



JUNIOR COLLEGE MATH MASTERY GUIDE

College

Preparatory

Mathematics

Global Sovereign University

"Building a Bridge to Freedom Through
Education—Not Handouts"

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INTRODUCTION

Welcome to Junior College Math Mastery!

This guide is designed by Global Sovereign University to prepare you for college-level mathematics. Whether you're heading to community college, university, or need math skills for your career, this guide builds the foundation you need.

Our Philosophy: College success starts with confidence in algebra and problem-solving. Master these concepts now, and higher mathematics becomes accessible, not intimidating.

Preparing for College Success

Why This Matters:

Math placement tests determine your starting college course

Higher placement = less remedial work = faster graduation

Strong math skills open doors to STEM careers

Problem-solving ability transfers to all subjects

What You'll Master:

Algebraic thinking and equation solving

Coordinate graphing and linear equations

Working with exponents and roots

Applying formulas to real problems

Translating word problems into math

How to Use This Guide

Step 1: Read concept reviews—understanding principles beats memorization

Step 2: Start with Bronze to build solid foundations

Step 3: Progress through Silver and Gold systematically

Step 4: Use answer key to learn methods, not just check answers

Step 5: Track progress toward college readiness!

Achievement Levels

◆◆ **BRONZE LEVEL** - Foundation Building Master fundamental concepts Goal: 80% accuracy

◆◆ **SILVER LEVEL** - Skill Development Apply concepts to varied problems

Goal: 80% accuracy

◆◆ **GOLD LEVEL** - College Ready Solve complex, multi-step problems Goal: 80% accuracy =
COLLEGE READY!

SECTION 1: ALGEBRA BASICS

Understanding Algebra

What is Algebra? Algebra uses letters (variables) to represent numbers we don't know yet or that can change. It's the language of mathematics.

Key Concepts:

VARIABLES: Letters that represent unknown values

x , y , n , a , b are common variables

$2x$ means "2 times x "

x^2 means " x times x "

EXPRESSIONS vs EQUATIONS:

Expression: $3x + 5$ (no equals sign)

Equation: $3x + 5 = 14$ (has equals sign)

SOLVING EQUATIONS: Goal: Get variable alone on one side

ONE-STEP EQUATIONS: $x + 5 = 12 \rightarrow$ Subtract 5 $\rightarrow x = 7$ $x - 3 = 10 \rightarrow$ Add 3 $\rightarrow x = 13$ $3x = 21 \rightarrow$ Divide by 3 $\rightarrow x = 7$ $x/4 = 5 \rightarrow$ Multiply by 4 $\rightarrow x = 20$

TWO-STEP EQUATIONS: $2x + 5 = 13$ Step 1: Subtract 5 $\rightarrow 2x = 8$ Step 2: Divide by 2 $\rightarrow x = 4$

DISTRIBUTIVE PROPERTY: $a(b + c) = ab + ac$ Example: $3(x + 4) = 3x + 12$

COMBINING LIKE TERMS: $3x + 5x = 8x$ $4y - 2y = 2y$ Cannot combine: $3x + 5y$ (different variables)

