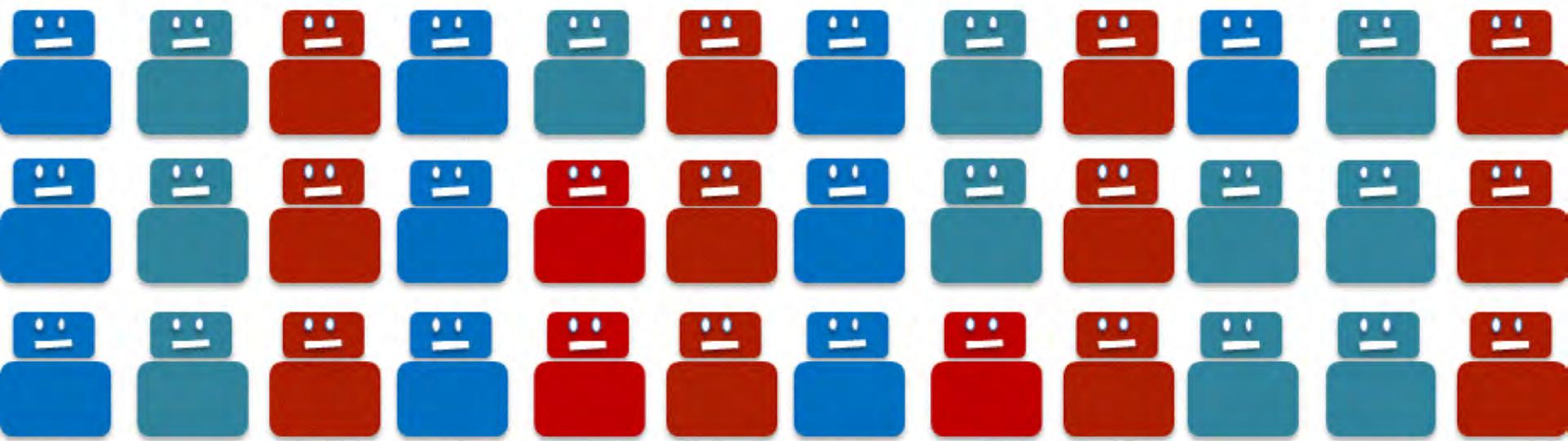
Estimate & remove order effects *per group*.

Penalize BIC accordingly.

Obtain best mixture model.

Research in Progress...

# Comparison



Model selection via BIC.

Review plots (original scale and latent space).

Research in Progress...

A vibrant, crowded street scene, likely Istiklal Street in Istanbul, during a festive period. The street is lined with buildings adorned with numerous Christmas lights, stars, and decorative garlands. A red tram is visible in the center of the street, and a large crowd of people is walking in both directions. The atmosphere is festive and bustling.

Consumer acceptance  
(repeated measures)

# Some Potential Strategies

		1 min	2 min	5 min	10 min
A	4 <sup>th</sup>	7	6	6	5
B	3 <sup>rd</sup>	5	7	6	4
C	1 <sup>st</sup>	8	7	6	5
D	2 <sup>nd</sup>	7	8	6	5



## Conventional clustering

use summary data (e.g. sample means)  
unfold data

	2 min	5 min	10 min
A	8	8	8
B	5	5	5
C	8	7	6
D	8	6	6



## Clustering matrices

E.g., cluster consumers assuming a mixture of matrix normal distributions

	1 min	2 min	5 min	10 min
A	2 <sup>nd</sup>	7	7	8
B	1 <sup>st</sup>	9	8	8
C	4 <sup>th</sup>	5	6	7
D	3 <sup>rd</sup>	8	8	7





My responses are honest and momentary.



My liking responses are an honest integration of my response from my initial impressions until the current time.



My liking responses are an honest integration of my response since the last time I was asked.



To be consistent I give the sample the same liking response every time that I am asked.



I'm so happy to be here that I rate every sample as "Like Very Much"!

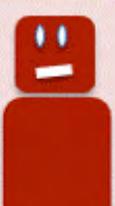
# Point in time data

e.g. at 10 min.

	A	B	C	D
	5	4	5	5
	8	5	6	6
	7	6	6	7
	5	5	8	5

# Summarize data

e.g. area under curve

	A	B	C	D
	24	22	26	26
	32	21	28	28
	29	31	24	30
	25	19	22	22

# Unfold data

	A1	A2	A5	A10	B1	B2	B5	B10	C1	C2	C5	C10	D1	D2	D5	D10
	7	6	6	5	5	7	6	4	8	7	6	5	7	8	6	5
	8	8	8	8	6	5	5	5	7	8	7	6	8	8	6	6
	7	7	8	7	9	8	8	6	5	6	7	6	8	8	7	7
	6	6	7	6	5	5	4	4	3	3	5	5	5	5	5	5

# Matrix clustering

This is a potential application for matrix normal mixture model-based clustering\*.

		1 min	2 min	5 min	10 min
A	4 <sup>th</sup>	7	6	6	5
B	3 <sup>rd</sup>	5	7	6	4
C	1 <sup>st</sup>	8	7	6	5
D	2 <sup>nd</sup>	7	8	6	5



		1 min	2 min	5 min	10 min
A	1 <sup>st</sup>	8	8	8	8
B	4 <sup>th</sup>	6	5	5	5
C	3 <sup>rd</sup>	7	8	7	6
D	2 <sup>nd</sup>	8	8	6	6



		1 min	2 min	5 min	10 min
A	2 <sup>nd</sup>	7	7	8	7
B	1 <sup>st</sup>	9	8	8	6
C	4 <sup>th</sup>	5	6	7	6
D	3 <sup>rd</sup>	8	8	7	7



\* See Li (2014, Ch. 3) for applications of matrix clustering to selected sensory evaluation data.

A loaf of bread with several slices cut off, illustrating incomplete block designs.

Incomplete block  
designs

# Balanced Incomplete Block Design

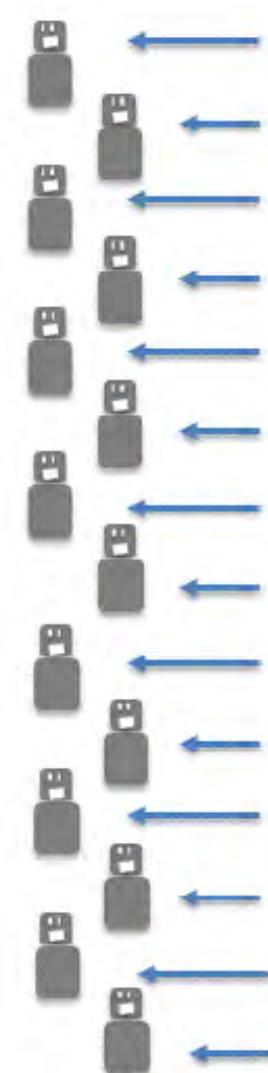
Each consumer evaluates  $k$  of  $t$  samples  
( $k < t$ )

$t$ -present- $k$  design

Goal:

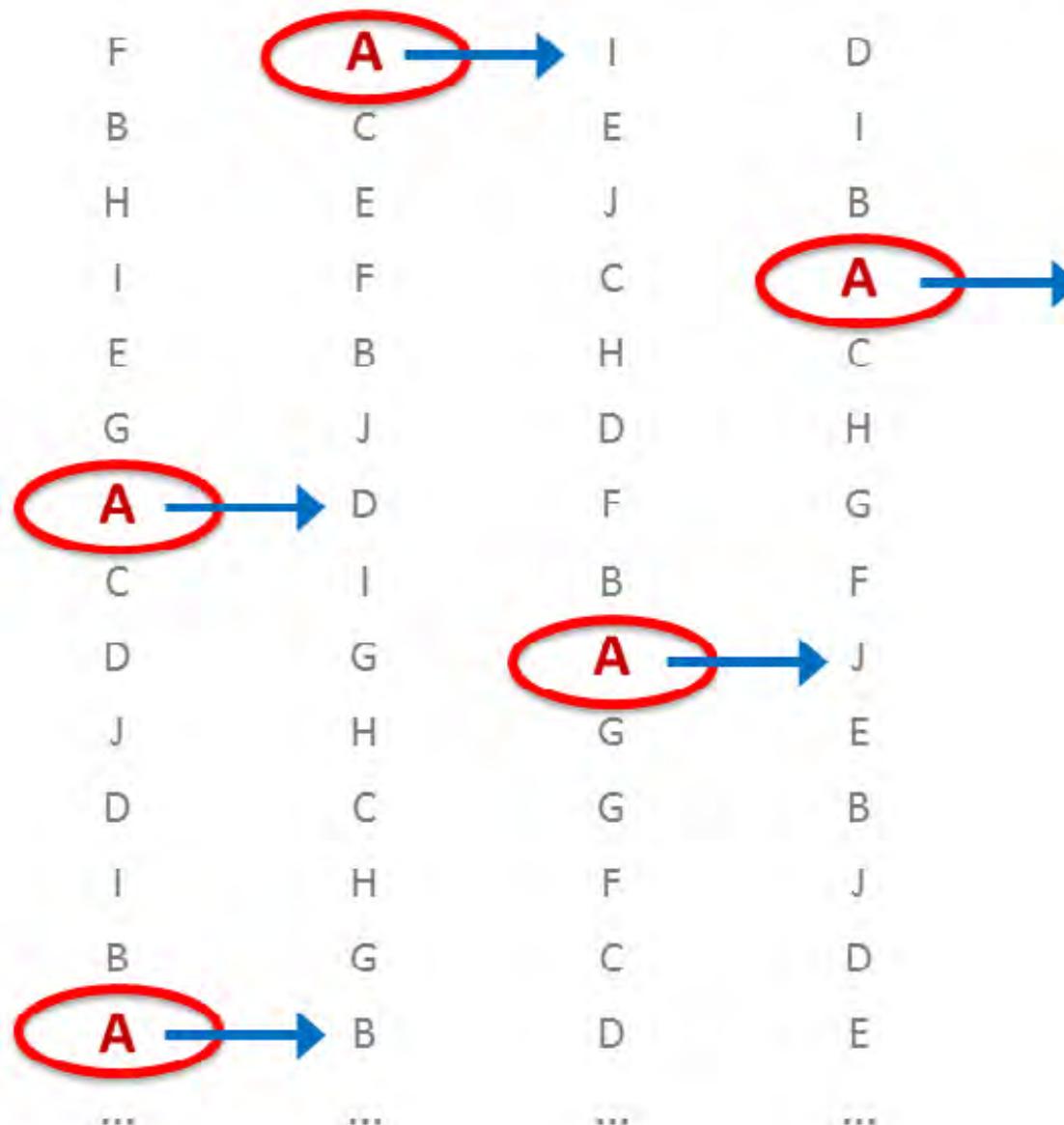
Order and carryover balanced  
Unbiased product estimates

# Balanced Incomplete Block Design



F	<b>A</b>	I	D
B	C	E	I
H	E	J	B
I	F	C	<b>A</b>
E	B	H	C
G	J	D	H
<b>A</b>	D	F	G
C	I	B	F
D	G	<b>A</b>	J
J	H	G	E
D	C	G	B
I	H	F	J
B	G	C	D
<b>A</b>	B	D	E
...	...	...	...

# Balanced Incomplete Block Design



# Balanced Incomplete Block Design

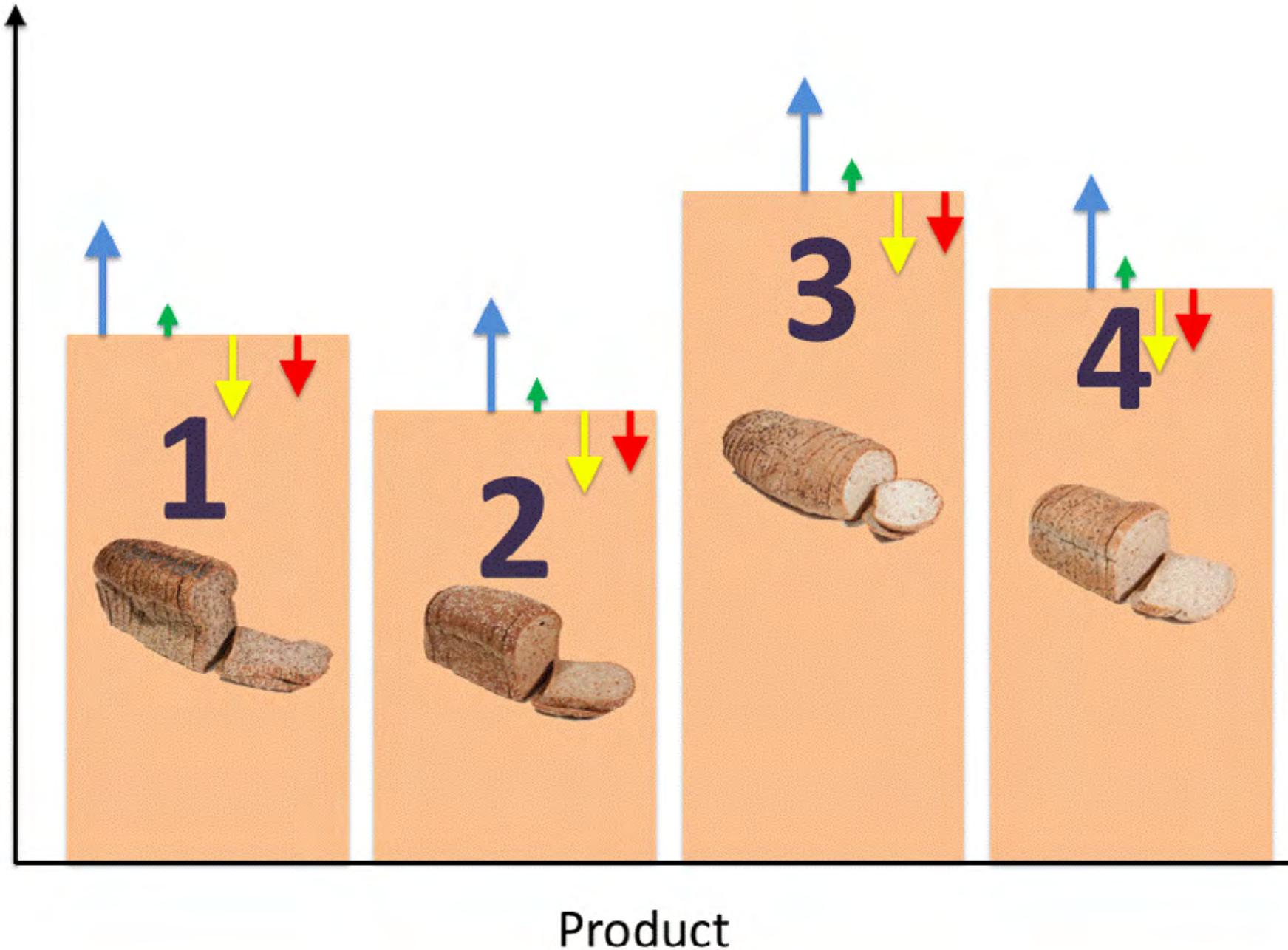
	F	A	I	D
	B	C	E	I
	H	E	J	B
	I	F	C	A
	E	B	H	C
	G	J	D	H
	D	D	F	G
	C	I	B	F
	D	G	A	J
	J	H	G	E
	D	C	G	B
	I	H	F	J
	B	G	C	D
	B	B	D	E
...	...	...	...	...

