

## The Discriminant

### Multiple Choice

1.  $3x^2 + 23x - 13 = 0$   
  
How many distinct real solutions does the given equation have?  
A) Exactly one  
B) Exactly two  
C) Infinitely many  
D) Zero
2. If the quadratic equation  $x^2 - kx + 25 = 0$  has one real solution, which of the following is a possible value of  $k$ ?  
A)  $-15$   
B)  $-5$   
C)  $0$   
D)  $10$
3. Which of the following most accurately describes the roots of  $3x^2 + 3x + 1 = 0$ ?  
A) Exactly one  
B) Exactly two  
C) Infinitely many  
D) Zero
4. For what values of  $c$  does the equation  $x^2 + cx + 4 = 0$  have no real solutions?  
A) All  $c < 0$   
B) All  $c < 4$   
C)  $0 < c < 4$   
D)  $-4 < c < 4$
5. 
$$y = x^2$$
$$px + qy = -z$$
  
  
In the above system of equations,  $p$ ,  $q$ , and  $z$  are integers. For which of the following will there be more than one real solution for the system?  
A)  $p^2 + 4qz > 0$   
B)  $q^2 - 4pz < 0$   
C)  $p^2 - 4qz > 0$   
D)  $q^2 + 4pz < 0$

**Grid-In**

6. How many real solutions does the equation  $-4x^2 - x + 3 = 0$  have?

7.  $4x^2 + bx + 169 = 0$

In the given equation,  $b$  is a positive integer. The equation has one real solution. What is the value of  $b$ ?

8.  $-x^2 + 5x + k = 0$

In the given equation,  $k$  is a constant. One of the solutions can be written as  $\frac{1}{2}(5 - \sqrt{53})$ . What is the value of  $k$ ?

9. If the quadratic equation  $-9x^2 + kx - 441 = 0$  has one real solution, what is the value of  $k$ , where  $k$  is a positive integer?

10.  $-x^2 + bx - 625 = 0$

In the given equation,  $b$  is a positive integer. The equation has no real solutions. What is the greatest possible value of  $b$ ?