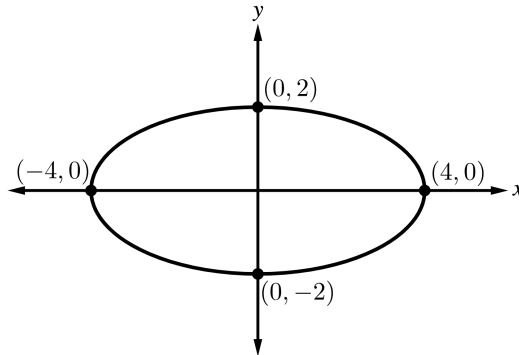


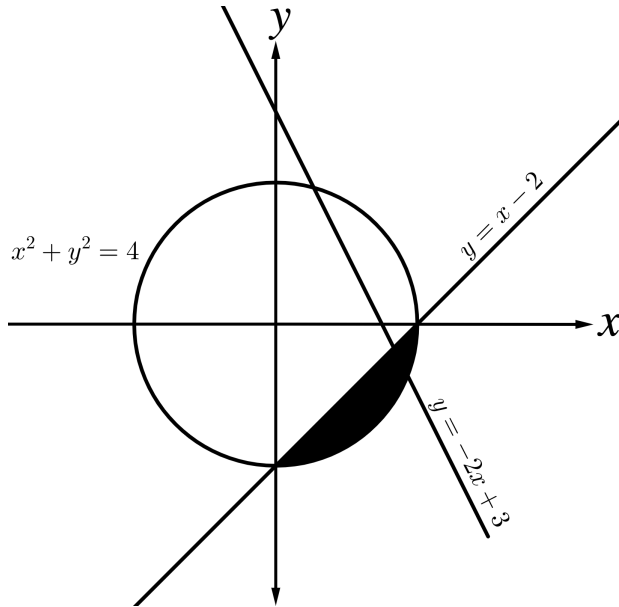
## Conic Sections

1. Which of the following equations determines the ellipse shown in the standard  $(x, y)$  coordinate plane below?



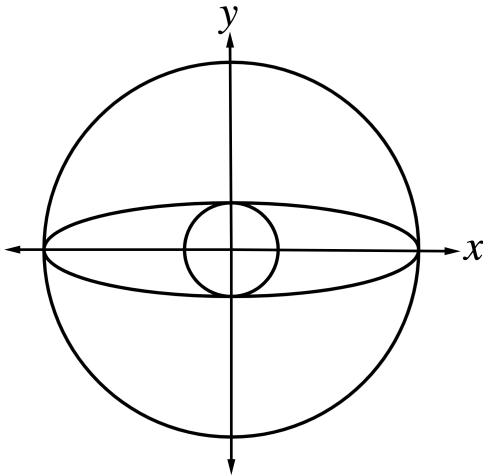
- A.  $2x^2 + 4y^2 = 8$   
B.  $4x^2 + 2y^2 = 8$   
C.  $x^2 + 4y^2 = 16$   
D.  $4x^2 + y^2 = 16$   
E.  $x^2 + 4y^2 = 64$
2. Suppose the equations  $(x - 6)^2 + (y - 10)^2 = 9$  and  $\frac{(x - 6)^2}{4} + \frac{(y - 4)^2}{9} = 1$  are graphed in the same standard  $(x, y)$  coordinate plane. How many points of intersection do these graphs share?
- A. 0  
B. 1  
C. 2  
D. 3  
E. 4

- 3 The graphs of  $y = -2x + 3$ ,  $y = x - 2$ , and  $x^2 + y^2 = 4$  are shown in the standard  $(x, y)$  coordinate plane below. The shaded region is the solution set to one of the following systems of inequalities. What system is it?



- A.  $y \leq x - 2$   
 $x^2 + y^2 \leq 4$
- B.  $y \leq x - 2$   
 $x^2 + y^2 \geq 4$
- C.  $y \leq -2x + 3$   
 $x^2 + y^2 \leq 4$
- D.  $y \geq x - 2$   
 $x^2 + y^2 \leq 4$
- E.  $y \geq -2x + 3$   
 $x^2 + y^2 \geq 4$
4. Which of the following equations is that of a circle that is in the standard  $(x, y)$  coordinate plane, has center  $(3, -6)$  and radius of 6 coordinate units?
- A.  $(x - 3) + (y + 6) = 36$
- B.  $(x + 3) + (y - 6) = 6$
- C.  $(x + 3)^2 + (y - 6)^2 = 36$
- D.  $(x - 3)^2 + (y + 6)^2 = 6$
- E.  $(x - 3)^2 + (y + 6)^2 = 36$

5. Shown below in the standard  $(x, y)$  coordinate plane are two circles and one ellipse, each centered at  $(0, 0)$ . The larger circle has equation  $x^2 + y^2 = 16$  and intersects the ellipse at exactly two points, both on the  $x$ -axis. The smaller circle has equation  $x^2 + y^2 = 1$  and intersects the ellipse at exactly two points, both on the  $y$ -axis. Which of the following equations represents the ellipse?