BRONZE LEVEL - ALGEBRA

Problems 1-30: One-step equations

1. $x + 8 = 15$; $x = \underline{\hspace{2cm}}$

2. $x - 6 = 12$; $x = \underline{\hspace{2cm}}$

3. $x + 11 = 28$; $x = \underline{\hspace{2cm}}$

4. $x - 9 = 17$; $x = \underline{\hspace{2cm}}$

5. $x + 14 = 35$; $x = \underline{\hspace{2cm}}$

6. $4x = 28$; $x = \underline{\hspace{2cm}}$

7. $6x = 42$; $x = \underline{\hspace{2cm}}$

8. $8x = 56$; $x = \underline{\hspace{2cm}}$

9. $10x = 90$; $x = \underline{\hspace{2cm}}$

10. $12x = 96$; $x = \underline{\hspace{2cm}}$

11. $x/3 = 7$; $x = \underline{\hspace{2cm}}$

12. $x/5 = 9$; $x = \underline{\hspace{2cm}}$

13. $x/7 = 8$; $x = \underline{\hspace{2cm}}$

14. $x/4 = 11$; $x = \underline{\hspace{2cm}}$

15. $x/6 = 10$; $x = \underline{\hspace{2cm}}$

16. $x + 15 = 42$; $x = \underline{\hspace{2cm}}$

17. $x - 13 = 25$; $x = \underline{\hspace{2cm}}$

18. $9x = 81$; $x = \underline{\hspace{2cm}}$

19. $x/8 = 6$; $x = \underline{\hspace{2cm}}$

20. $x + 22 = 50$; $x = \underline{\hspace{2cm}}$

21. $x - 18 = 31$; $x = \underline{\hspace{2cm}}$

22. $15x = 75$; $x = \underline{\hspace{2cm}}$

23. $x/9 = 7$; $x = \underline{\hspace{2cm}}$

24. $x + 19 = 45$; $x = \underline{\hspace{2cm}}$

25. $x - 14 = 28$; $x = \underline{\hspace{2cm}}$

26. $11x = 88$; $x = \underline{\hspace{2cm}}$

27. $x/12 = 5$; $x = \underline{\hspace{2cm}}$

28. $x + 25 = 60$; $x = \underline{\hspace{2cm}}$

29. $x - 16 = 34$; $x = \underline{\hspace{2cm}}$

30. $13x = 91$; $x = \underline{\hspace{2cm}}$

Problems 31-60: Two-step equations

31. $2x + 5 = 17$; $x = \underline{\hspace{2cm}}$

32. $3x - 7 = 20$; $x = \underline{\hspace{2cm}}$

33. $4x + 9 = 29$; $x = \underline{\hspace{2cm}}$

34. $5x - 12 = 23$; $x = \underline{\hspace{2cm}}$

35. $6x + 8 = 38$; $x = \underline{\hspace{2cm}}$

36. $7x - 15 = 27$; $x = \underline{\hspace{2cm}}$

37. $8x + 11 = 51$; $x = \underline{\hspace{2cm}}$

38. $9x - 18 = 36$; $x = \underline{\hspace{2cm}}$

39. $10x + 7 = 57$; $x = \underline{\hspace{2cm}}$

40. $12x - 24 = 48$; $x = \underline{\hspace{2cm}}$

41. $3x + 10 = 31$; $x = \underline{\hspace{2cm}}$

42. $4x - 8 = 24$; $x = \underline{\hspace{2cm}}$

43. $5x + 15 = 45$; $x = \underline{\hspace{2cm}}$

44. $6x - 18 = 36$; $x = \underline{\hspace{2cm}}$

45. $7x + 12 = 54$; $x = \underline{\hspace{2cm}}$

46. $8x - 16 = 40$; $x = \underline{\hspace{2cm}}$

47. $9x + 20 = 65$; $x = \underline{\hspace{2cm}}$

48. $11x - 22 = 55$; $x = \underline{\hspace{2cm}}$

49. $2x + 18 = 44$; $x = \underline{\hspace{2cm}}$

50. $3x - 12 = 21$; $x = \underline{\hspace{2cm}}$

51. $4x + 6 = 34$; $x = \underline{\hspace{2cm}}$

52. $5x - 10 = 30$; $x = \underline{\hspace{2cm}}$

53. $6x + 14 = 56$; $x = \underline{\hspace{2cm}}$

54. $7x - 21 = 35$; $x = \underline{\hspace{2cm}}$

55. $8x + 9 = 57$; $x = \underline{\hspace{2cm}}$

56. $9x - 27 = 45$; $x = \underline{\hspace{2cm}}$

57. $10x + 5 = 65$; $x = \underline{\hspace{2cm}}$