# Consumer data



		6	5	7		5			
	8	8		4		5			
		8	7		8			6	
		6			5	5			9

Average Liking



**There is additional information!**

**A trained sensory descriptive analysis panel evaluated 16 whole grain breads...**

# Sensory space

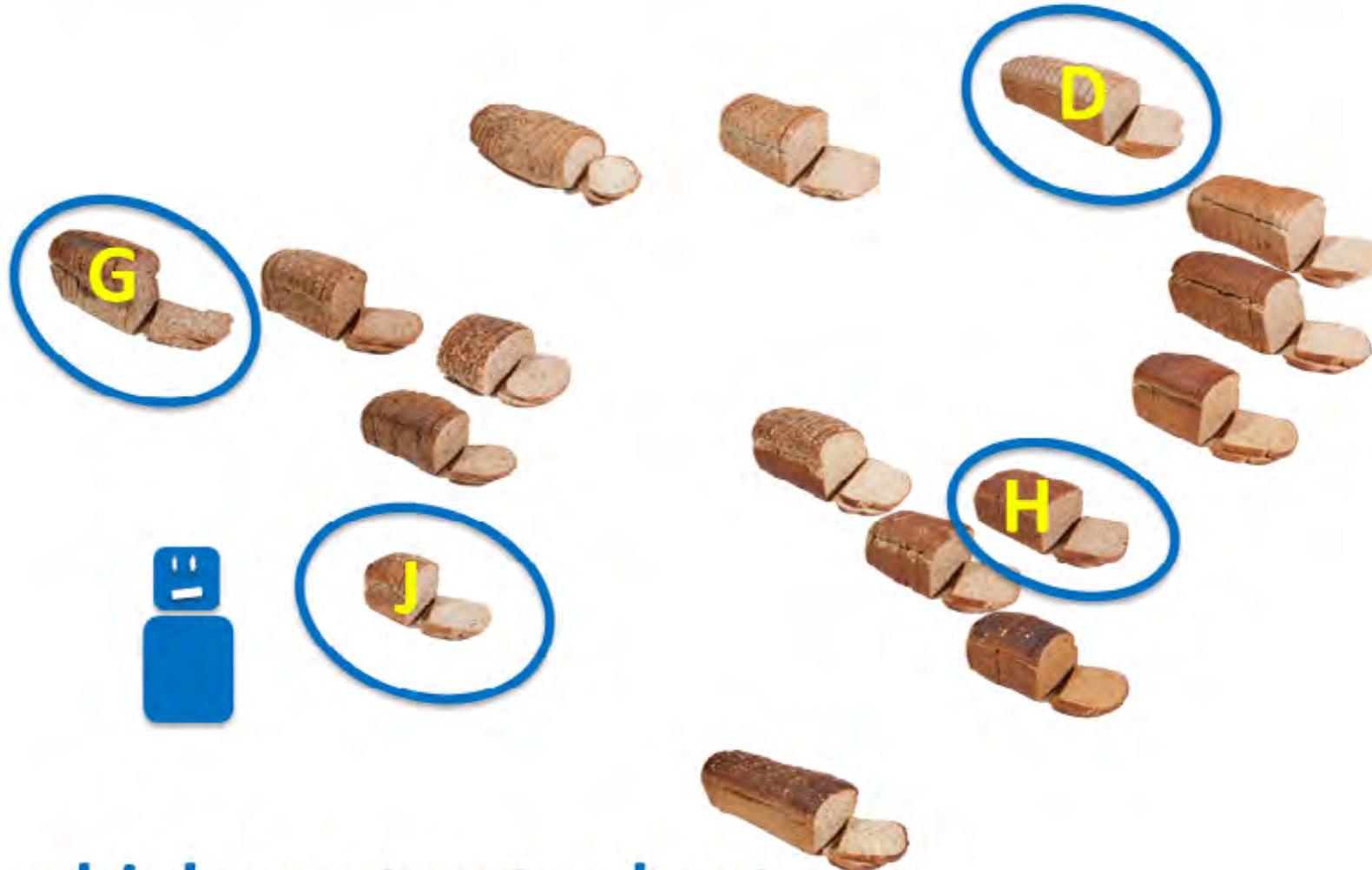


# Balanced Incomplete Block Design



F	A	I	D
B	C	E	I
H	E	J	B
I	F	C	A
E	B	H	C
<b>G</b>	<b>J</b>	<b>D</b>	<b>H</b>
A	D	F	G
C	I	B	F
D	G	A	J
J	H	G	E
D	C	G	B
I	H	F	J
B	G	C	D
A	B	D	E
...	...	...	...

## Sample set order #6



a high-contrast subset

## Sample set order #6

Hedonic responses are given for a wide range of products.

From these few responses we learn a lot about this consumer's preferences.



a high-contrast subset

# Balanced Incomplete Block Design



F	A	I	D
B	C	E	I
H	E	J	B
I	F	C	A
<b>E</b>	<b>B</b>	<b>H</b>	<b>C</b>

G	J	D	H
A	D	F	G
C	I	B	F
D	G	A	J
J	H	G	E
D	C	G	B
I	H	F	J
B	G	C	D
A	B	D	E
...	...	...	...

## Sample set order #5



a low-contrast subset

Sample set order #5

Hedonic responses are given for a narrow range of products.

So we learn little about this consumer's preferences.



a low-contrast subset

Would this  
product have  
been liked or  
disliked



a low-contrast subset

# Sensory Informed Design

$t$ -present- $k$  design

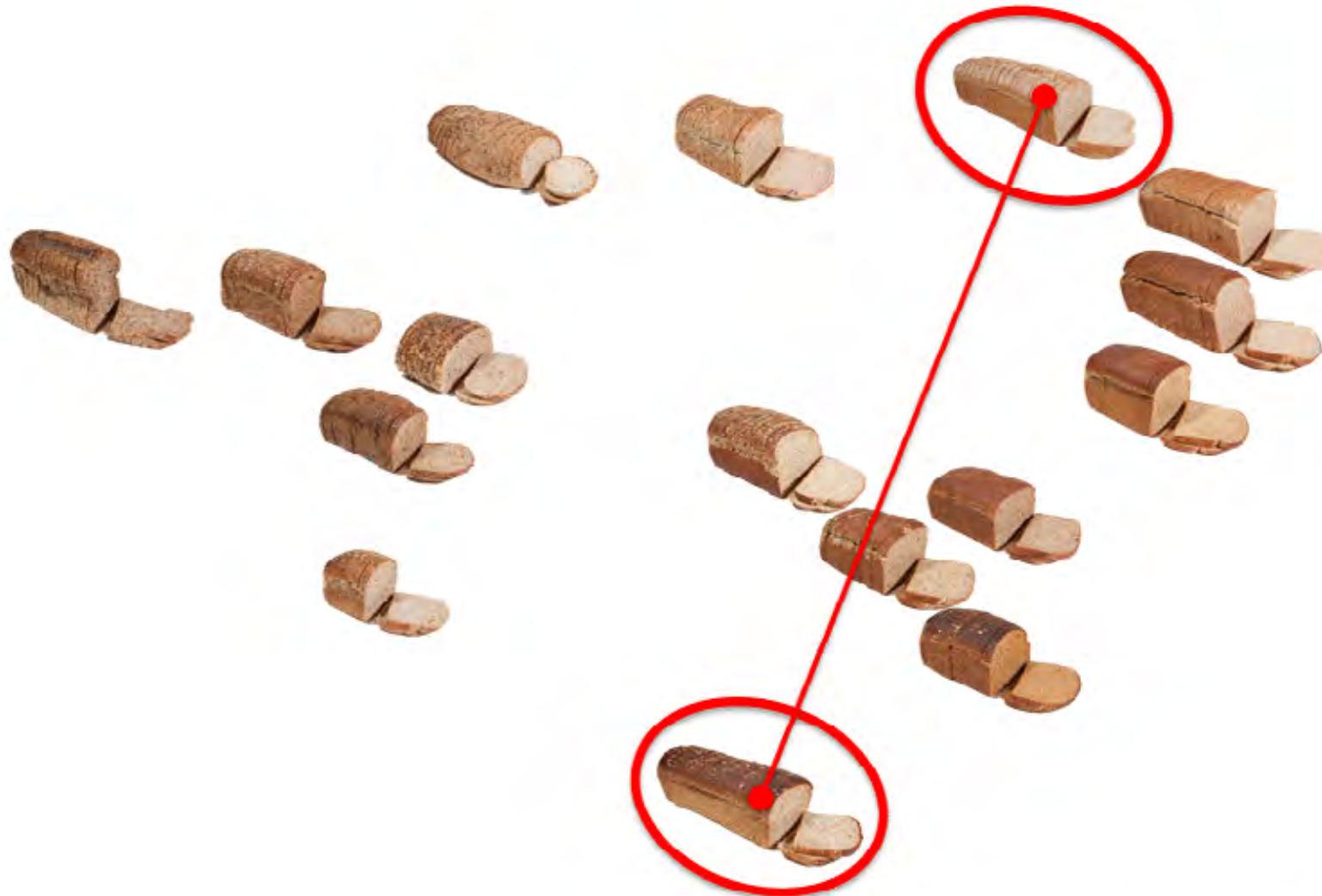
Goal:

