

## Non-Quadratic Polynomials

### Multiple Choice

1. The function  $y = f(x)$  is graphed in the  $xy$ -plane and crosses the  $x$ -axis at 4 distinct points. Which of the following could define the function  $f$ ?

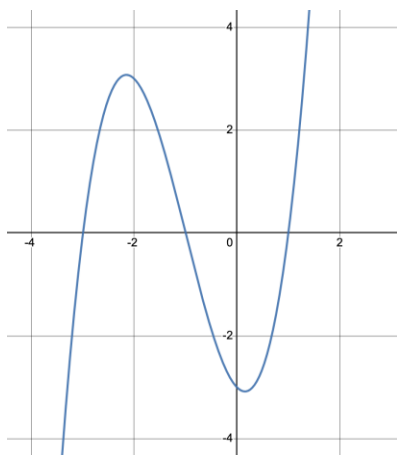
A)  $f(x) = x^4$   
B)  $f(x) = (x - 4)^2(x + 4)^2$   
C)  $f(x) = (x - 2)(x + 2)(x + 4)^2$   
D)  $f(x) = x(x - 2)(x + 2)(x + 4)$

2.  $f(x) = a(x + b)(x + c)(x + d)$

For the cubic function  $f$  shown,  $a$ ,  $b$ ,  $c$ , and  $d$  are constants. Which of the following is the value of  $f(0)$ ?

A) 0  
B)  $a$   
C)  $bcd$   
D)  $abcd$

3.



The graph of the function above is shown in the  $xy$ -plane. Which of the following could define  $f$ ?

A)  $f(x) = -(x + 3)(x + 1)(x - 1)$   
B)  $f(x) = -(x - 3)(x + 1)(x - 1)$   
C)  $f(x) = (x - 3)(x + 1)(x - 1)$   
D)  $f(x) = (x + 3)(x + 1)(x - 1)$

4.  $y = -(x - 2)(x - 3)(x - 4)$

If the given function  $h$  is graphed in the  $xy$ -plane, where  $y = h(x)$ , which of the following is an  $x$ -intercept of the graph?

- A)  $(-24, 0)$
- B)  $(-4, 0)$
- C)  $(4, 0)$
- D)  $(24, 0)$

5.  $y = -(x - 2)(x - 1)(x + 1)$

The graph in the  $xy$ -plane of the equation above contains the point  $(a, b)$ . If  $-1 \leq a \leq 1$ , which of the following is NOT a possible value of  $b$ ?

- A)  $-2$
- B)  $-1$
- C)  $0$
- D)  $1$

### Grid-In

6.  $f(x) = x^3 + 4x^2 - 5x - 2$

For the function  $f$  defined above, what is the value of  $f(-1)$ ?

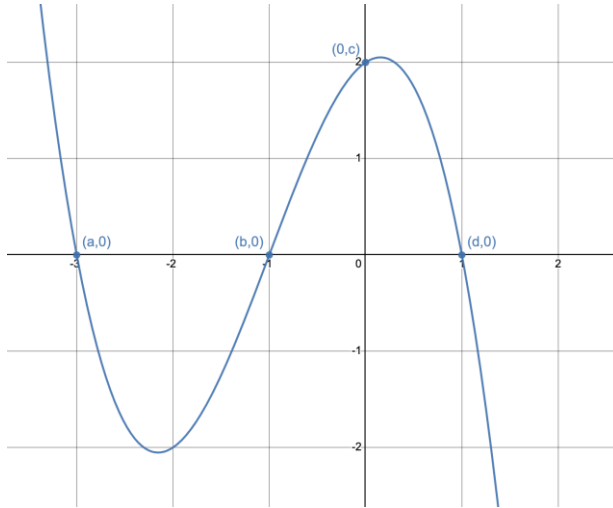
7.  $(x - 3) = (x - 4)(x - 3)$

What is the sum of the solutions to the given equation?

8.  $x(x - 8)(x + 4)(x + 9)^2 = 0$

What is the largest value of  $x$  that satisfies the given equation?

9.



The graph of the cubic polynomial function  $f$  is shown in the  $xy$ -plane, where  $y = f(x)$  and  $a, b, c$ , and  $d$  are constants. When  $f(x) = 0$ , the value of  $x$  is an integer. What is the absolute value of the smallest value of  $x$  such that  $f(x) = 0$ ?

10.

$$f(x) = x^3 + ax^2 + bx + c$$

The function  $f$  is defined above, where  $a, b$ , and  $c$  are integer constants. If the zeros of the function are  $-7$ ,  $2$ , and  $3$ , what is the value of  $c$ ?

11.

$$x(x - 8)(x + 4)(x + 9)^2 = 0$$

If  $k$  is the smallest is the value of  $x$  that satisfies the given equation, what is the value of  $|k|$ ?

12.

$$x^2(x + 4)(x - c) = 0$$

In the given equation,  $c$  is a positive constant. The sum of the solutions of the equation is  $6$ . What is the value of  $c$ ?

13. In the  $xy$ -plane, at how many points does the graph of  $f(x) = (x - 6)(x + 2)(x + 5)$  intersect the  $x$ -axis?

14.  $3(x + 6) = (x - 2)(x + 6)$

What positive value of  $x$  satisfies the given equation?

15.  $f(x) = x^3 + ax^2 + bx + c$

In the  $xy$ -plane, the graph of the cubic equation  $y = x^3 + ax^2 + bx + c$  where  $a$ ,  $b$ , and  $c$  are constants, has  $x$ -intercepts at  $x = -3$ ,  $x = -5$ , and  $x = -6$ . What is the value of  $a$  ?