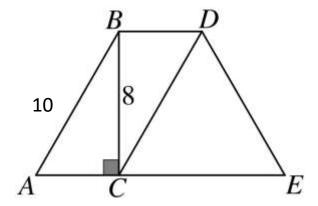
## ESM

## **Geometry (Intermediate)**

Use the information below to answer questions 1 - 3.

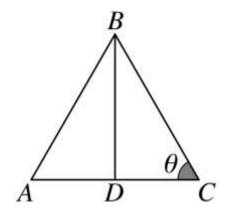
In the diagram below,  $\overline{BD} \parallel \overline{AE}$  and  $\overline{AB} \parallel \overline{CD}$  and  $\Delta CDE$  is equilateral.



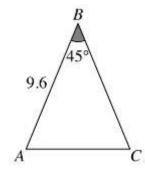
- **1.** What is the perimeter of *CBDE*?
  - **A.** 24
  - **B.** 28
  - **C.** 34
  - **D.**  $8 + \frac{40\sqrt{3}}{3}$
  - **E.**  $8 + 40\sqrt{3}$
- **2.** What is the area of *ABDC*?
  - **A.** 16
  - **B.** 24
  - **C.** 32
  - **D.** 48
  - **E.** 60
- **3.** What is the sum of  $m \angle EDC$  and  $m \angle BCE$  in degrees?
  - **A.** 120°
  - **B.** 145°
  - $\text{C. }150^{\circ}$
  - **D.** 160°
  - **E.** 170°

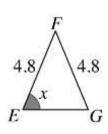


- 4. The equilateral triangle  $\triangle ABC$  is shown to the right.  $\overline{BD}$  is the perpendicular bisector of  $\overline{AC}$ , and  $\overline{BD}$  measures  $8\sqrt{3}$  inches. What is the perimeter of  $\triangle ABC$  in inches?
  - **A.** 16
  - **B.** 24
  - **C.**  $24\sqrt{3}$
  - **D.** 48
  - **E.**  $64\sqrt{3}$

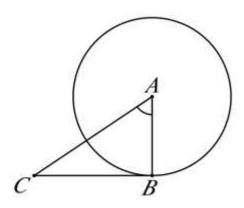


5. In the figure below,  $\triangle ABC \sim \triangle EFG$ , sides  $\overline{EF}$  and  $\overline{FG}$  are both 4.8 cm long, side  $\overline{AB}$  is 9.6 cm long, and the measure of  $\angle ABC$  is 45°. What is the measure of x?



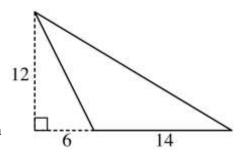


- **A.** 60°
- **B.** 65°
- **C.** 67.5°
- **D.** 72.5°
- **E.** 75°
- **6.** In the diagram to the right,  $\overline{CB}$  is tangent to circle A at point B, and  $\angle CAB = 56.49^{\circ}$ . What is the measure of  $\angle ACB$  to the nearest degree?
  - **A.** 23°
  - **B.** 29°
  - **C.** 34°
  - **D.** 37°
  - **E.** 45°

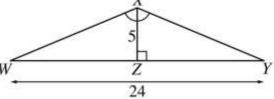




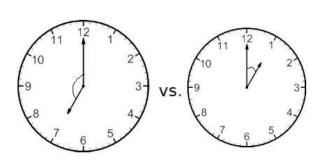
- 7. The height of the triangle to the right is 12 units. What is its area in square units?
  - **A.** 72
  - **B.** 84
  - **C.** 168
  - **D.** 240
  - E. Cannot be determined from the given information



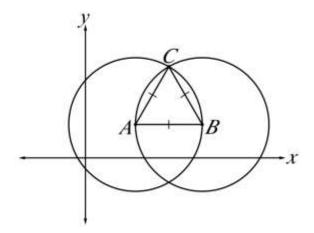
- **8.** An angle is bisected, and each of the resulting angles is trisected. The final angle measure of each resulting angle is 12.5°. What was the measure of the original angle?
  - **A.** 58°
  - **B.** 65°
  - **C.** 72°
  - **D.** 75°
  - **E.** 82°
- 9. In the figure to the right,  $\overline{XZ}$  is the perpendicular bisector of  $\Delta WXY$ , and  $\overline{WY} = 24$ . What is the ratio of the area to the perimeter of  $\Delta WXY$ ?
  - **A.** 6: 5
  - **B.** 4:3
  - **C.** 3: 5
  - **D.** 2: 3
  - **E.** 1:2



- **10.** How much larger is the smallest angle created by the hour and minute hand at 7:00 than the smallest angle created by the hour and minute hand at 1:00?
  - **A.** 100°
  - **B.** 120°
  - **C.** 130°
  - **D.** 140°
  - **E.** 150°



## Use the information below to answer questions 11 - 12



In the diagram,  $\triangle ABC$  is inscribed between two overlapping circles with center points A (3, 2) and B (7, 2).  $\triangle ABC$  is an equilateral triangle.