Favour sample sets with **sensory contrast**

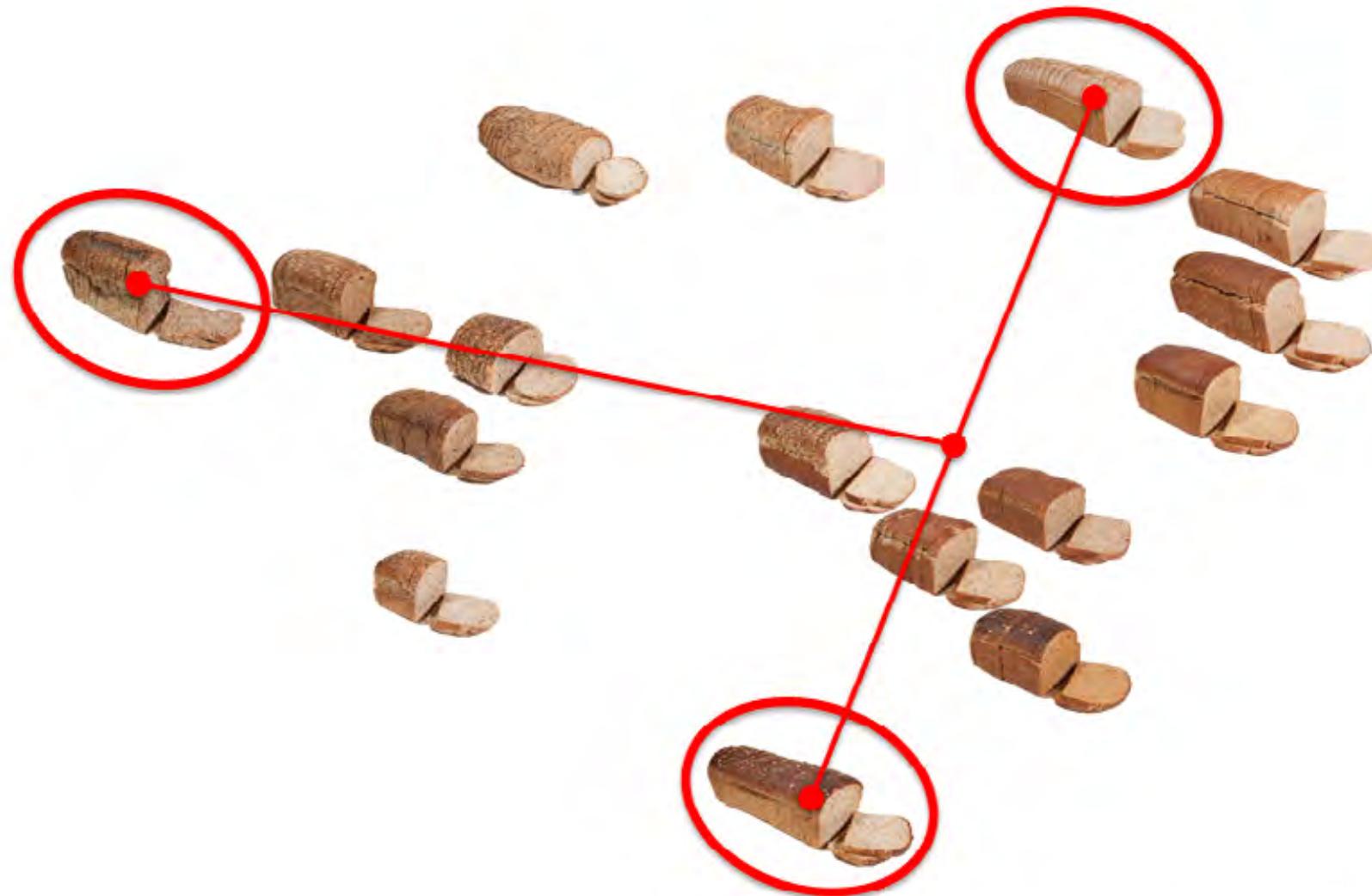
Order balanced

*Compromise:* carryover unbalanced

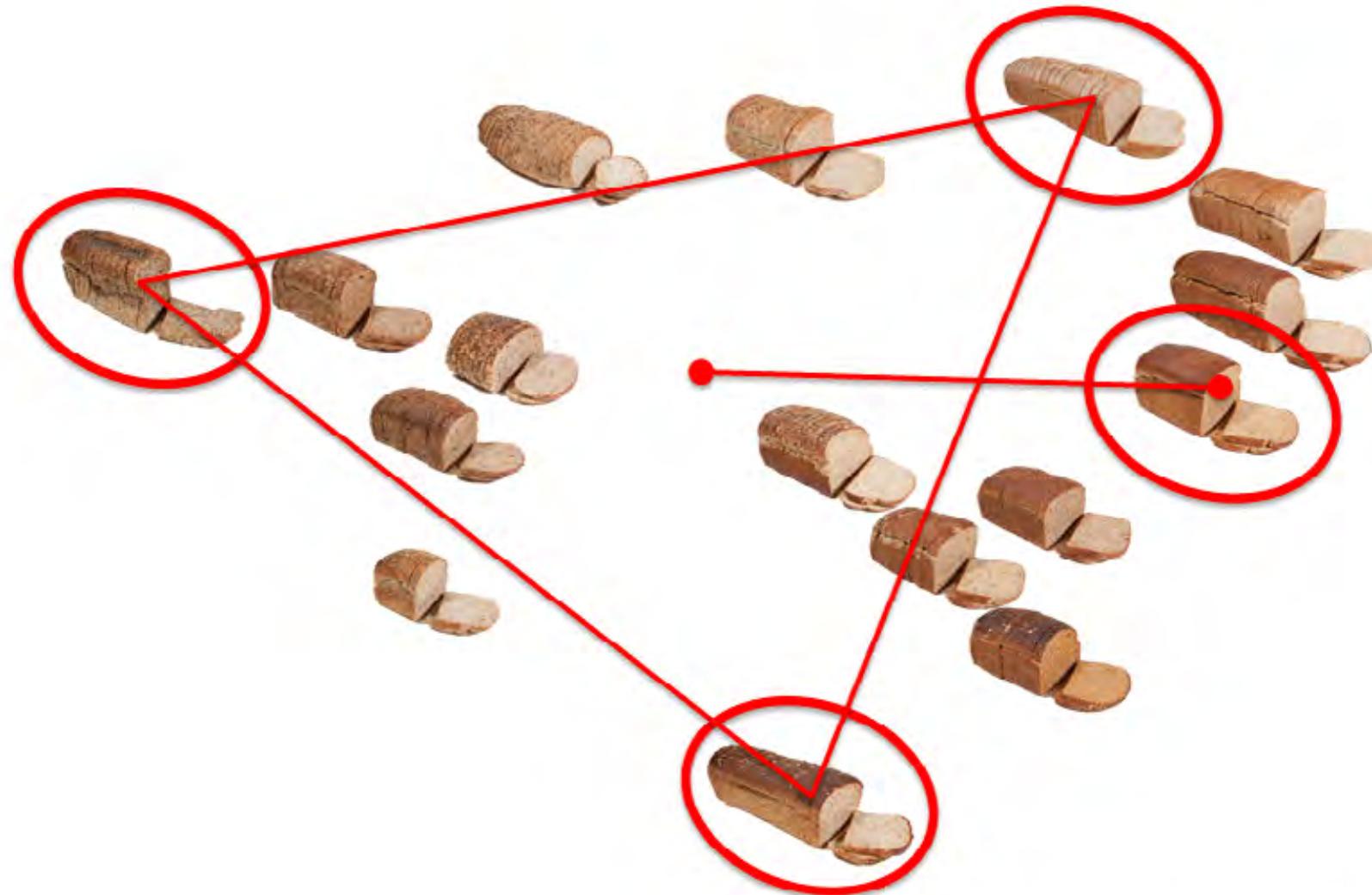
# Sensory Informed Design



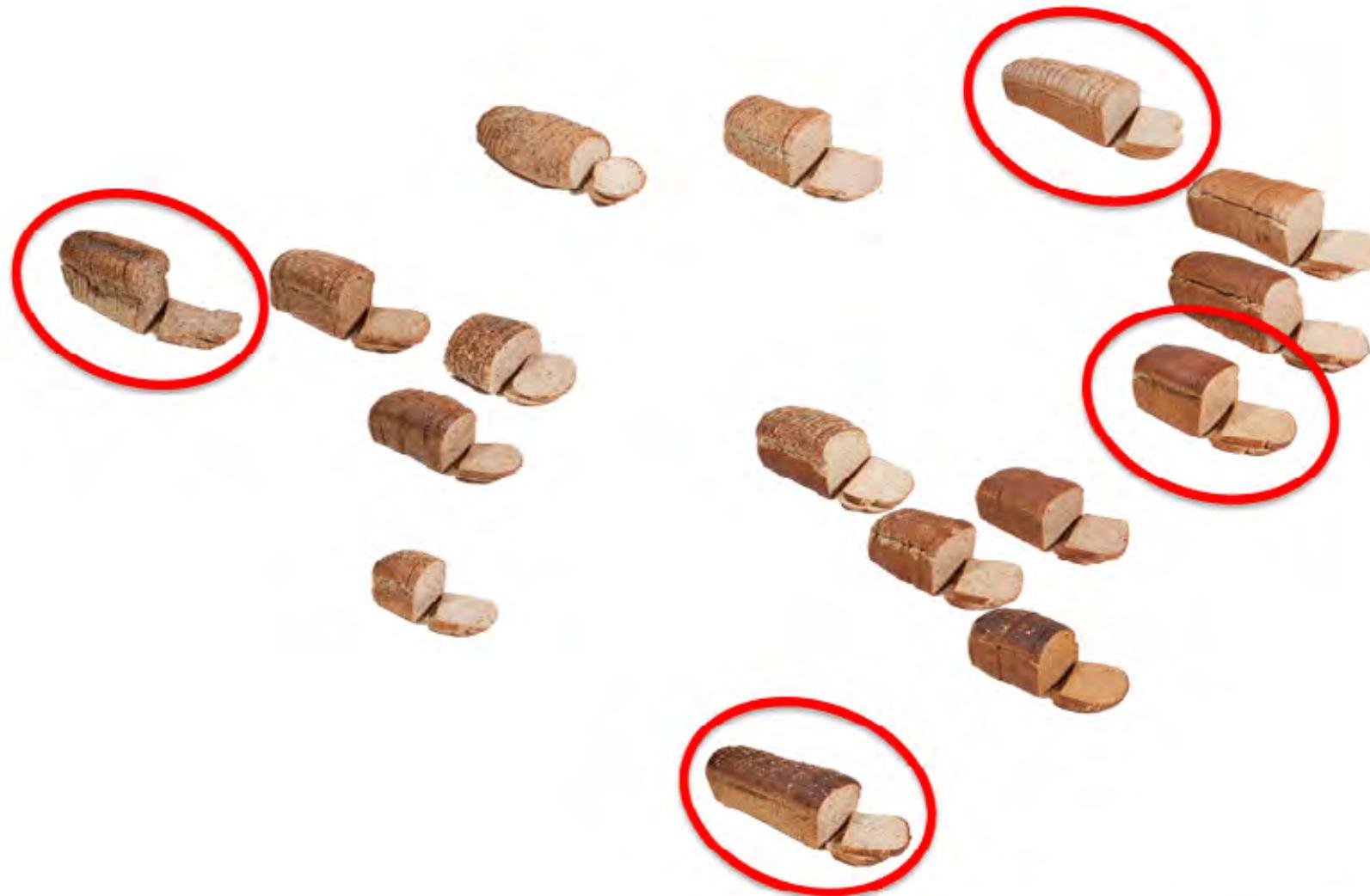
# Sensory Informed Design



# Sensory Informed Design

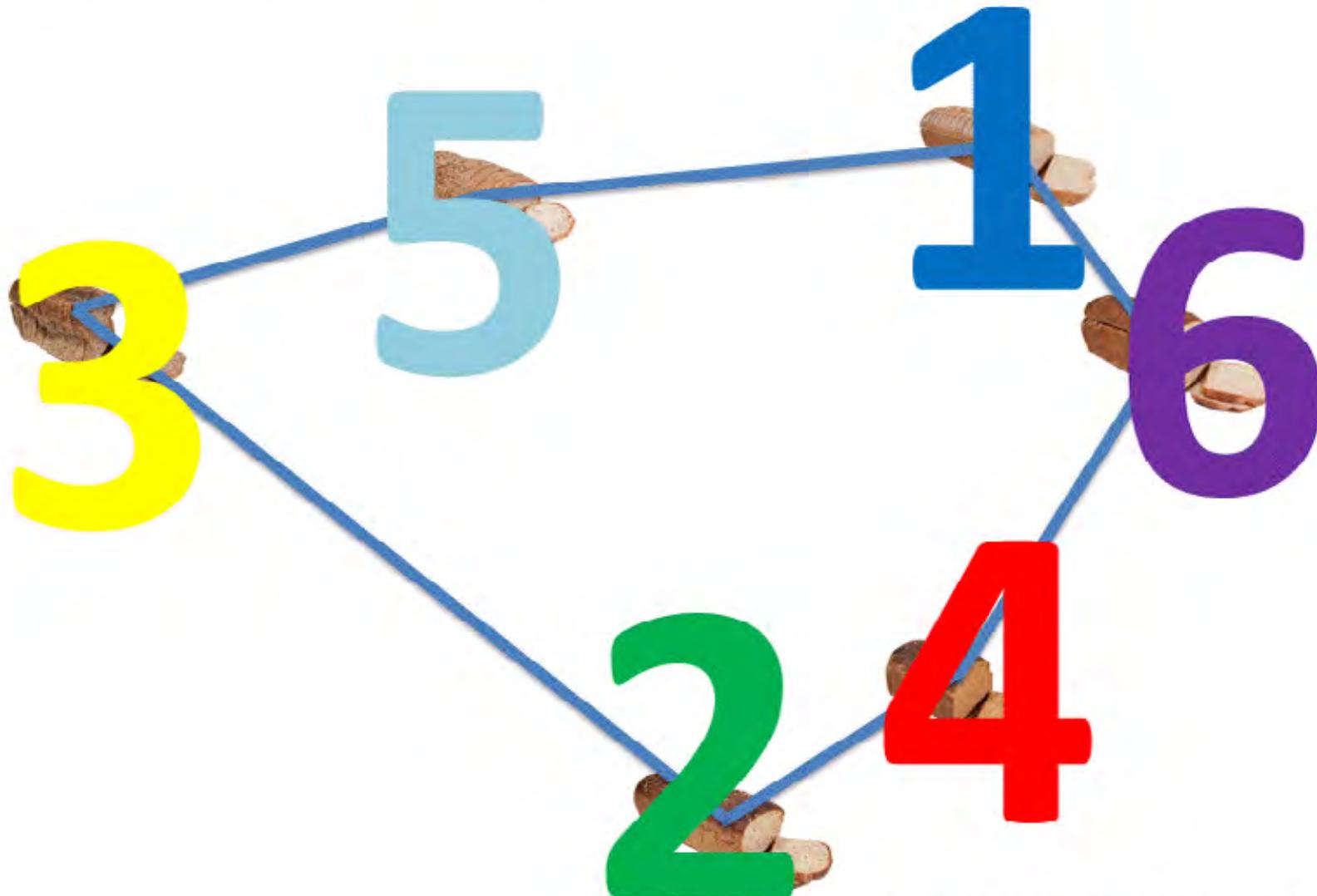