58. $12x - 30 = 54$; $x = \underline{\hspace{2cm}}$

59. $15x + 12 = 87$; $x = \underline{\hspace{2cm}}$

60. $20x - 40 = 80$; $x = \underline{\hspace{2cm}}$

SILVER LEVEL - ALGEBRA**Problems 61-90: Multi-step and distributive property**

61. $3x + 7 - 2 = 23$; $x = \underline{\hspace{2cm}}$

62. $5x - 9 + 4 = 30$; $x = \underline{\hspace{2cm}}$

63. $2(x + 5) = 24$; $x = \underline{\hspace{2cm}}$

64. $3(x - 4) = 21$; $x = \underline{\hspace{2cm}}$

65. $4(2x + 3) = 52$; $x = \underline{\hspace{2cm}}$

66. $5(3x - 2) = 55$; $x = \underline{\hspace{2cm}}$

67. $2(x + 7) + 3 = 29$; $x = \underline{\hspace{2cm}}$

68. $3(x - 5) - 4 = 17$; $x = \underline{\hspace{2cm}}$

69. $4(x + 2) = 36$; $x = \underline{\hspace{2cm}}$

70. $6(x - 3) = 42$; $x = \underline{\hspace{2cm}}$

71. $2x + 3x = 35$; $x = \underline{\hspace{2cm}}$

72. $7x - 3x = 32$; $x = \underline{\hspace{2cm}}$

73. $4x + 2x - 5 = 37$; $x = \underline{\hspace{2cm}}$

74. $6x - 2x + 8 = 36$; $x = \underline{\hspace{2cm}}$

75. $3(x + 4) = 2x + 22$; $x = \underline{\hspace{2cm}}$

76. $4(x - 2) = 3x + 5$; $x = \underline{\hspace{2cm}}$

77. $5(x + 3) = 4x + 23$; $x = \underline{\hspace{2cm}}$

78. $6(x - 1) = 5x + 7$; $x = \underline{\hspace{2cm}}$

79. $2(3x + 5) = 34$; $x = \underline{\hspace{2cm}}$

80. $3(2x - 4) = 30$; $x = \underline{\hspace{2cm}}$

81. $4(x + 6) - 5 = 43$; $x = \underline{\hspace{2cm}}$

82. $5(x - 3) + 7 = 42$; $x = \underline{\hspace{2cm}}$

83. $3(2x + 1) = 27$; $x = \underline{\hspace{2cm}}$

84. $4(3x - 2) = 40$; $x = \underline{\hspace{2cm}}$

85. $5x + 2(x + 4) = 36$; $x = \underline{\hspace{2cm}}$

86. $6x - 3(x - 2) = 24$; $x = \underline{\hspace{2cm}}$

87. $2(x + 5) + 3(x - 2) = 34$; $x = \underline{\hspace{2cm}}$

88. $4(x - 3) - 2(x + 1) = 10$; $x = \underline{\hspace{2cm}}$

89. $3(2x + 4) - 2x = 40$; $x = \underline{\hspace{2cm}}$

90. $5(x - 2) + 3x = 54$; $x = \underline{\hspace{2cm}}$

GOLD LEVEL - ALGEBRA

Problems 91-100: Advanced equations and word problems

91. $2x/3 + 5 = 17$; $x = \underline{\hspace{2cm}}$

92. $3x/4 - 6 = 12$; $x = \underline{\hspace{2cm}}$

93. $(x + 5)/2 = 8$; $x = \underline{\hspace{2cm}}$

94. $(x - 3)/4 = 5$; $x = \underline{\hspace{2cm}}$

95. $0.5x + 3.2 = 8.7$; $x = \underline{\hspace{2cm}}$

96. $0.75x - 2.5 = 7$; $x = \underline{\hspace{2cm}}$

97. $1.2x + 4.8 = 16.8$; $x = \underline{\hspace{2cm}}$

98. $2.5x - 3.5 = 11.5$; $x = \underline{\hspace{2cm}}$

99. $3(x + 4) - 2(x - 1) = 23$; $x = \underline{\hspace{2cm}}$

100. $4(2x - 3) - 3(x - 2) = 28$; $x = \underline{\hspace{2cm}}$

SECTION 2: GRAPHING & COORDINATE PLANE

Understanding Graphing

The Coordinate Plane: Two number lines that cross at right angles

Horizontal line = x-axis

Vertical line = y-axis

Where they cross = origin (0, 0)

Ordered Pairs: Points written as (x, y)

First number = x-coordinate (left/right)

Second number = y-coordinate (up/down)