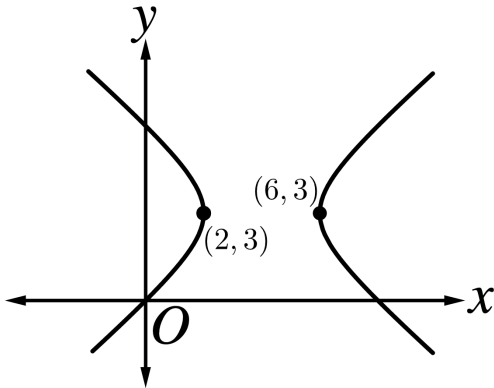


- A.  $\frac{x^2}{1} + \frac{y^2}{16} = 1$
- B.  $\frac{x^2}{1} - \frac{y^2}{16} = 1$
- C.  $\frac{x^2}{4} + \frac{y^2}{16} = 1$
- D.  $\frac{x^2}{4} - \frac{y^2}{16} = 1$
- E.  $\frac{x^2}{16} + \frac{y^2}{1} = 1$
6. The equation  $(x + 5)^2 + (y - 10)^2 = 25$  is that of a circle that lies in the standard  $(x, y)$  coordinate plane. One endpoint of a diameter of the circle has  $y$ -coordinate 6. What is the  $y$ -coordinate of the other endpoint of that diameter?
- A. -5
- B. 2
- C. 4
- D. 10
- E. 14

7. The circle with equation  $x^2 + (y - 2)^2 = 4$  is graphed in the standard  $(x, y)$  coordinate plane below. Suppose the circle rolls along the positive  $x$ -axis for 1 rotation and then stops. Which of the following is an equation of the circle in its new position?



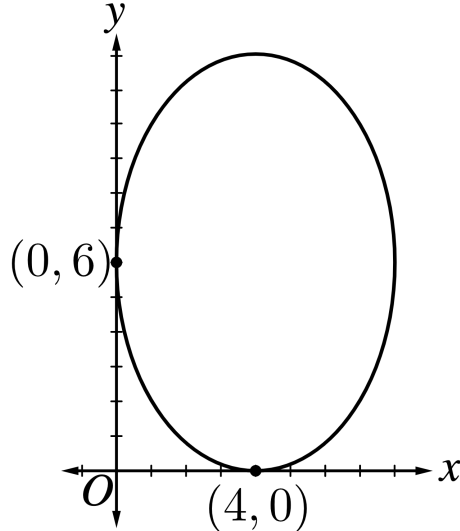
- A.  $(x - 4)^2 + (y - 2)^2 = 4$   
 B.  $(x - 2\pi)^2 + (y - 2)^2 = 4$   
 C.  $(x + 4\pi)^2 + (y - 2)^2 = 4$   
 D.  $(x - 4\pi)^2 + (y - 2)^2 = 4$   
 E.  $(x - 8\pi)^2 + (y - 2)^2 = 4$
8. A hyperbola that has vertices  $(2, 3)$  and  $(6, 3)$  and that passes through the origin is shown below in the standard  $(x, y)$  coordinate plane. The hyperbola has which of the following equations.



- A.  $\frac{(x - 4)^2}{4} - \frac{(y - 3)^2}{9} = 1$   
 B.  $\frac{(x - 4)^2}{4} - \frac{(y - 3)^2}{3} = 1$   
 C.  $\frac{(x + 4)^2}{1} - \frac{(y + 3)^2}{9} = 1$   
 D.  $\frac{(x - 4)^2}{1} + \frac{3(y - 3)^2}{4} = 1$   
 E.  $\frac{(x + 4)^2}{4} + \frac{(y + 3)^2}{3} = 1$

9. In the standard  $(x,y)$  coordinate plane, the circle centered at  $(2,4)$  that passes through  $(5,0)$  is the set of all points that are:
- A. 5 coordinate units from  $(2,4)$
  - B. equidistant from  $(2,4)$  and  $(5,0)$
  - C. 5 coordinate units from both  $(2,4)$  and  $(5,0)$
  - D. 5 coordinate units from the line segment with endpoints  $(2,4)$  and  $(5,0)$
  - E. equidistant from the line segment with endpoints  $(2,4)$  and  $(5,0)$

- 10 The ellipse shown in the standard  $(x,y)$  coordinate plane below has equation  $\frac{(x-4)^2}{16} + \frac{(y-6)^2}{36} = 1$ . Which of the following ordered pairs are the foci of the ellipse?



- A.  $(4, 2)$  and  $(4, 10)$
- B.  $(4, 6 - \sqrt{20})$  and  $(4, 6 + \sqrt{20})$
- C.  $(4, 3)$  and  $(4, 9)$
- D.  $(4 - \sqrt{20}, 6)$  and  $(4 + \sqrt{20}, 6)$
- E.  $(4 - \sqrt{52}, 6)$  and  $(4 + \sqrt{52}, 6)$