# Sensory Informed Design

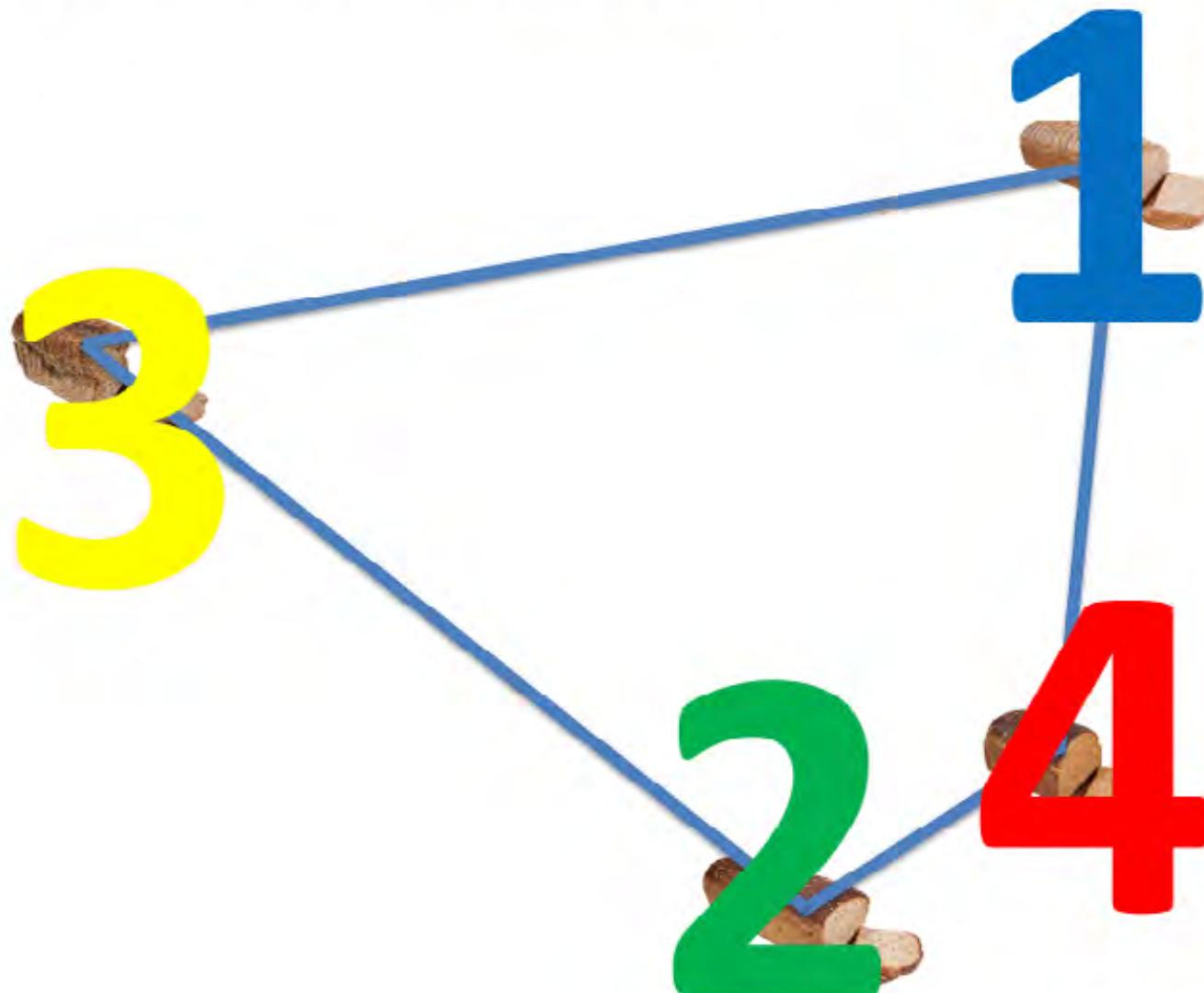


Franczak et al. (2015) describe a  
**16-present-6** sensory informed design.

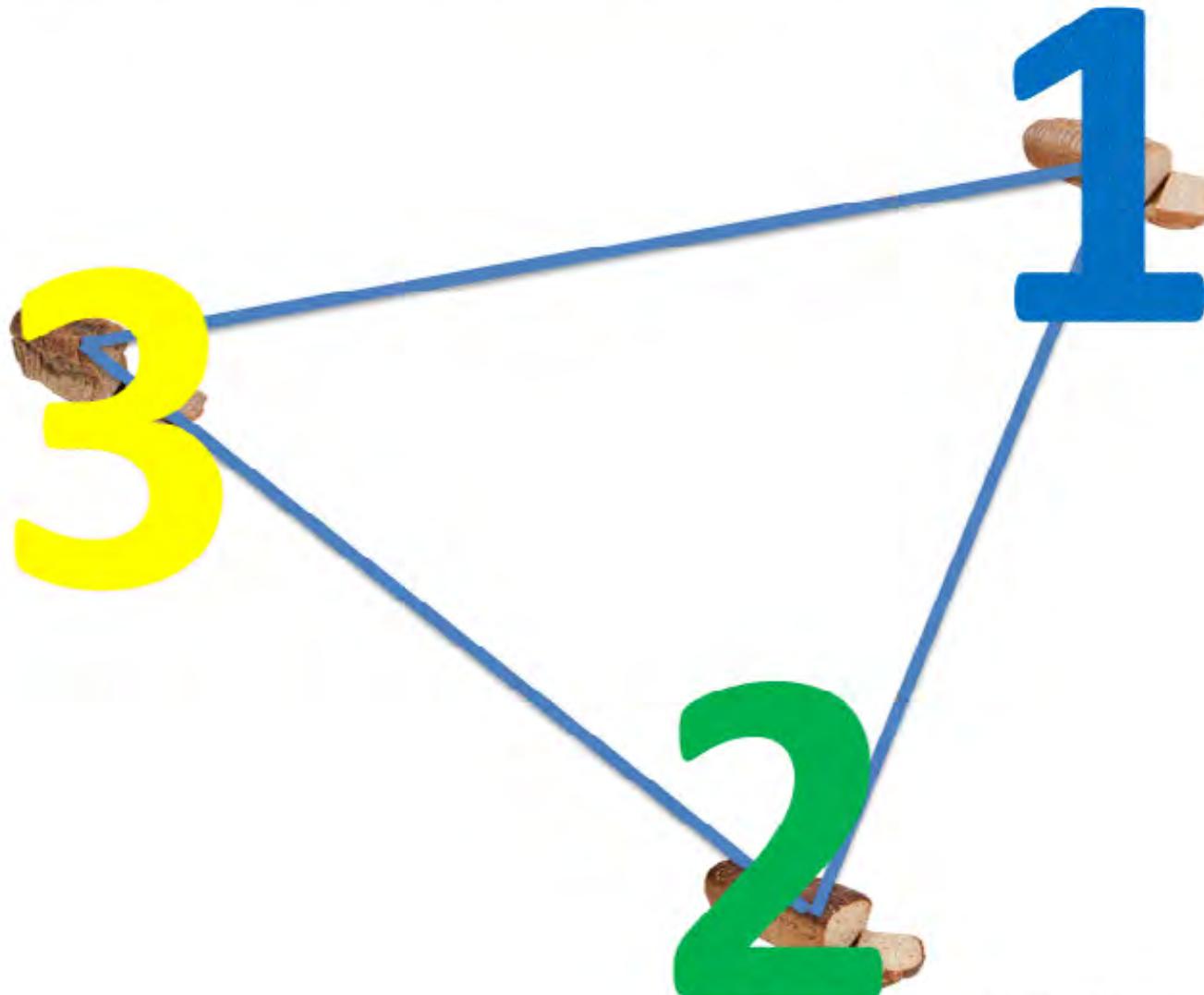
# Sensory Informed design (16-present-6 design)



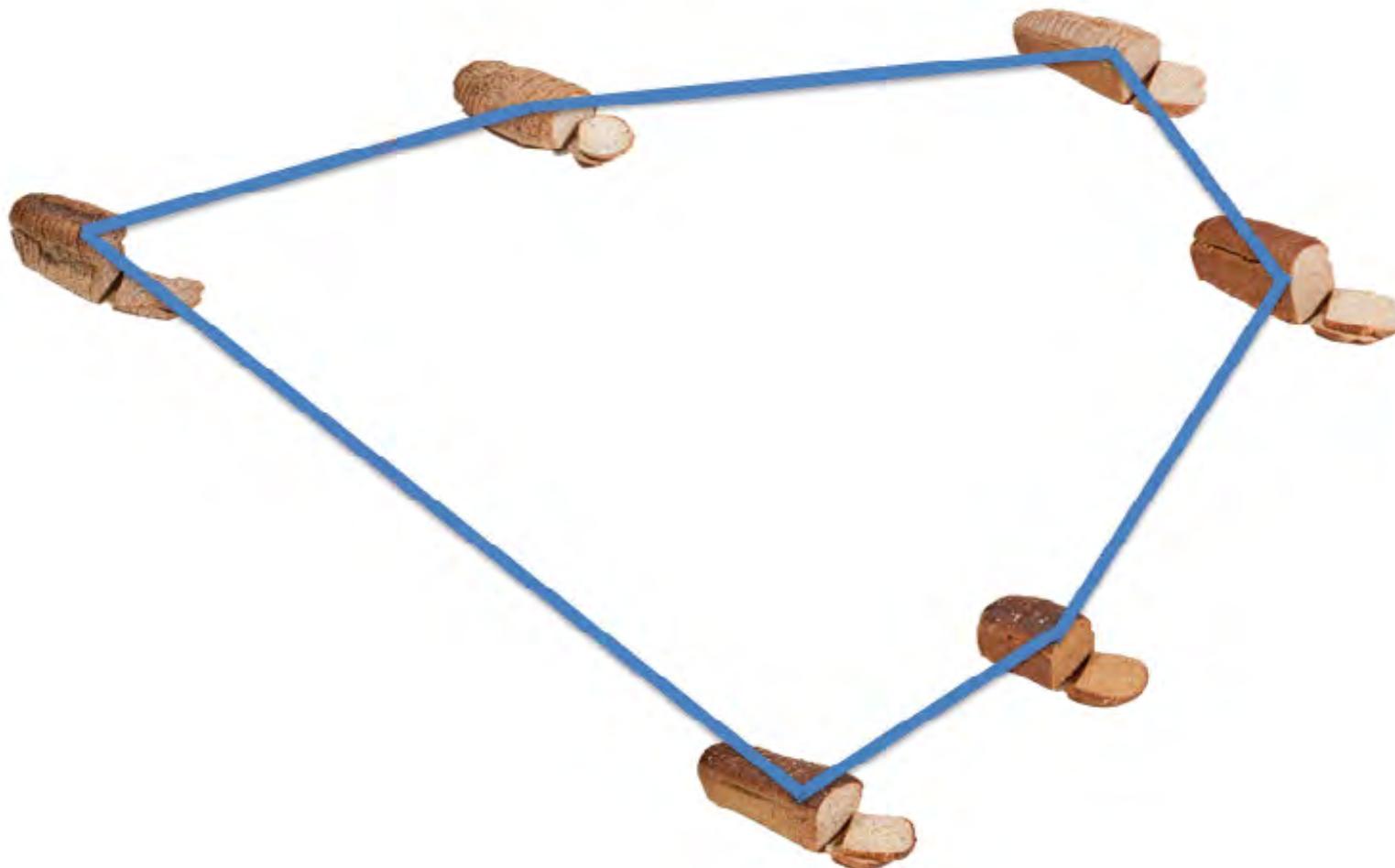
# Sensory Informed design (16-present-4 *nested* design)