11. What is the circumference of the circle with center point

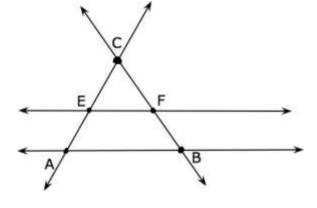
A?

- **A.** 4π
- **B.** 8π
- C.  $12\pi$
- **D.**  $14\pi$
- **E.** 16π
- **12.** What is the length of the arc between points *B* and *C* on circle *A*?
  - A.  $\frac{1}{2}\pi$
  - Β. π
  - C.  $\frac{4}{3}\pi$
  - **D.** 2π
  - **E.** 4π



**13.** In the figure to the right,  $\triangle ABC$  is an equilateral triangle.  $\overrightarrow{AB} \parallel \overrightarrow{EF}$ , E bisects  $\overrightarrow{AC}$  and F bisects  $\overrightarrow{BC}$ . What is the ratio of the area of  $\triangle EFC$  to that of  $\triangle ABC$ ?





**14.** A circle is inscribed in a square, which has a perimeter of 40 cm. What is the area of the circle?

$$\mathbf{B}.25\pi$$

$$C.40\pi$$

$$\mathbf{D}$$
.  $50\pi$ 

E. 
$$100\pi$$

**15.** Point R exists at some distance from a circle. Lines are drawn from point R and run tangent to the circle at points P and Q. If  $\angle PRQ$  is 50°, what is the measure of  $\angle RPQ$ ?

**16.** Two cylinders both have a height of 4, but the first cylinder has a radius of 3, and the second has a radius of 5. What is the ratio of the volume of these cylinders?

17. In  $\triangle ABC$ ,  $\overline{AB} = 5$  cm,  $\overline{AC} = 10$  cm,  $m \angle A = 60$ , and  $\overline{AC}$  is the longest side. Which of the following statements about the measures of the angles in  $\triangle ABC$  must be true?

**A.** 
$$m \angle A = m \angle B = m \angle C$$

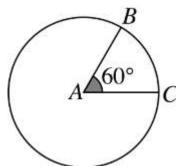
**B.** 
$$m \angle B > m \angle A > m \angle C$$

C. 
$$m \angle B = m \angle C > m \angle A$$

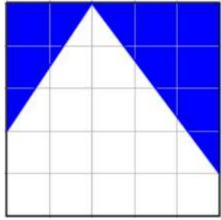
**D.** 
$$m \angle B > m \angle C = m \angle A$$

**E.** 
$$m \angle C > m \angle A > m \angle B$$

- **18.** Given the circle below with AB = 6, and  $\angle BAC = 60^{\circ}$  find the length of arc BC.
  - **A.**  $\frac{\pi}{6}$
  - $\mathbf{B}.\frac{\pi}{2}$
  - C.  $\pi$
  - D.  $2\pi$
  - E.  $6\pi$



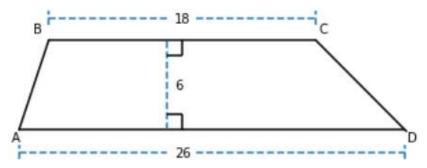
**19.** A 5-inch-by-5-inch square grid shown below is divided into 25 squares, each with a side length of 1 inch. Each vertex of the two shaded triangles lies at an intersection of 2 grid lines. What fractional part of the 5-inch-by-5-inch square is shaded?



- **A.**  $\frac{1}{3}$
- **B.**  $\frac{9}{25}$
- C.  $\frac{1}{2}$
- **D.**  $\frac{3}{5}$
- **E.**  $\frac{3}{4}$



- **20.** What is the perimeter of an isosceles right triangle with hypotenuse  $5\sqrt{2}$  feet long?
  - **A.** 10
  - **B.** 15
  - **C.** 5 +  $5\sqrt{2}$
  - **D.**  $10 + 5\sqrt{2}$
  - **E.**  $15 + 5\sqrt{2}$
- **21.** In quadrilateral ABCD shown below,  $\overline{AD} \mid \mid \overline{BC}$ , BC = 18 centimeters, AD = 26 centimeters, and the distance between  $\overline{AC}$  and  $\overline{AC}$  is 6 centimeters. What is the area, in square centimeters, of quadrilateral ABCD?



- **A.** 108
- **B.** 132
- **C.** 156
- **D.** 264
- **E.** 468