Example: (3, 5) means "3 right, 5 up" from origin

Quadrants:

```

II | I
-----+-----
III | IV

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Quadrant I: Both positive (+, +)

Quadrant II: (-, +)

Quadrant III: (-, -)

Quadrant IV: (+, -)

Linear Equations: Form: $y = mx + b$

m = slope (steepness)

b = y-intercept (where line crosses y-axis)

Slope: Rise over run = Change in y / Change in x Slope between (x_1, y_1) and (x_2, y_2) : $m = (y_2 - y_1) / (x_2 - x_1)$

Types of Slope:

Positive slope: Line goes up from left to right

Negative slope: Line goes down from left to right

Zero slope: Horizontal line

Undefined slope: Vertical line

BRONZE LEVEL - GRAPHING

Problems 101-130: Identifying coordinates

What are the coordinates? 101. 3 right, 4 up = (__,) 102. 5 right, 2 up = (,) 103. 2 left, 3 up = (,) 104. 4 left, 1 up = (,) 105. 6 right, 5 down = (,) 106. 3 right, 2 down = (,) 107. 1 left, 4 down = (,) 108. 5 left, 3 down = (,) 109. Origin = (,) 110. 7 right on x-axis = (,) 111. 4 up on y-axis = (,) 112. 8 right, 1 up = (,) 113. 2 left, 6 up = (,) 114. 5 right, 7 down = (,) 115. 9 left, 2 down = (, __)

Which quadrant?

- 116. (5, 3) is in Quadrant ____
- 117. (-4, 2) is in Quadrant ____
- 118. (-3, -5) is in Quadrant ____
- 119. (6, -2) is in Quadrant ____
- 120. (7, 8) is in Quadrant ____
- 121. (-2, 9) is in Quadrant ____
- 122. (-6, -4) is in Quadrant ____
- 123. (4, -7) is in Quadrant ____
- 124. (1, 5) is in Quadrant ____
- 125. (-8, 3) is in Quadrant ____
- 126. (-5, -1) is in Quadrant ____
- 127. (9, -6) is in Quadrant ____
- 128. (3, 10) is in Quadrant ____
- 129. (-7, 4) is in Quadrant ____
- 130. (2, -8) is in Quadrant ____

SILVER LEVEL - GRAPHING

Problems 131-160: Finding slope

Find the slope between these points:

- 131. (1, 2) and (3, 6): $m =$ ____
- 132. (2, 3) and (4, 7): $m =$ ____
- 133. (0, 1) and (2, 5): $m =$ ____
- 134. (1, 4) and (3, 8): $m =$ ____
- 135. (2, 5) and (4, 9): $m =$ ____

136. (0, 0) and (3, 6): $m =$ ____
137. (1, 3) and (4, 9): $m =$ ____
138. (2, 1) and (5, 7): $m =$ ____
139. (0, 2) and (4, 10): $m =$ ____
140. (1, 5) and (4, 11): $m =$ ____
141. (1, 8) and (3, 4): $m =$ ____
142. (2, 10) and (4, 6): $m =$ ____
143. (0, 5) and (2, 3): $m =$ ____
144. (1, 7) and (3, 1): $m =$ ____
145. (2, 9) and (4, 5): $m =$ ____
146. (0, 4) and (4, 4): $m =$ ____
147. (1, 6) and (5, 6): $m =$ ____
148. (2, 3) and (6, 3): $m =$ ____
149. (0, 7) and (3, 7): $m =$ ____
150. (1, 2) and (4, 2): $m =$ ____
151. (3, 1) and (3, 5): $m =$ ____
152. (2, 4) and (2, 8): $m =$ ____
153. (5, 2) and (5, 7): $m =$ ____
154. (1, 3) and (1, 9): $m =$ ____
155. (4, 0) and (4, 6): $m =$ ____
156. (2, 1) and (5, 4): $m =$ ____
157. (1, 2) and (4, 8): $m =$ ____
158. (0, 3) and (3, 9): $m =$ ____
159. (1, 1) and (3, 7): $m =$ ____
160. (2, 4) and (6, 12): $m =$ ____

GOLD LEVEL - GRAPHING

Problems 161-180: Linear equations

Find the y-intercept (b) when $x = 0$:

161. $y = 2x + 5$; when $x=0$, $y =$ ____
162. $y = 3x - 4$; when $x=0$, $y =$ ____
163. $y = -2x + 7$; when $x=0$, $y =$ ____
164. $y = 4x + 3$; when $x=0$, $y =$ ____
165. $y = -x + 6$; when $x=0$, $y =$ ____

Find y when $x = 3$:

166. $y = 2x + 1$; $y =$ ____
167. $y = 3x - 5$; $y =$ ____

168. $y = 4x + 2$; $y = \underline{\hspace{2cm}}$

169. $y = -2x + 10$; $y = \underline{\hspace{2cm}}$

170. $y = 5x - 7$; $y = \underline{\hspace{2cm}}$

Find x when $y = 0$:

171. $y = 2x - 6$; $x = \underline{\hspace{2cm}}$

172. $y = 3x - 9$; $x = \underline{\hspace{2cm}}$

173. $y = 4x - 12$; $x = \underline{\hspace{2cm}}$

174. $y = 5x - 15$; $x = \underline{\hspace{2cm}}$

175. $y = -2x + 8$; $x = \underline{\hspace{2cm}}$

Identify slope (m) and y -intercept (b): 176. $y = 3x + 7$; $m =$, $b =$ 177. $y = -2x + 4$; $m =$, $b =$ 178. $y = 5x - 3$; $m =$, $b =$

179. $y = -4x + 9$; $m =$, $b =$ 180. $y = 6x - 8$; $m =$, $b =$

SECTION 3: EXPONENTS & ROOTS

Understanding Exponents

What are Exponents? Exponents show repeated multiplication

$$2^3 = 2 \times 2 \times 2 = 8$$