# Sensory Informed design (16-present-3 *nested* design)



# Scaling data?



# Scaling data?

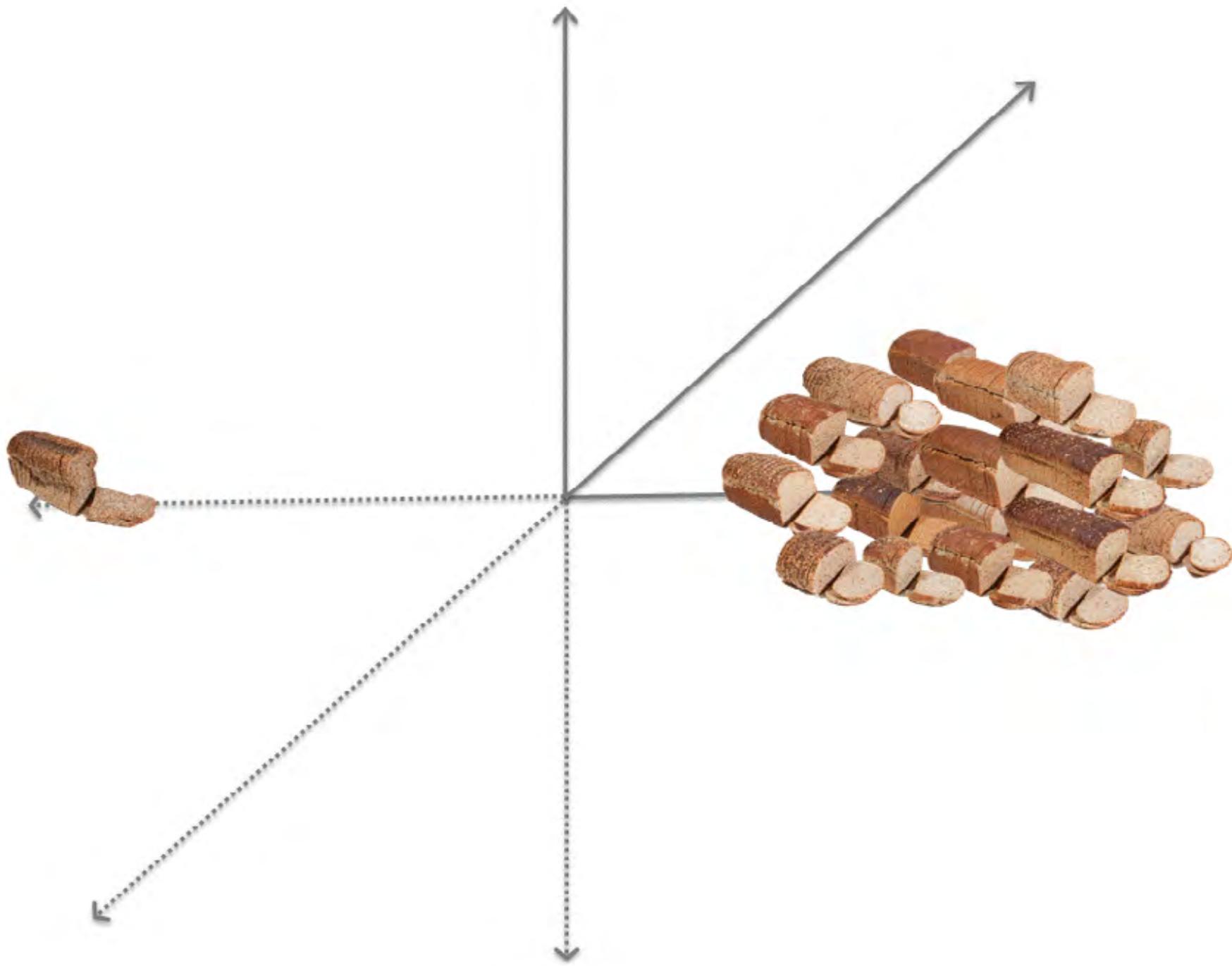


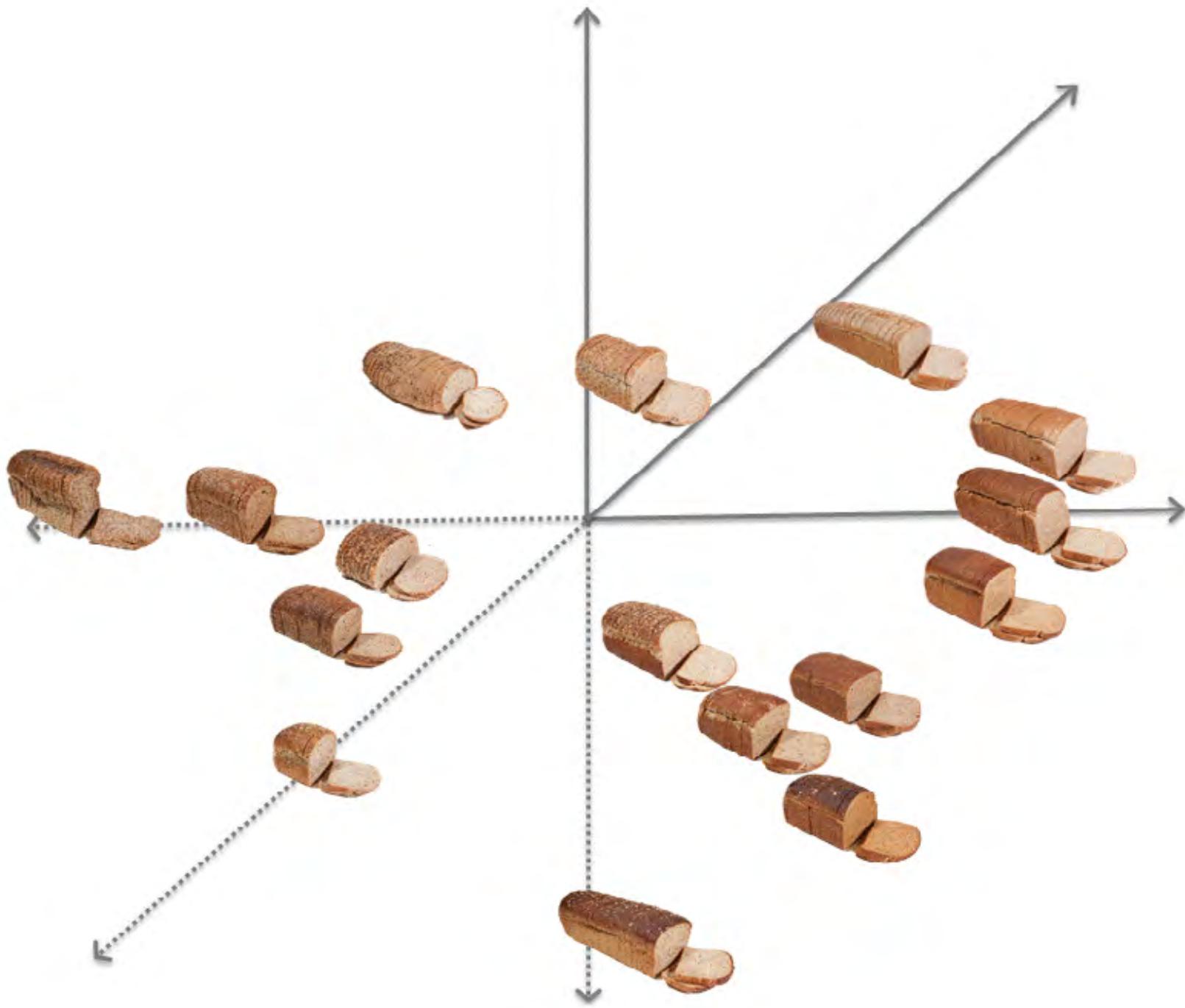
Is it *really* wise to  
center or rescale this  
consumer's liking data?

## Sensory Informed Designs

- t*** number of products
- product variability
- sensory space
- k*** number of samples presented
- N*** number of consumers
- consumer diversity
- & c. context effects & biases (e.g. order)
- scale used for data collection
- sensory-liking relationship

***Further research required!***

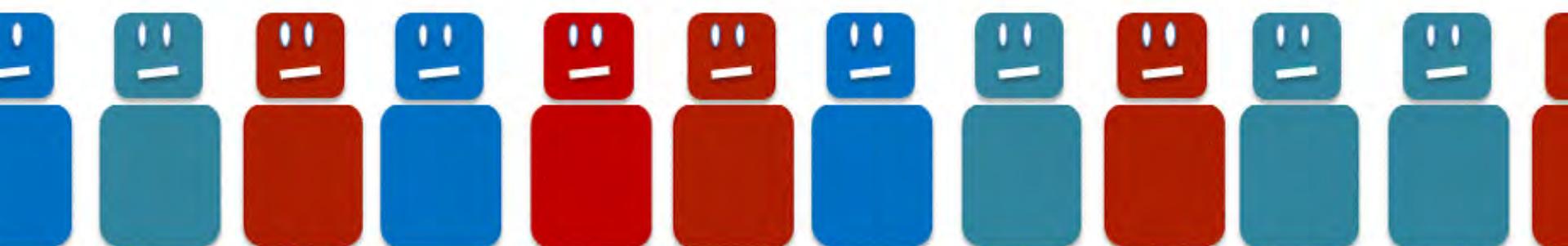




Clusters: heterogeneous

Products: variables

Order: heterogeneous



Estimate & remove order effects *per group*.

Estimate and impute missing data *per group* via  
conditional E-steps.

Obtain best mixture model

Penalize BIC according to

Research in Progress...

# Part II: Consumer perception



**Please check all that apply.**

<input type="checkbox"/> Artificial Flavor	<input type="checkbox"/> High Sweet Taste	<input type="checkbox"/> Plastic Flavor
<input type="checkbox"/> Bitter Taste	<input type="checkbox"/> Lemon Flavor	<input type="checkbox"/> Processed Flavor
<input type="checkbox"/> Cheap Taste	<input type="checkbox"/> Low Sweet Taste	<input type="checkbox"/> Refreshing Flavor
<input type="checkbox"/> Earthy Flavor	<input type="checkbox"/> Low Acidic/Sour/Tart Taste	<input type="checkbox"/> Rotten/Overripe Orange Flavor
<input type="checkbox"/> Expensive Flavor	<input type="checkbox"/> Natural Flavor	<input type="checkbox"/> Shelf Stable Flavor
<input type="checkbox"/> Fresh Orange Flavor	<input type="checkbox"/> Not From Concentrate Flavor	<input type="checkbox"/> Strong Flavor
<input type="checkbox"/> Fresh Squeezed Flavor	<input type="checkbox"/> Organic Flavor	<input type="checkbox"/> Weak/Watery Flavor
<input type="checkbox"/> From Concentrate Flavor	<input type="checkbox"/> Other Citrus Flavor	<input type="checkbox"/> None of these apply
<input type="checkbox"/> Green/Unripe Orange Flavor	<input type="checkbox"/> Oxidized Flavor	
<input type="checkbox"/> High Acidic/Sour/Tart Taste	<input type="checkbox"/> Papery/Cardboard Flavor	

**Check-all-that-apply  
(CATA) questions**

# Question order

Liking → CATA

Investigate

**perception responses within  
liking clusters**

and / or

**liking responses within  
perception clusters**

# Balance sample serving orders



	A	B	D	C
	B	C	A	D
	<b>C</b>	<b>D</b>	<b>B</b>	<b>A</b>
	D	A	C	B
	B	A	C	D
	A	D	B	C
	D	C	A	B
	<b>C</b>	<b>B</b>	<b>D</b>	<b>A</b>

	C	B	A	D
	B	B	C	A

# Balance & attribute positions

a	b	h	c	g	d	f	e
b	c	a	d	h	e	g	f
<b>c</b>	<b>d</b>	<b>b</b>	<b>e</b>	<b>a</b>	<b>f</b>	<b>h</b>	<b>g</b>
d	e	c	f	b	e	a	h
e	f	d	g	c	f	b	a
f	g	e	h	d	g	c	b
g	h	f	a	e	a	d	c
<b>h</b>	<b>a</b>	<b>g</b>	<b>b</b>	<b>f</b>	<b>b</b>	<b>e</b>	<b>d</b>
g	e	c	d	a	b	h	d
a	d	g	b	c	f	a	b

1 0 0 0 0 0 0 0 1 0 0 1 0 0 0 0 0 0 1 1 1 0 1 1 0 1 0 1 0 0 0 0 0  
1 0 0 1 1 1 0 1 1 0 1 1 0 0 0 1 0 1 1 1 1 0 0 1 0 0 0 0 0 1  
0 0 1 0 0 0 1 0 0 0 1 0 0 1 0 0 0 1 0 0 0 1 0 0 0 1 0 0 0 0 1  
1 0 0 0 0 0 0 1 1 1 0 1 1 0 1 0 0 1 1 1 1 0 1 1 0 1 1 0 1 0 1  
0 0 0 0 0 1 0 1 0 0 0 1 0 0 0 1 0 0 0 1 0 0 0 1 0 0 0 0 0 0 0  
1 0 1 1 1 1 0 0 0 1 0 1 0 0 1 0 0 0 1 0 1 0 1 1 0 1 0 0 1 0 0  
1 0 0 1 0 1 0 0 0 0 1 0 0 0 0 0 0 1 0 0 1 1 0 1 0 1 0 0 0 0 0  
1 0 0 0 0 1 0 0 0 0 1 0 0 0 0 0 1 0 0 0 0 1 0 0 0 0 1 0 1 1  
1 0 0 1 0 0 0 1 1 1 0 1 1 1 1 0 0 1 1 1 1 0 1 1 1 1 0 1 1 1  
0 0 0 0 1 1 0 1 1 1 0 1 1 0 0 0 0 1 0 0 0 0 1 0 0 0 0 0 0 0 0  
0 0 0 1 0 1 0 0 0 1 0 1 1 0 1 0 1 0 1 1 0 1 0 1 0 1 0 1 1 0 0  
1 0 0 1 0 0 0 1 0 0 0 1 0 0 0 1 0 0 0 1 0 0 0 1 0 1 0 1 0 0 0  
0 0 0 0 1 0 0 0 0 1 1 1 0 0 1 0 0 0 1 1 1 0 0 1 0 0 0 0 0 1 0  
0 0 0 0 0 0 0 1 0 0 0 0 0 0 1 0 0 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0  
0 0 0 1 1 1 1 0 1 1 0 0 0 0 0 0 0 1 0 0 0 0 0 0 1 0 0 0 0 0 0 0 0

