

Date Completed: \_\_\_\_\_

Mentor Initials: \_\_\_\_\_

A mentor can change everything.



## Functions (Advanced)

### Multiple Choice

1. The table of values for the two functions  $f$  and  $g$  are shown below. What is the value of  $f(g(10))$ ?

| $x$ | $f(x)$ |
|-----|--------|
| -5  | 10     |
| -3  | 12     |
| 0   | 4      |
| 8   | 7      |

| $x$ | $g(x)$ |
|-----|--------|
| -3  | 4      |
| 0   | 10     |
| 10  | 0      |
| 12  | 7      |

- A) 0
- B) 4
- C) 10
- D) 12

2.  $g(x) = 3^x - 3$

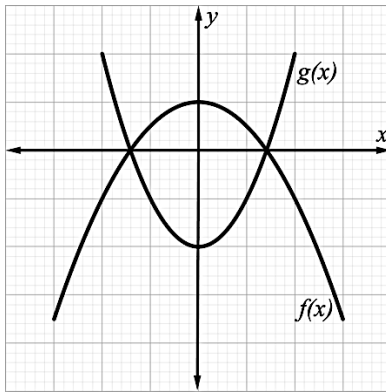
The function  $g$  is defined by the equation above. Which of the following points in the  $xy$ -plane is a  $y$ -intercept of the graph of the equation  $y = g(x)$ ?

- A)  $-3, g(-3)$
- B)  $-1, g(-1)$
- C)  $0, g(0)$
- D)  $1, g(1)$

3. Given that  $h(x) = \frac{x-2}{x^2}$ , which of the following expressions is equal to  $h(x+2)$  for all  $x$  in its domain?

- A)  $\frac{x}{x^2+4}$   
 B)  $\frac{x}{x^2+4x+4}$   
 C)  $\frac{x+2}{x^2+4}$   
 D)  $\frac{x+2}{x^2+4x+4}$

4. The graphs of  $f(x) = -\frac{1}{2}x^2 + 1$  and  $g(x) = x^2 - 2$  are shown below.



The graphs of  $f$  and  $g$  intersect at the points  $(-k, 0)$  and  $(k, 0)$ . What is the value of  $k$ ?

- A) 1.5  
 B) 2  
 C)  $\sqrt{2}$   
 D)  $\sqrt{3}$
5. The function  $h$  has the property that if point  $(j, k)$  is on the graph of the equation  $y = h(x)$  in the  $xy$ -plane, then the point  $(j+1, 4k)$  is also on the graph. Which of the following could define  $h$ ?

- A)  $h(x) = \frac{1}{4}\left(\frac{1}{15}\right)^x$   
 B)  $h(x) = 15\left(\frac{1}{4}\right)^x$   
 C)  $h(x) = 15(4)^x$   
 D)  $h(x) = \frac{1}{4}(15)^x$

**Grid-In**

6. Two functions are defined as  $f(x) = 2x^2 - 4$  and  $g(x) = -x^2 + 8$ . The graphs of  $f$  and  $g$  intersect at the points  $(-k, 4)$  and  $(k, 4)$ . What is the value of  $k$ ?

7. 
$$g(x) = kx^2 - 10x$$

For the function  $g$  above,  $k$  is a constant and  $g(2) = 4$ . What is the value of  $g(-2)$ ?

8. The table of values for the two functions  $f$  and  $g$  are shown below. What is the value of  $g(f(-3))$ ?

| $x$ | $f(x)$ |
|-----|--------|
| -5  | 10     |
| -3  | 12     |
| 0   | 4      |
| 8   | 7      |

| $x$ | $g(x)$ |
|-----|--------|
| -3  | 4      |
| 0   | 10     |
| 10  | 0      |
| 12  | 7      |

9. The function  $g$  is defined by  $g(q) = (q - 3)(q - 4)^2$ . If  $g(k - 2) = 0$ , what is one possible value of  $k$ ?

10. 
$$g(x) = ax^2 + 12$$

For the function  $g$  defined above,  $a$  is a constant, and  $g(2) = 20$ . What is the value of  $g(3)$ ?