Base = 2, Exponent = 3

Exponent Rules:

MULTIPLICATION (same base): $x^a \times x^b = x^{(a+b)}$ Example: $2^3 \times 2^4 = 2^7$

DIVISION (same base): $x^a \div x^b = x^{(a-b)}$ Example: $2^5 \div 2^2 = 2^3$

POWER TO A POWER: $(x^a)^b = x^{(ab)}$ Example: $(2^3)^2 = 2^6$

ZERO EXPONENT: $x^0 = 1$ (any number to the zero power equals 1)

NEGATIVE EXPONENT: $x^{-a} = 1/x^a$ Example: $2^{-3} = 1/2^3 = 1/8$

Square Roots: \sqrt{x} asks "what number times itself equals x ?"

$$\sqrt{16} = 4 \text{ (because } 4 \times 4 = 16 \text{)}$$

$$\sqrt{25} = 5 \text{ (because } 5 \times 5 = 25 \text{)}$$

Perfect Squares: 1, 4, 9, 16, 25, 36, 49, 64, 81, 100, 121, 144, 169, 196, 225...

BRONZE LEVEL - EXPONENTS

Problems 181-210: Basic exponents

Calculate:

181. $2^2 = \underline{\hspace{2cm}}$

182. $3^2 = \underline{\hspace{2cm}}$

183. $4^2 = \underline{\hspace{2cm}}$

184. $5^2 = \underline{\hspace{2cm}}$

185. $6^2 = \underline{\hspace{2cm}}$

186. $7^2 = \underline{\hspace{2cm}}$

187. $8^2 = \underline{\hspace{2cm}}$

188. $9^2 = \underline{\hspace{2cm}}$

189. $10^2 = \underline{\hspace{2cm}}$

190. $11^2 = \underline{\hspace{2cm}}$

191. $12^2 = \underline{\hspace{2cm}}$

192. $13^2 = \underline{\hspace{2cm}}$

193. $14^2 = \underline{\hspace{2cm}}$

194. $15^2 = \underline{\hspace{2cm}}$

195. $20^2 = \underline{\hspace{2cm}}$

196. $2^3 = \underline{\hspace{2cm}}$

197. $3^3 = \underline{\hspace{2cm}}$

198. $4^3 = \underline{\hspace{2cm}}$

199. $5^3 = \underline{\hspace{2cm}}$

200. $10^3 = \underline{\hspace{2cm}}$

201. $2^4 = \underline{\hspace{2cm}}$

202. $3^4 = \underline{\hspace{2cm}}$

203. $5^4 = \underline{\hspace{2cm}}$

204. $2^5 = \underline{\hspace{2cm}}$

205. $3^5 = \underline{\hspace{2cm}}$

206. $2^6 = \underline{\hspace{2cm}}$

207. $10^4 = \underline{\hspace{2cm}}$

208. $2^7 = \underline{\hspace{2cm}}$

209. $2^8 = \underline{\hspace{2cm}}$

210. $10^5 = \underline{\hspace{2cm}}$

SILVER LEVEL - EXPONENTS

Problems 211-240: Square roots and exponent rules

Find the square root:

211. $\sqrt{4} = \underline{\hspace{2cm}}$

212. $\sqrt{9} = \underline{\hspace{2cm}}$

213. $\sqrt{16} = \underline{\hspace{2cm}}$

214. $\sqrt{25} = \underline{\hspace{2cm}}$

215. $\sqrt{36} = \underline{\hspace{2cm}}$

216. $\sqrt{49} = \underline{\hspace{2cm}}$

217. $\sqrt{64} = \underline{\hspace{2cm}}$

218. $\sqrt{81} = \underline{\hspace{2cm}}$

219. $\sqrt{100} = \underline{\hspace{2cm}}$

220. $\sqrt{121} = \underline{\hspace{2cm}}$

221. $\sqrt{144} = \underline{\hspace{2cm}}$

222. $\sqrt{169} = \underline{\hspace{2cm}}$

223. $\sqrt{196} = \underline{\hspace{2cm}}$

224. $\sqrt{225} = \underline{\hspace{2cm}}$

225. $\sqrt{1} = \underline{\hspace{2cm}}$

Multiply (add exponents):

226. $2^2 \times 2^3 = 2^{\underline{\hspace{2cm}}}$

227. $3^2 \times 3^4 = 3^{\underline{\hspace{2cm}}}$

228. $5^3 \times 5^2 = 5^{\underline{\hspace{2cm}}}$

229. $2^4 \times 2^2 = 2^{\underline{\hspace{2cm}}}$

230. $4^2 \times 4^3 = 4^{\underline{\hspace{2cm}}}$

Divide (subtract exponents):

231. $2^5 \div 2^2 = 2^{\underline{\hspace{2cm}}}$

232. $3^6 \div 3^2 = 3^{\underline{\hspace{2cm}}}$

233. $5^5 \div 5^3 = 5^{\underline{\hspace{2cm}}}$

234. $2^8 \div 2^4 = 2^{\underline{\hspace{2cm}}}$

235. $4^6 \div 4^2 = 4^{\underline{\hspace{2cm}}}$

Power to power (multiply exponents):

236. $(2^2)^3 = 2^{\underline{\hspace{2cm}}}$

237. $(3^2)^2 = 3^{\underline{\hspace{2cm}}}$

238. $(5^2)^3 = 5^{\underline{\hspace{2cm}}}$

239. $(2^3)^2 = 2^{\underline{\hspace{2cm}}}$

240. $(4^2)^2 = 4^{\underline{\hspace{2cm}}}$

GOLD LEVEL - EXPONENTS

Problems 241-250: Advanced exponent problems

241. $5^0 = \underline{\hspace{2cm}}$

242. $10^0 = \underline{\hspace{2cm}}$

243. $2^{(-2)} = \underline{\hspace{2cm}}$

244. $3^{(-2)} = \underline{\hspace{2cm}}$

245. $2^{(-3)} = \underline{\hspace{2cm}}$

246. $(2^3)^2 = \underline{\hspace{2cm}}$

247. $2^3 \times 2^2 \div 2^4 = 2^{\underline{\hspace{2cm}}}$

248. $(3^2)^3 \div 3^4 = 3^{\underline{\hspace{2cm}}}$

249. $\sqrt{(4 \times 9)} = \underline{\hspace{2cm}}$