**Rows: Consumers**

×

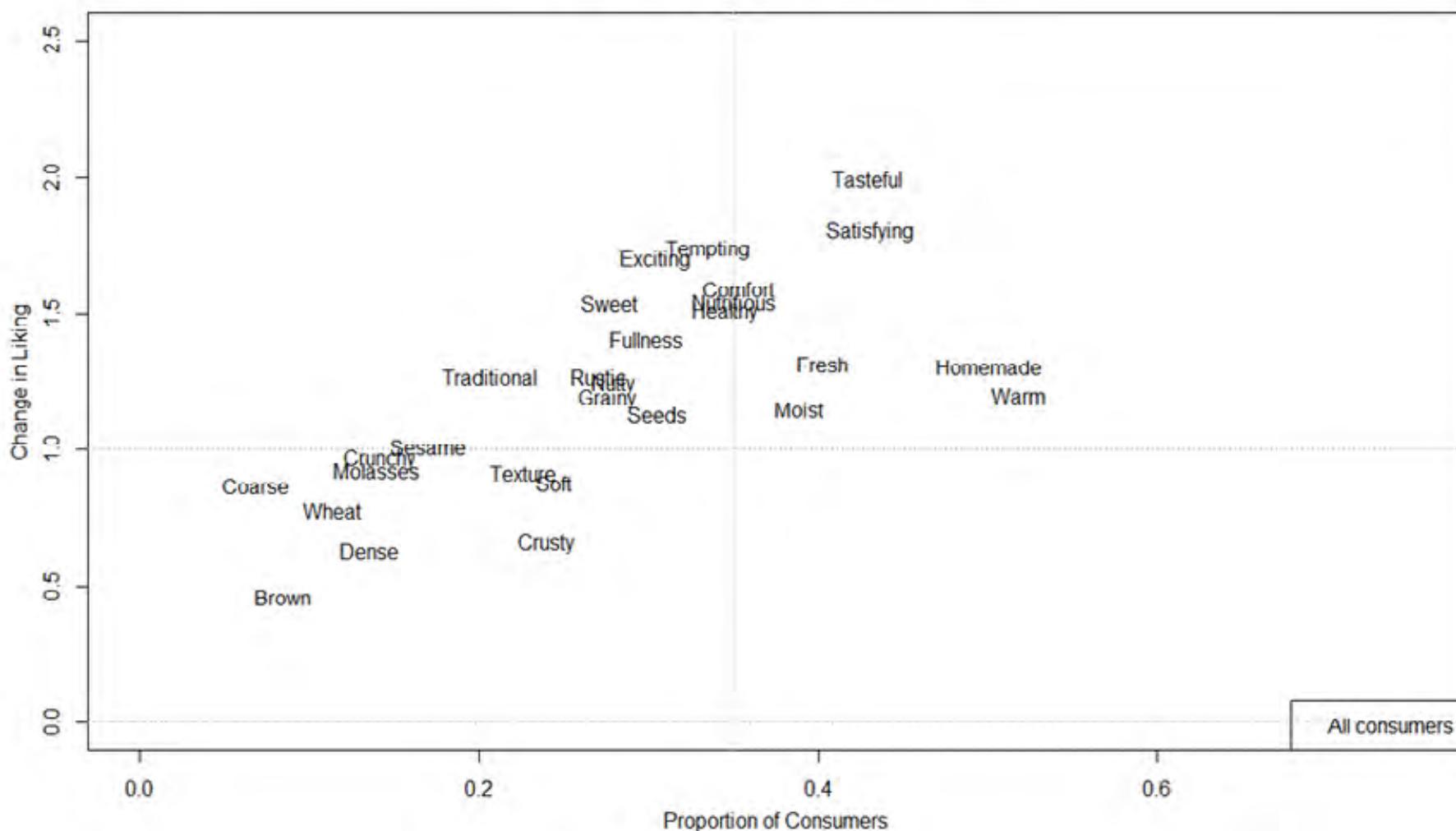
**Columns: Attributes**

×

**Slices: Products**

# Penalty analysis

'Must have' attributes (ideal selected)



## “Ideal Product”

1000000010010000001110110100000  
100111101101100010111100100001  
00100000000000000000000000000000  
1000000111011001111011011010101  
0000010100010010001100001000000  
10111100010100100010110100100  
1001010000100000001100110100000  
1000111011011000101101010101011  
1001000111011001101101101101000  
00001101110110110101101101001100  
00010100010110110101101101001100  
1001001111011100111110110110100  
00001000011100100011100110011000  
00000001000000100010000000000000

**Rows: Consumers** × **Columns: Attributes**

# Rows: Consumers

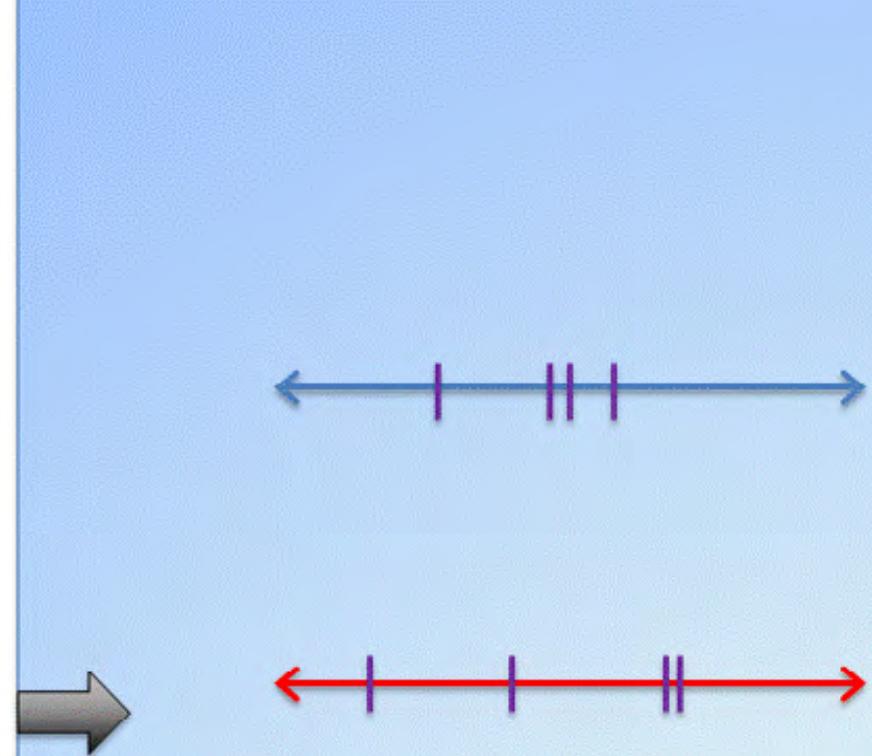
10

# Columns: Attributes

A magnifying glass with a black handle and a blue frame is positioned over a grid of binary digits (0s and 1s). The grid is arranged in 20 rows and 10 columns. The magnifying glass is centered on the 5th row and 5th column, which contains the sequence 1 1 0 0 0. The background is a light gray, and the overall image has a white border.



# Observed Variables



# Latent Variables

# Mixture of Latent Trait Models with Common Slope Parameters

Attribute  $k$ , Consumer  $i$ , Group  $g$

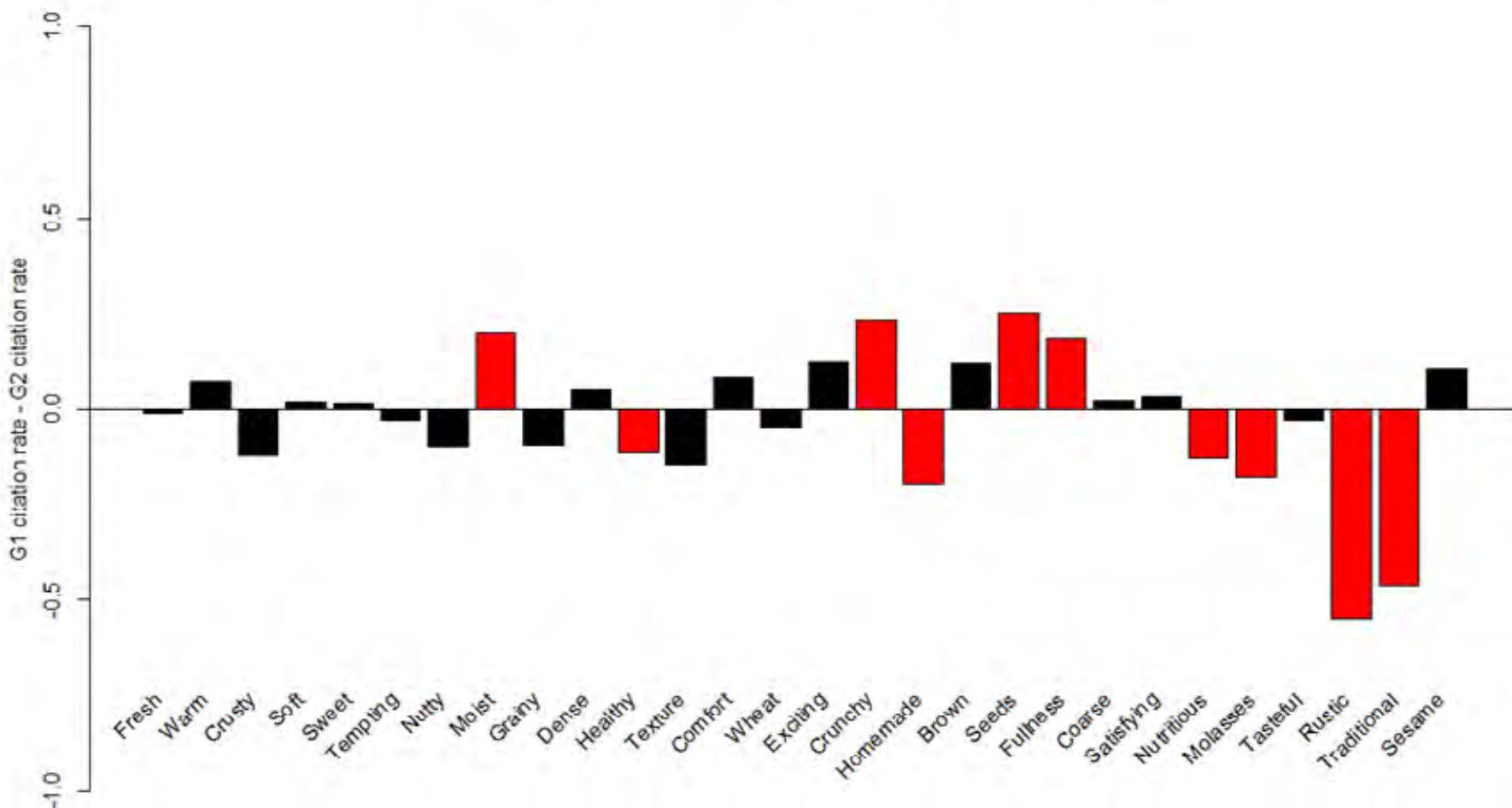
$$p(x_{ik} = 1 | y_{ig}, z_{ig} = 1) = \frac{1}{1 + \exp(-\mathbf{w}'_k y_{ig})}$$

$$Y_{ig} \sim \text{MVN}(\mu_g, \Sigma_g)$$

$$\Sigma_g = \lambda_g \mathbf{Q}_g \mathbf{A}_g \mathbf{Q}'_g$$

Volume      Orientation      Shape

### Difference in Attribute Selection Rates for the Ideal Product



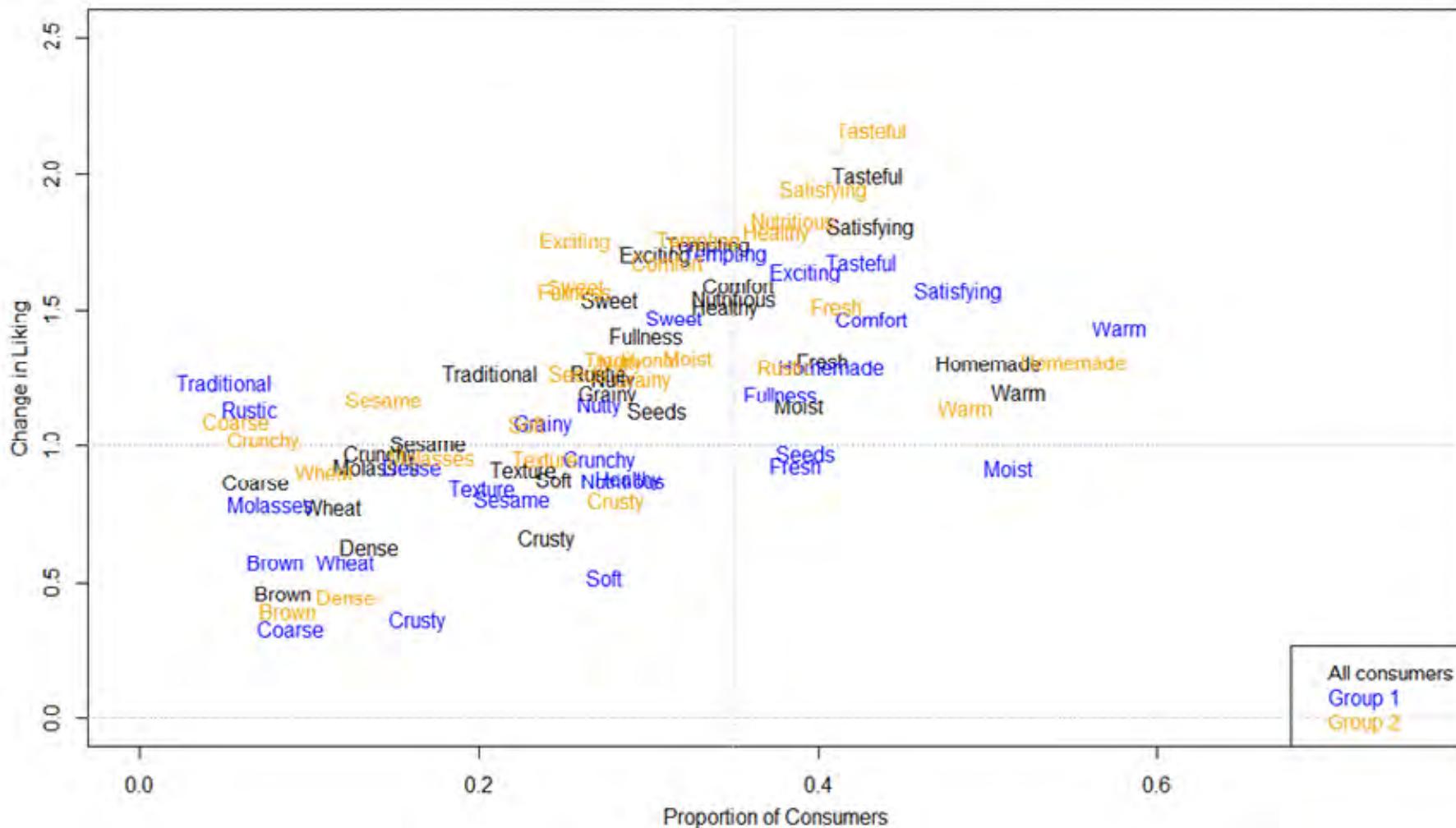
Consumers clustered by CATA profiles of an ideal bread into G1 (n=56) and G2 (n=105) via mixture of latent trait models with common slope parameters (MCLT)

BIC selects the following solution:  
**2 groups, 2 latent variables**

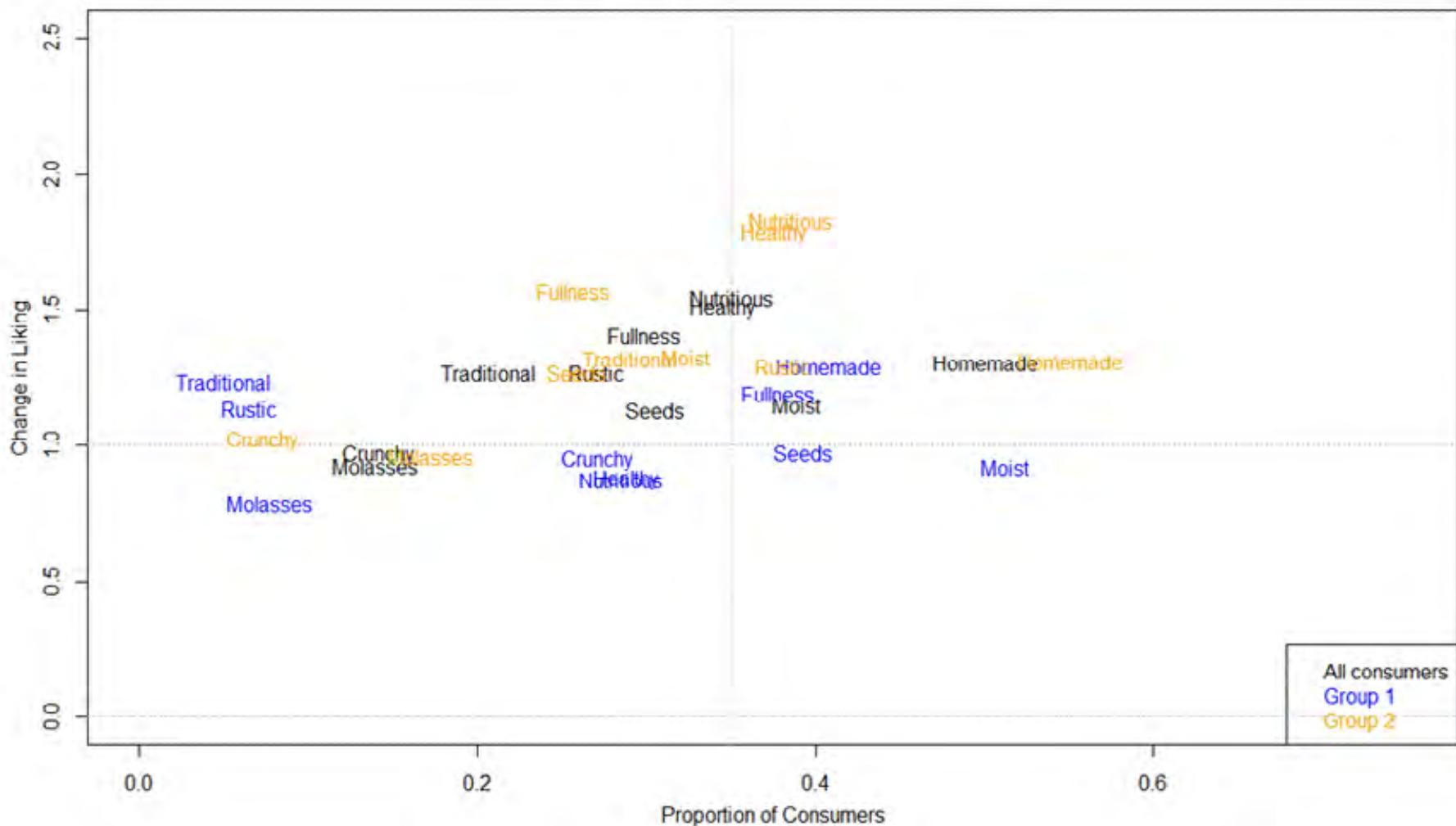
 Citation proportions differ significantly  
 Citation proportions do not differ significantly

Early results from research (in progress)

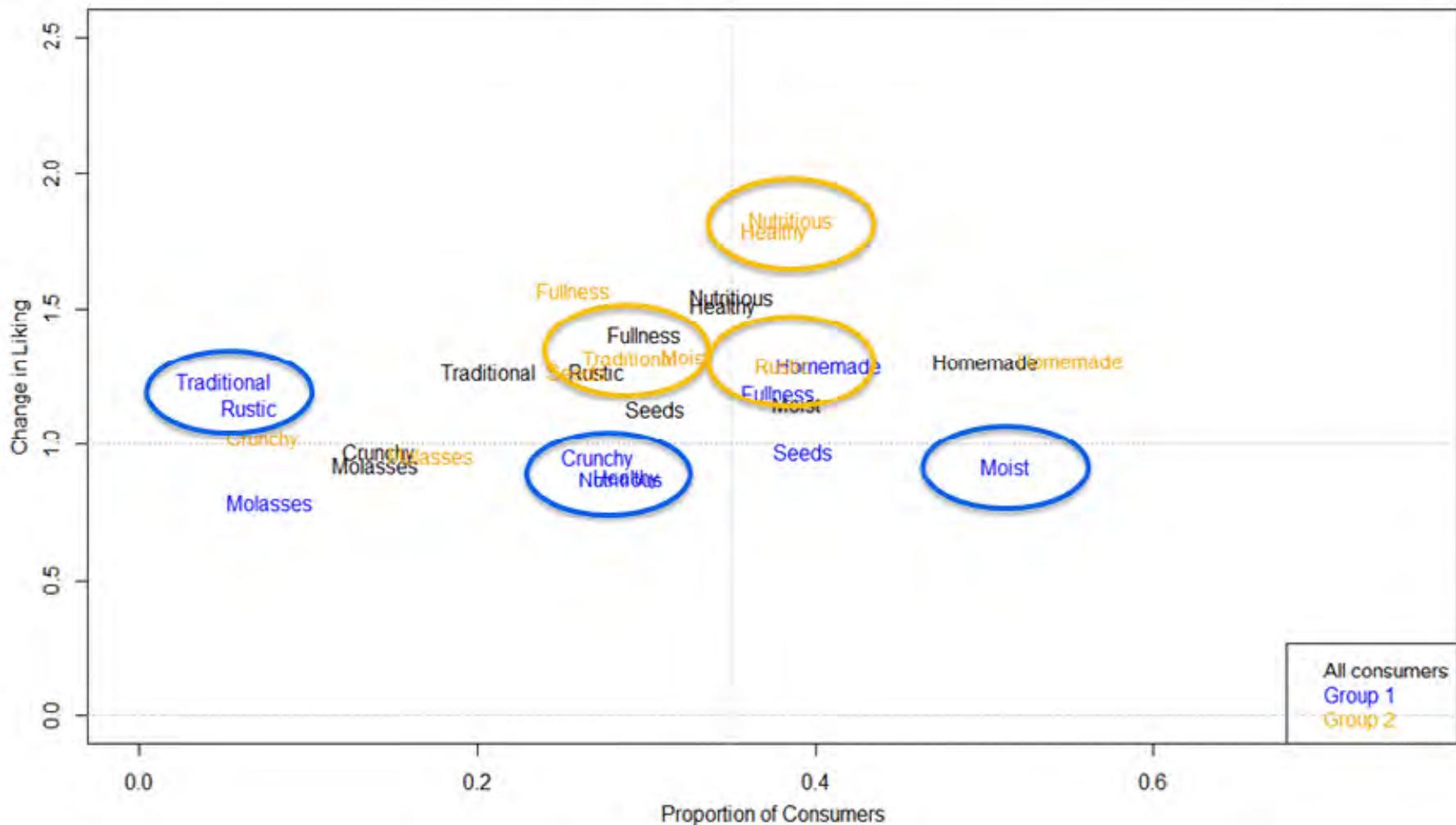
### 'Must have' attributes (ideal selected)



### 'Must have' attributes (ideal selected)



### 'Must have' attributes (ideal selected)



Check and re-check words to track changes in the cereal.



0:00

Oat flavour

Corn/corn meal flavour

Chocolate flavour

Bitter taste

Sweet taste

Peanut butter flavour

Crunchy texture

Other

# Temporal Check-all-that-apply (TCATA)

## Sample 527 (Sip 2)

After the prompt to swallow, track changes over time by checking (and re-checking) the attributes below.