250. $\sqrt{(16 + 9)} = \underline{\hspace{2cm}}$

SECTION 4: FORMULAS & APPLICATIONS

Understanding Formulas

Common Formulas:

GEOMETRY:

Rectangle Area: $A = lw$

Triangle Area: $A = \frac{1}{2}bh$

Circle Area: $A = \pi r^2$

Circle Circumference: $C = 2\pi r$

MOTION:

Distance: $d = rt$ (distance = rate \times time)

Rate: $r = d/t$

Time: $t = d/r$

TEMPERATURE:

Fahrenheit to Celsius: $C = (F - 32) \times 5/9$

Celsius to Fahrenheit: $F = (C \times 9/5) + 32$

BUSINESS:

Simple Interest: $I = Prt$ (Interest = Principal \times rate \times time)

Profit: $P = R - C$ (Profit = Revenue - Cost)

Using Formulas:

1. Write the formula
2. Substitute known values
3. Solve for the unknown

BRONZE LEVEL - FORMULAS

Problems 251-280: Distance, rate, time

Distance = rate \times time

251. Rate=50 mph, Time=3 hours. Distance = ____

252. Rate=60 mph, Time=2 hours. Distance = ____

253. Rate=45 mph, Time=4 hours. Distance = ____

254. Rate=55 mph, Time=5 hours. Distance = ____

255. Rate=70 mph, Time=2.5 hours. Distance = ____

256. Distance=120 mi, Time=2 hr. Rate = ____

257. Distance=180 mi, Time=3 hr. Rate = ____

258. Distance=240 mi, Time=4 hr. Rate = ____

259. Distance=300 mi, Time=5 hr. Rate = ____ 260.

Distance=150 mi, Time=2.5 hr. Rate = ____ 261.

Distance=100 mi, Rate=50 mph. Time = ____ 262.

Distance=150 mi, Rate=60 mph. Time = ____ 263.

Distance=200 mi, Rate=40 mph. Time = ____ 264.

Distance=240 mi, Rate=60 mph. Time = ____ 265.

Distance=300 mi, Rate=75 mph. Time = ____ 266.

Rate=65 mph, Time=3.5 hours. Distance = ____ 267.

Rate=72 mph, Time=2.25 hours. Distance = ____ 268.

Distance=225 mi, Time=3.75 hr. Rate = ____ 269.

Distance=350 mi, Rate=70 mph. Time = ____ 270.

Distance=420 mi, Rate=60 mph. Time = ____ 271.

Rate=80 mph, Time=1.5 hours. Distance = ____ 272.

Rate=90 mph, Time=2.5 hours. Distance = ____ 273.

Distance=280 mi, Time=4 hr. Rate = ____ 274.

Distance=360 mi, Time=6 hr. Rate = ____ 275.

Distance=480 mi, Rate=80 mph. Time = ____ 276.

Rate=55 mph, Time=6 hours. Distance = ____ 277.

Rate=65 mph, Time=4.5 hours. Distance = ____ 278.

Distance=195 mi, Time=3 hr. Rate = ____ 279.

Distance=540 mi, Rate=90 mph. Time = ____ 280.

Distance=400 mi, Rate=50 mph. Time = ____

SILVER LEVEL - FORMULAS

Problems 281-310: Area and perimeter

281. Rectangle: $l=12$, $w=8$. Area = ____

282. Rectangle: $l=15$, $w=10$. Perimeter = ____

283. Triangle: $b=10$, $h=8$. Area = ____

284. Square: $s=9$. Area = ____

285. Square: $s=12$. Perimeter = ____

286. Circle: $r=5$, $\pi \approx 3.14$. Area \approx ____

287. Circle: $r=7$, $\pi \approx 3.14$. Circumference \approx ____

288. Rectangle: $l=18$, $w=12$. Area = ____ 289.

Triangle: $b=14$, $h=10$. Area = ____ 290. Square:

$s=15$. Area = ____

291. Rectangle: $l=20$, $w=14$. Perimeter = ____

292. Triangle: $b=16$, $h=12$. Area = ____ 293.

Circle: $r=10$, $\pi \approx 3.14$. Area \approx ____ 294.

Rectangle: $l=25$, $w=16$. Area = ____ 295.

Square: $s=18$. Perimeter = ____

296. Circle: $r=8$, $\pi \approx 3.14$. Circumference \approx ____

297. Triangle: $b=20$, $h=15$. Area = ____ 298.

Rectangle: $l=30$, $w=20$. Area = ____ 299.

Circle: $r=12$, $\pi \approx 3.14$. Area \approx ____ 300. Square:

$s=20$. Area = ____

301. Rectangle: $l=22$, $w=15$. Area = ____

302. Triangle: $b=18$, $h=14$. Area = ____

303. Circle: $r=6$, $\pi \approx 3.14$. Area \approx ____

304. Rectangle: $l=28$, $w=18$. Perimeter = ____

305. Square: $s=25$. Area = ____

306. Triangle: $b=24$, $h=16$. Area = ____ 307.

Circle: $r=9$, $\pi \approx 3.14$. Circumference \approx ____ 308.

Rectangle: $l=32$, $w=24$. Area = ____ 309.

Square: $s=22$. Perimeter = ____

310. Circle: $r=15$, $\pi \approx 3.14$. Area \approx ____

GOLD LEVEL - FORMULAS

Problems 311-320: Mixed formula applications

311. Convert 86°F to Celsius. $C = (F-32) \times 5/9 =$ ____ 312.

Convert 30°C to Fahrenheit. $F = (C \times 9/5) + 32 =$ ____ 313. Simple

Interest: $P=\$1,000$, $r=5\%$ (0.05), $t=3$ years. $I =$ ____ 314. Simple

Interest: $P=\$2,500$, $r=4\%$ (0.04), $t=2$ years. $I = \underline{\hspace{1cm}}$ 315. Profit:

Revenue= $\$8,000$, Cost= $\$5,200$. Profit = $\underline{\hspace{1cm}}$ 316. A car travels

180 miles in 3 hours. Average speed = $\underline{\hspace{1cm}}$ 317. You invest

$\$5,000$ at 6% for 4 years. Interest earned = $\underline{\hspace{1cm}}$ 318. A rectangle

has area 144 sq ft and width 8 ft. Length = $\underline{\hspace{1cm}}$ 319. A circle

has circumference 62.8 ft ($\pi \approx 3.14$). Radius = $\underline{\hspace{1cm}}$ 320. You

drive 240 miles at 60 mph. Time taken = $\underline{\hspace{1cm}}$

SECTION 5: WORD PROBLEMS

Understanding Problem-Solving

Steps to Solve Word Problems:

1. **READ** carefully - understand what's being asked
2. **IDENTIFY** known and unknown values
3. **CHOOSE** the right operation or formula
4. **SOLVE** step by step
5. **CHECK** if the answer makes sense

Key Words:

ADDITION: total, sum, altogether, combined

SUBTRACTION: difference, less than, remaining

MULTIPLICATION: times, product, each, per

DIVISION: divided by, per, each, average

Translation Examples:

"5 more than x" $\rightarrow x + 5$

"3 less than x" $\rightarrow x - 3$

"twice x" $\rightarrow 2x$

"x divided by 4" $\rightarrow x/4$

"the sum of x and 7" $\rightarrow x + 7$

BRONZE LEVEL - WORD PROBLEMS

Problems 321-350: Basic word problems

321. Maria has \$45. She earns \$18 more. How much total?
322. John had \$80. He spent \$32. How much left?
323. A book costs \$15. How much for 6 books?
324. 96 students divided equally into 8 groups. Students per group?
325. Tom is 14 years old. His brother is 5 years younger. Brother's age?
326. A number increased by 12 equals 35. Find the number. 327. Three times a number is 72. Find the number.
328. A number decreased by 18 is 27. Find the number.
329. Sarah ran 3 miles on Monday and 4 miles on Tuesday. Total miles? 330. A rope is 50 feet long. 18 feet are cut off. Length remaining? 331. Each box holds 24 items. How many items in 8 boxes? 332. 144 cookies divided equally among 12 people. Cookies per person? 333. Jake has \$125. He wants to buy a \$95 jacket. Money left after purchase? 334. A number plus 23 equals 58. Find the number.
335. Five times a number is 95. Find the number.
336. A school has 450 students. 178 are boys. How many girls?
337. Movie tickets cost \$12 each. Cost for 5 tickets?
338. A car travels 180 miles in 3 hours. Average speed?
339. The sum of two numbers is 45. One number is 18. Find the other.
340. A rectangle's length is 12 and width is 8. Find area.
341. Twice a number plus 7 equals 31. Find the number.
342. Maria saved \$15 per week for 8 weeks. Total saved?
343. A pizza is cut into 12 slices. If you eat 5 slices, how many remain?

344. Three consecutive numbers sum to 75. Find the middle number.
345. A number minus 14 equals 36. Find the number.
346. The product of 8 and a number is 120. Find the number.
347. A baker makes 48 cookies per batch. How many cookies in 6 batches?
348. 216 people divided equally into 9 buses. People per bus?
349. The quotient of a number and 5 is 18. Find the number.
350. Seven more than twice a number is 29. Find the number.

SILVER LEVEL - WORD PROBLEMS

Problems 351-370: Multi-step word problems

351. Maria has \$120. She buys 3 books at \$18 each. How much left? 352. A store bought shirts for \$25 each and sold them for \$40 each. Profit per shirt? 353. John works 8 hours at \$15/hour. How much does he earn?
354. A number is tripled, then 12 is added, giving 57. Find the number. 355. The sum of three consecutive numbers is 78. Find the smallest number. 356. A rectangle's length is 3 times its width. If width is 7, find area. 357. Tom scored 85, 92, and 88 on three tests. What's his average? 358. A car rental costs \$45 per day plus \$0.25 per mile. Cost for 3 days and 120 miles? 359. The perimeter of a square is 68. Find the length of one side.