0:10

Green

Earthy

Dark Fruit

Heat

Red Fruit

Bitter

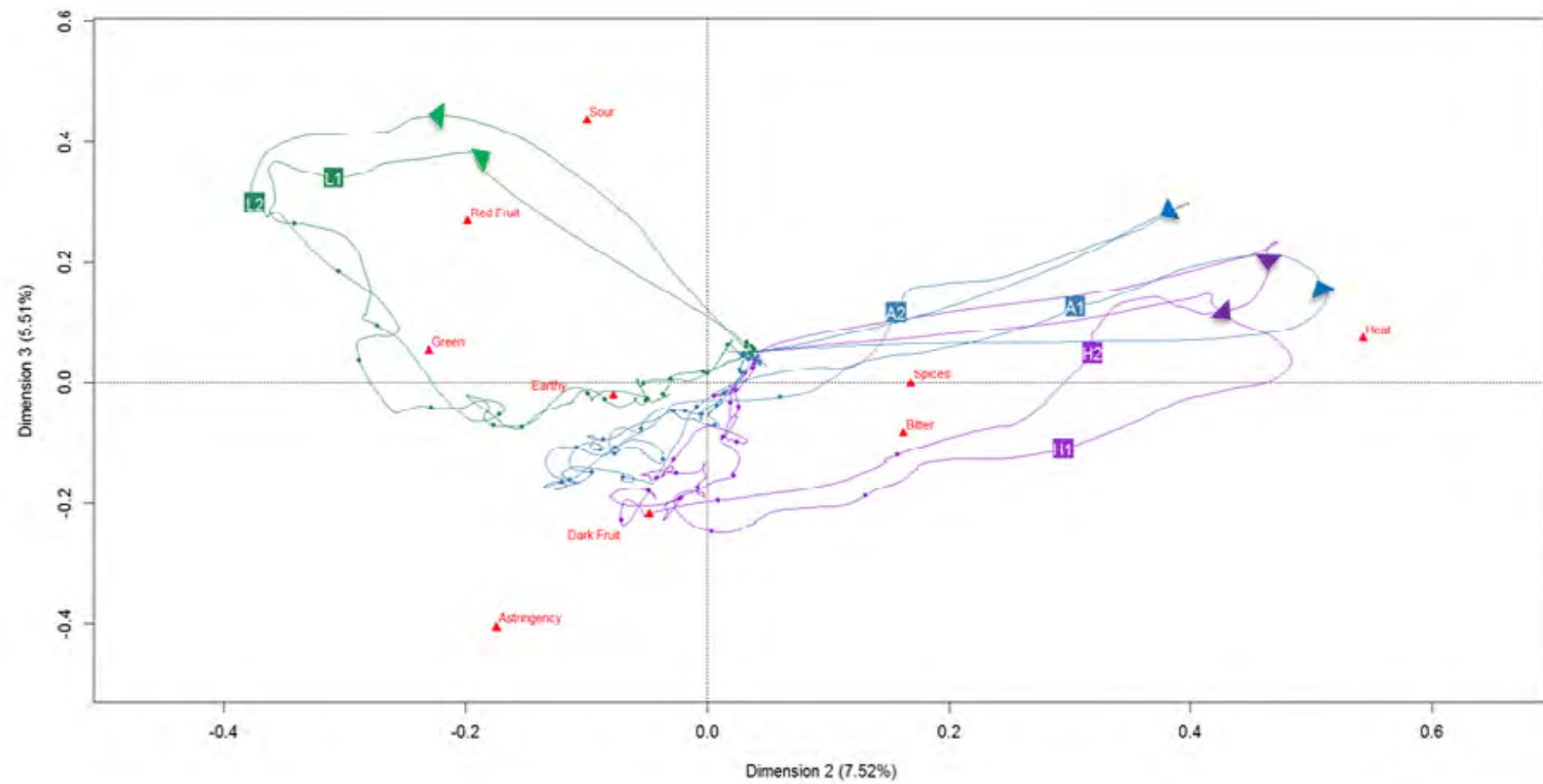
Sour

Astringency

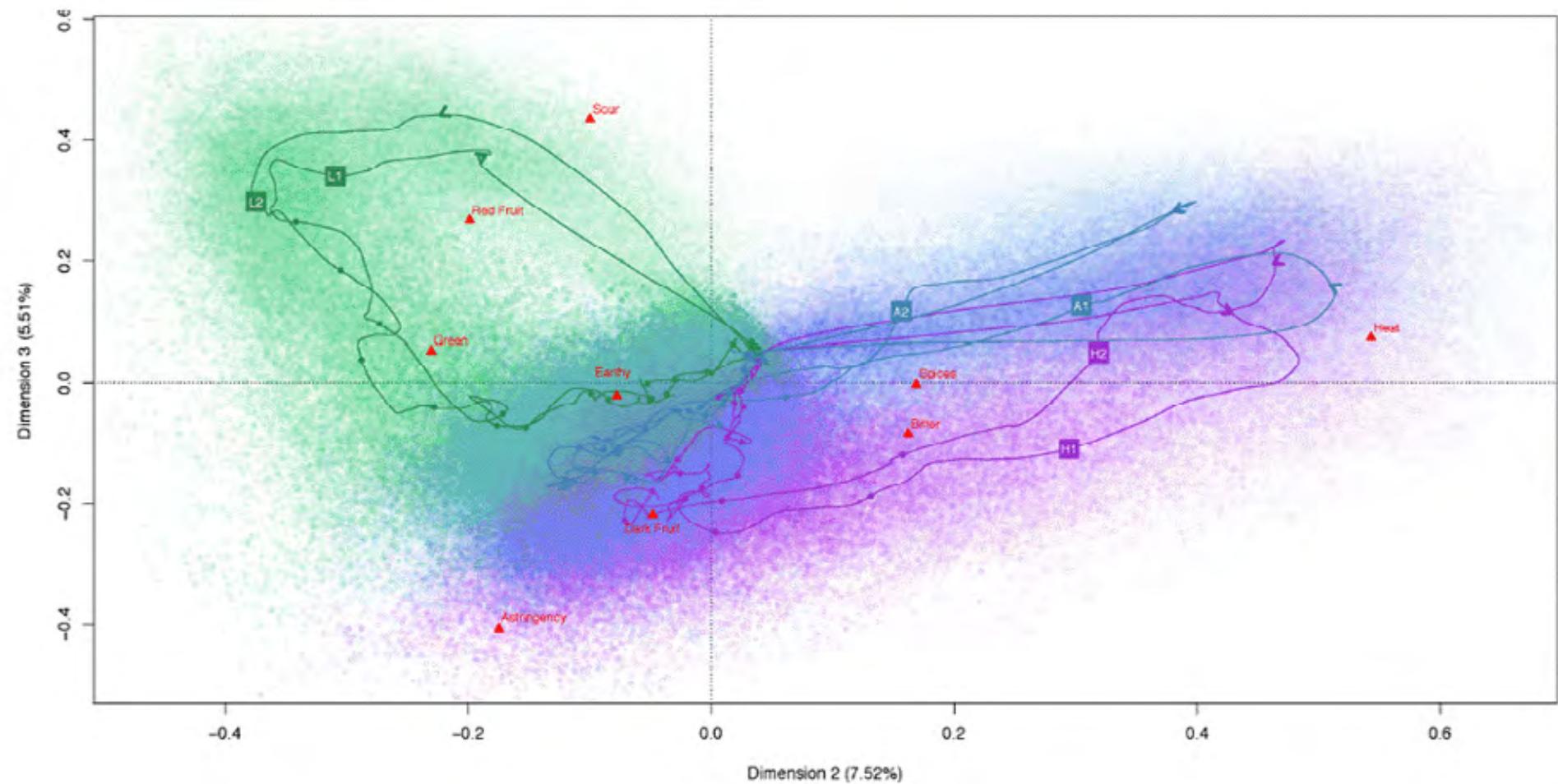
Spice

Other

# Trajectories



# Trajectories & contrails



# TCATA studies: Question order

TCATA → Liking

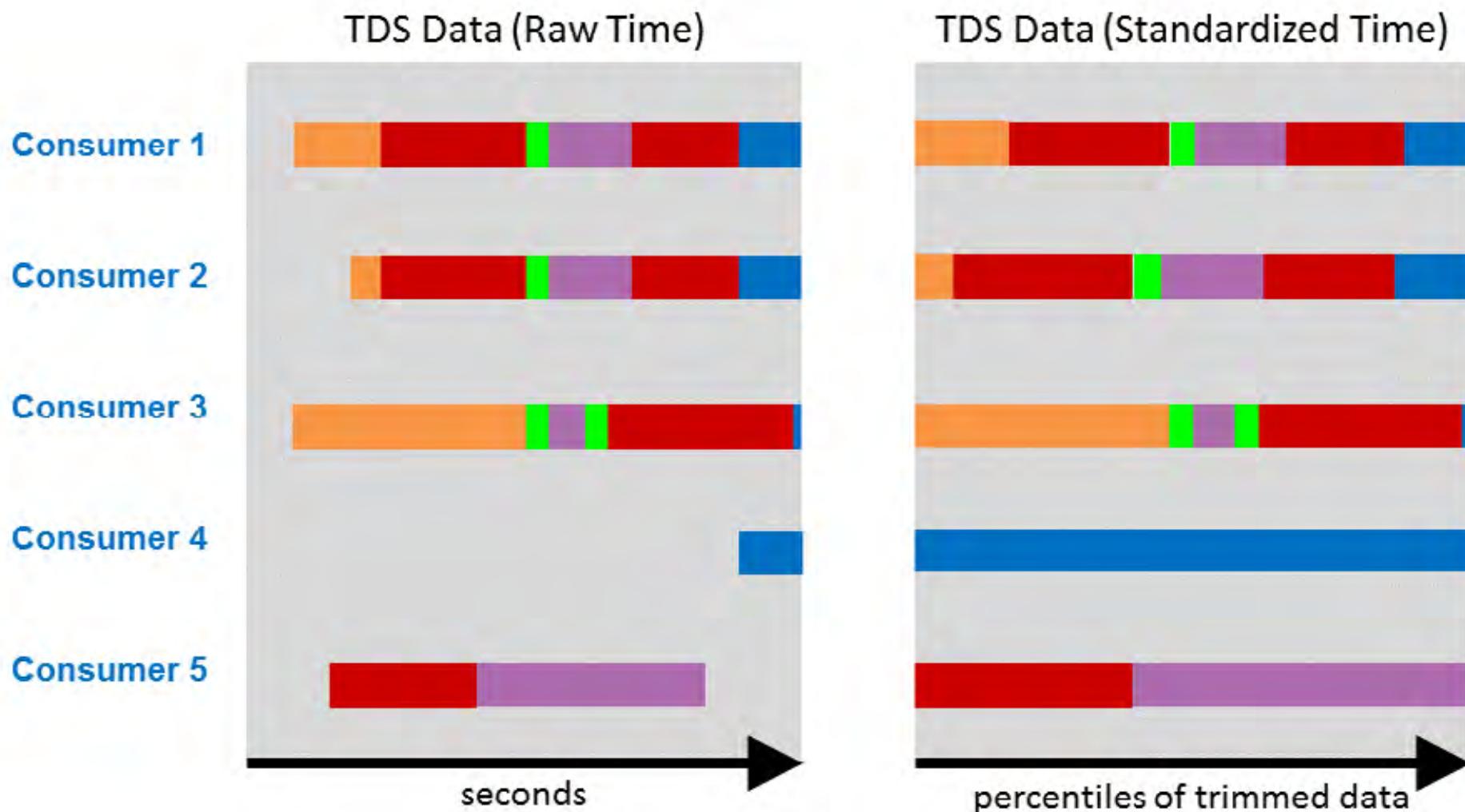
Investigate

**perception responses within  
liking clusters**

and / or

**liking responses within  
perception clusters**

# Time standardization



## Time standardization

This can have a dramatic effect on results!

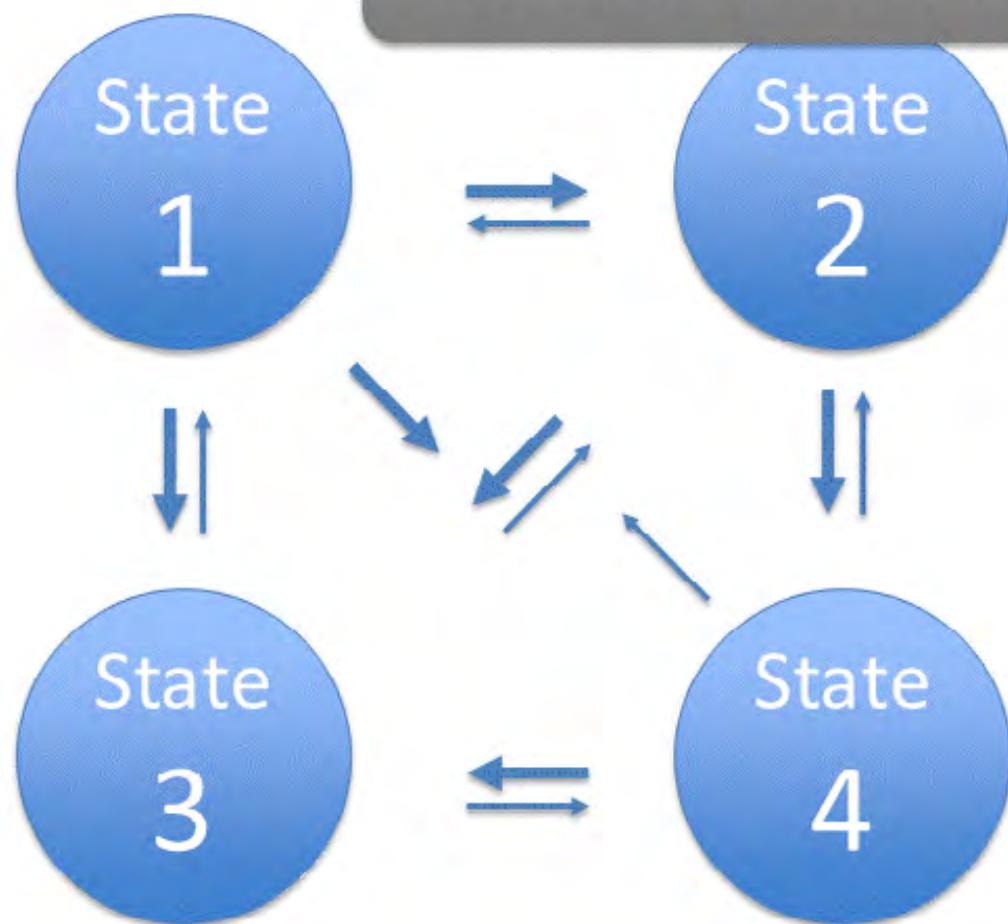
Are we **aligning** or **distorting** the data?

In TCATA evaluations of sparkling wines, **duration of perception** was found to increase with carbonation level... thus **time standardizing removes real product effects!**

**Apply with caution!**

Hidden Markov Models for clustering consumers based on dynamic (TCATA) perception data.

Research in Progress...



# Part III: Conclusion

**“A foolish consistency is  
the hobgoblin of little  
minds...”**



**Ralph Waldo Emerson**  
1841

Does a study that is designed and analyzed in a manner that is consistent with standard practices always make sense?

Of course not.

It's important to follow the design and analysis rules that need to be followed and break the rules that need to be broken.

Which rules are which?

**“Experience is knowing  
when to put your hand in  
the wood chipper.”**

**Chris Findlay**, as quoted by **John Hayes**  
at the Society of Sensory Professionals 2014 Conference  
in Tucson, Arizona

# Selected References

Browne, R.P. et al. (2013). A partial EM algorithm for clustering white breads. arXiv:1302.6625.

Castura, J.C., et al. (2016). Using contrails and animated sequences to visualize uncertainty in dynamic sensory profiles obtained from temporal check-all-that-apply (TCATA) data. *Food Quality and Preference* **54**, 90-100.

Franczak, B.C., et al. (2015). Product selection for liking studies: The sensory informed design. *Food Quality and Preference* **44**, 36–43.

Hottenstein, A.W., et al. (2008). Preference segments: A deeper understanding of consumer acceptance or a serving order effect? *Food Quality and Preference* **19**, 711–718.

Lawless, H.T., & Heymann, H. (2010). *Sensory Evaluation of Food*, Food Science Text Series, DOI 10.1007/978-1-4419-6488-5\_9, Springer Science+Business Media, LLC.

Li, M. (2014). *Model-Based Clustering for Sensory Data and Liking* (Doctoral dissertation). Retrieved from <http://atrium.lib.uoguelph.ca/xmlui/handle/10214/8108>.

McMahon, K.M., et al. (2017). Perception of carbonation in sparkling wines using descriptive analysis (DA) and temporal check-all-that-apply (TCATA). *Food Quality and Preference* **59**, 14-26.

McNicholas, P.D. (2017). *Mixture Model-Based Classification*. Boca Raton, FL: CRC Press.

Meynens, M., et al. (2013). Existing and new approaches for the analysis of CATA data. *Food Quality and Preference* **30**, 309–319.

Tang, Y., et al. (2014). Model Based Clustering of High-Dimensional Binary Data. *Computational Statistics & Data Analysis* **87**, 84-101. arXiv:1404.3174.

Wakeling, I., & Macfie, H.J.H. (1995). Designing consumer trials balanced for first and higher orders of carry-over effect when only a subset of  $k$  samples from  $t$  may be tested. *Food Quality and Preference* **6**, 299-308.

Williams, E.J. (1949). Experimental Designs Balanced for the Estimation of Residual Effects of Treatments. *Australian Journal of Scientific Research* **2**, 149-168.

# THANK YOU

# MERCI

**John C. Castura**  
VP Innovation & Research

AGROSTAT 2018, édition 2018