360. A number is doubled, then decreased by 15, giving 49. Find the number. 361. Maria and Jake together have \$95. Maria has \$55. How much does Jake have? 362. A triangle has base 14 and height 10. Find the area.
363. You buy 5 pounds of apples at \$2.40 per pound. Total cost?
364. The difference between two numbers is 23. The larger is 58. Find the smaller.
365. A rectangular garden is 25 feet by 18 feet. How many feet of fencing needed?
366. Three friends split a \$72 restaurant bill equally. How much each? 367. A

number increased by 40% is 84. Find the original number. 368. The product of 7 and a number, decreased by 12, is 44. Find the number. 369. A circle has radius 8. Find the area ($\pi \approx 3.14$).

370. You save \$25 per week. How many weeks to save \$450?

GOLD LEVEL - WORD PROBLEMS

Problems 371-380: Complex word problems

371. A store marks up items 40%. If an item costs \$60, what's the selling price?

372. An investment of \$2,000 earns 5% simple interest annually. How much interest after 3 years?

373. Two numbers are in ratio 3:5. Their sum is 96. Find both numbers.

374. A car travels 120 miles at 60 mph, then 180 miles at 45 mph. What's the total time? 375.

The length of a rectangle is 8 more than twice its width. If the width is 7, find the perimeter.

376. You mix 6 liters of 20% acid solution with 4 liters of 50% acid solution. What's the concentration of the mixture?

377. Maria is 3 years older than twice Jake's age. If Maria is 23, how old is Jake?

378. A box contains 5 more red marbles than blue marbles. If there are 63 marbles total and an equal number of green marbles as blue marbles, how many red marbles?

379. The temperature drops from 15°C at a rate of 2°C per hour. After how many hours will it reach -3°C ?

380. A water tank is draining at 8 gallons per minute. If it starts with 320 gallons, how many minutes until it's empty?

SECTION 6: MIXED PRACTICE

Problems 381-400: Comprehensive review

381. Solve: $3x - 7 = 20$

382. What are the coordinates: 4 right, 3 down?

383. Calculate: 5^3

384. Find the slope between (2, 3) and (6, 11)

385. $\sqrt{81} = \underline{\hspace{2cm}}$

386. Distance = 240 miles, Rate = 60 mph. Time = $\underline{\hspace{2cm}}$

387. Solve: $2(x + 5) = 28$

388. Rectangle: $l=15$, $w=9$. Area = $\underline{\hspace{2cm}}$

389. Which quadrant: $(-5, 4)$?

390. $2^4 \times 2^3 = 2^{\underline{\hspace{2cm}}}$

391. Triangle: $b=12$, $h=8$. Area = $\underline{\hspace{2cm}}$

392. Solve: $4x + 15 = 51$

393. Find y when $x=2$: $y = 3x - 5$

394. Circle: $r=6$, $\pi \approx 3.14$. Area $\approx \underline{\hspace{2cm}}$

395. Solve: $5(x - 3) = 30$

396. Convert: 50°C to Fahrenheit

397. $\sqrt{144} = \underline{\hspace{2cm}}$

398. Solve: $2x/3 = 18$

399. Profit = Revenue \$5,000 - Cost \$3,200 = $\underline{\hspace{2cm}}$

400. A number plus 15 equals 62. Find the number.

COMPLETE ANSWER KEY

[Abbreviated - Full guide would include all 400 answers with explanations]

ALGEBRA (1-100)

1. 7 31. 6 61. 6 91. 18

2. 18 32. 9 62. 7 92. 24

3. 17 33. 5 63. 7 93. 11 [continuing...]

GRAPHING (101-180)

101. (3,4) 131. 2 161. 5

102. (5,2) 132. 2 162. -4 [continuing...]

EXPONENTS (181-250)

181. 4 211. 2 241. 1

182. 9 212. 3 242. 1 [continuing...]

FORMULAS (251-320)

251. 150 mi 281. 96 311. 30°C

252. 120 mi 282. 50 312. 86°F [continuing...]

WORD PROBLEMS (321-380)

321. \$63 351. \$66 371. \$84

322. \$48 352. \$15 372. \$300 [continuing...]

MIXED (381-400)

381. $x=9$ 391. 48 396. 122°F

382. (4,-3) 392. $x=9$ 397. 12 [continuing...]

PROGRESS TRACKER

ALGEBRA: $\frac{\quad}{100} = \quad\%$ **GRAPHING:** $\frac{\quad}{80} = \quad\%$ **EXPONENTS:** $\frac{\quad}{70} = \quad\%$ **FORMULAS:**
 $\frac{\quad}{70} = \quad\%$ **WORD PROBLEMS:** $\frac{\quad}{60} = \quad\%$ **MIXED:** $\frac{\quad}{20} = \quad\%$

TOTAL: $\frac{\quad}{400} = \quad\%$

COLLEGE READINESS:

90-100%:   HONORS READY

80-89%:   COLLEGE READY

70-79%:   NEARLY READY

Below 70%: Continue practicing

Global Sovereign University Teaching People to Fish, Not Giving Them Fish

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